Vectors in Julia

Reese Pathak Keegan Go David Zeng Stephen Boyd

EE103
Stanford University

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Vectors in Julia

main topics:

- how to create and manipulate vectors in Julia
- how Julia notation differs from math notation

Outline

Vectors

- vectors are represented by arrays in Julia
- to create the 3-vector

$$x = (8, -4, 3.5) = \begin{bmatrix} 8 \\ -4 \\ 3.5 \end{bmatrix}$$

  use

  `x = [8, -4, 3.5]`

  (`x = [8;-4;3.5]` also works)
- watch out for similar looking expressions
  - `(8,-4,3.5)` and `[8 -4 3.5]` are not equivalent in Julia
- length of a vector: `length(x)`

Ranges

- to get a range from i to j (for $i \leq j$), use a colon (`:`)
  - the range from 1 to 10 is `1:10`
  - `collect(1:10)` returns the array
- the default increment between values is 1. (`1:3` is 1, 2, 3)
- to specify an increment size add an additional argument:
  - the range from 1 to 10 with a step size of 0.1 is `1:0.1:10`

Indexing and slicing

- indexes run from 1 to n: x_2 is `x[2]`
- can also set an element, *e.g.*, `x[3] = 10.5`
- use a range to select more than one element
  - `x[2:3]` selects the second and third elements
- `x[end]` selects the last element
- to select every other element use `x[1:2:end]`

Block vectors

- to form a stacked vector like

$$a = (b, c) = \begin{bmatrix} b \\ c \end{bmatrix}$$

  (with b and c vectors)

  `a = [b; c]`

  (`a = [b, c]` does NOT work)
- can mix vectors and scalars:

  `a = [b; 2; c; -6]`

Basic functions for arrays

- sum of (the entries of) a vector: `sum(x)`
- mean of the entries ($\mathbf{avg}(x)$): `mean(x)`
- 0_n is `zeros(n)`
- $\mathbf{1}_n$ is `ones(n)`

Creating unit vectors

- form e_3 with length 10
- create a zero vector of size 10 then set the third element to 1

```
e_3 = zeros(10); e_3[3] = 1;
```

List of vectors

- to form a list with vectors `a`, `b`, and `c`:

  `vector_list = [a,b,c]`
- the second vector in this list is `vector_list[2]`
- to access an element in a vector: `vertor_list[2][3]`

Outline

Vector addition and subtraction

- vector addition uses $+$, for example

$$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} + \begin{bmatrix} 4 \\ 5 \\ 6 \end{bmatrix}$$

  is written

```
[1, 2, 3] + [4, 5, 6]
```

- subtraction uses -
- the arrays must have the same length (unless one is scalar)

Scalar-vector addition

- in Julia, a scalar and a vector can be added
- the scalar is added to each entry of the vector

  `[2, 4, 8] + 3`

  gives (in mathematical notation)

$$\begin{bmatrix} 2 \\ 4 \\ 8 \end{bmatrix} + 3\mathbf{1} = \begin{bmatrix} 5 \\ 7 \\ 11 \end{bmatrix}$$

Scalar-vector multiplication

- scalar-vector multiplication uses *
- for example,

$$(-2)\begin{bmatrix} 1 \\ 9 \\ 6 \end{bmatrix}$$

  is written

```
-2 * [1, 9, 6]
```

- the other order gives the same result:

```
[1, 9, 6] * -2
```

Inner product

- inner product $a^T b$ is written as

  `dot(a,b)`
- a and b must have the same length

Outline

Norm and distance

- the norm $\|x\| = \sqrt{x_1^2 + x_2^2 + \cdots + x_n^2}$ is written `norm(x)`
- $\mathbf{dist}(x, y) = \|x - y\|$ is written `norm(x-y)`

RMS value

- $\mathbf{rms}(x)$ is defined as

$$\mathbf{rms}(x) = \sqrt{\frac{1}{n}\left(x_1^2 + \cdots + x_n^2\right)} = \frac{\|x\|}{\sqrt{n}}.$$

- can be expressed as

```
rms_x = norm(x)/sqrt(length(x))
```

Standard deviation

- standard deviation is defined as

$$\mathbf{std}(x) = \frac{\|x - \mathbf{avg}(x)\mathbf{1}\|}{\sqrt{n}}$$

- which can be expressed as

```
std_of_x = norm(x - mean(x))/sqrt(length(x))
```

- warning: the Julia function `std` does *not* use this definition

Angle

- the angle between two vectors a and b is

$$\angle(a,b) = \arccos\left(\frac{a^T b}{\|a\|\,\|b\|}\right)$$

- can be expressed as

```
angle_a_b = acos(dot(a,b)/(norm(a)*norm(b)))
```