

Scale-space representation of images (cont.)

- Non-creation of local extrema (for $f(x, y)$ and all of its partial derivatives) since $g^t(x, y) \geq 0$ and unimodal.
- Solution to diffusion equation (heat equation)

$$\frac{\partial}{\partial t} f^t(x, y) = \frac{1}{2} \nabla^2 f^t(x, y)$$

$$\begin{aligned} \frac{\partial}{\partial t} F^t(\omega_x, \omega_y) &= \frac{\partial}{\partial t} G^t(\omega_x, \omega_y) F(\omega_x, \omega_y) \\ &= \frac{\partial}{\partial t} \exp\left(-\frac{t}{2}(\omega_x^2 + \omega_y^2)\right) F(\omega_x, \omega_y) \\ &= -\frac{1}{2}(\omega_x^2 + \omega_y^2) \exp\left(-\frac{t}{2}(\omega_x^2 + \omega_y^2)\right) F(\omega_x, \omega_y) \\ &= -\frac{1}{2}(\omega_x^2 + \omega_y^2) F^t(\omega_x, \omega_y) \end{aligned}$$

t = 0.07 sec

$$\frac{\partial}{\partial t} f^t(x, y) = \frac{1}{2} \nabla^2 f^t(x, y)$$

