

# Energy-efficiency of MIMO and Cooperative MIMO Techniques in Sensor Networks

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# Outline

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# Introduction

- ▶ In sensor networks, most sensors are powered by batteries.
- ▶ Replacement of batteries is difficult and expensive.
- ▶ Energy-efficient transmission schemes are needed for data transfer.
- ▶ MIMO has been showed to achieve higher data rate under the same transmit power budget and BER performance requirements as SISO system.
- ▶ Alternatively, for the same data rate, MIMO requires less transmission energy.
- ▶ In sensor network, the total energy consumption is a summation of the transmission energy and the circuit energy.
- ▶ Our goal: Optimize both parts.

# System Model

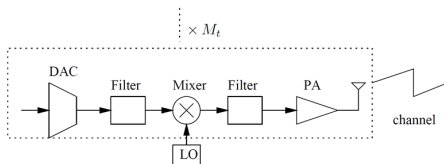


Figure: Transmitter Circuit Blocks(Analog)

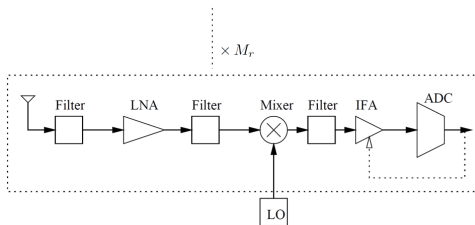


Figure: Receiver Circuit Blocks(Analog)

- ▶ The system is uncoded.
- ▶ Local oscillator is shared among all the antenna paths.
- ▶ For SISO,  $M_t = M_r = 1$ .
- ▶ Two power consumption along the signal path:
  - ▶ power consumption of all the power amplifiers  $P_{PA}$
  - ▶ power consumption of all other circuit blocks  $P_c$
- ▶ The Alamouti code is used in this paper.

# Power consumption of all the power amplifiers $P_{PA}$

$$P_{PA} = (1 + \alpha) \bar{E}_b R_b \frac{(4\pi d)^2}{G_t G_r \lambda^2} M_l N_f \quad (1)$$

where

- ▶  $\bar{E}_b$  is the required energy per bit at the receiver for a given BER requirement
- ▶  $R_b$  is the bit rate
- ▶  $G_t$  and  $G_r$  are the antenna gain at transmitter and receiver
- ▶  $\lambda$  is the carrier bandwidth
- ▶  $M_l$  is the link margin compensating the hardware process variations and other additive background noise or interference
- ▶  $N_f = \frac{N_r}{N_0}$  is the receiver noise figure with the single-sided thermal noise PSD at room temperature  $N_0$  and the PSD of the total effective noise at the receiver input  $N_r$
- ▶  $\alpha = \frac{\xi}{\eta} - 1$  with  $\eta$  the drain efficiency of the RF power amplifier and  $\xi$  the Peak to Average power ratio (PAR).

# Power consumption of all other circuit blocks $P_c$

$$P_c \approx M_t(P_{DAC} + P_{mix} + P_{filt}) + 2P_{syn} \\ + M_r(P_{LNA} + P_{mix} + P_{IFA} + P_{filr} + P_{ADC}) \quad (2)$$

$$P_{DAC} \approx \beta \left( \frac{1}{2} V_{dd} I_0 (2^{n_1} - 1) + n_1 C_p (2B + f_{cor}) V_{dd}^2 \right) \quad (3)$$

$$P_{ADC} \approx \frac{3V_{dd}^2 L_{min} (2B + f_{cor})}{10^{-0.1525n_2 + 4.838}} \quad (4)$$

where

- ▶  $V_{dd}$  is the power supply
- ▶  $I_0$  is the unit current source corresponding to the LSB
- ▶  $n_1$  and  $n_2$  are the number of significant bits at the DAC and the ADC
- ▶  $C_p$  is the parasitic capacitance
- ▶  $f_{cor}$  is the corner frequency
- ▶  $L_{min}$  is the minimum channel length for the given CMOS technology

# Fixed-rate System with BPSK Modulation: Alamouti $2 \times 1$

- ▶ For  $2 \times 1$  MISO: scalar fading matrix  $\mathbf{H} = [h_1 \quad h_2]$ .
- ▶ For SISO:  $\mathbf{H} = [h_1]$
- ▶ Instantaneous received SNR  $\gamma_b = \frac{\|\mathbf{H}\|_F^2 \bar{E}_b}{M_t N_0}$

$$\begin{aligned} \bar{P}_b &= \mathbf{E}_{\mathbf{H}} \left[ Q \left( \sqrt{2\gamma_b} \right) \right] \\ &\leq \left( \frac{\bar{E}_b}{M_t N_0} \right) \quad \text{since Chernoff bound} \end{aligned} \quad (5)$$

$$\bar{E}_b \leq \frac{M_t N_0}{\bar{P}_b^{1/M_t}} \quad (6)$$

$$E_{bt} = (P_{PA} + P_c)/R_b \quad (7)$$

$$\leq (1 + \alpha) \frac{M_t N_0}{\bar{P}_b^{1/M_t}} \times \frac{(4\pi d)^2}{G_t G_r \lambda^2} M_l N_f + P_c/R_b \quad (8)$$



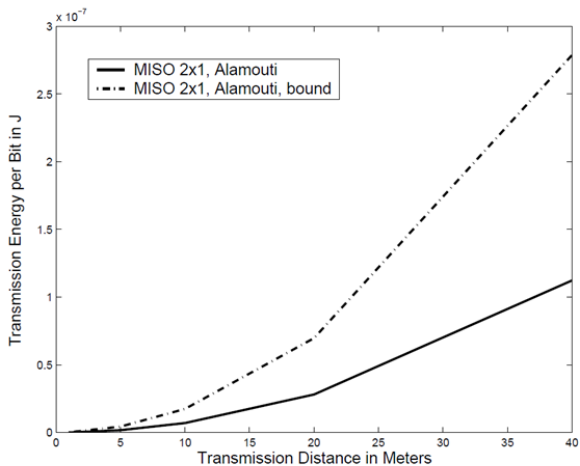


Figure: Transmission energy consumption per bit over  $d$

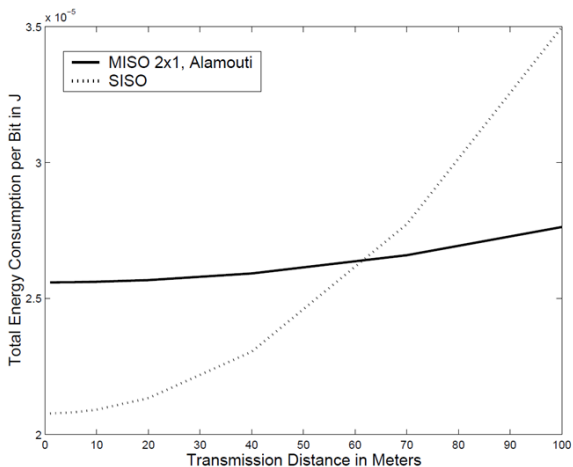


Figure: Transmission energy consumption per bit over  $d$ , MISO v.s. SISO

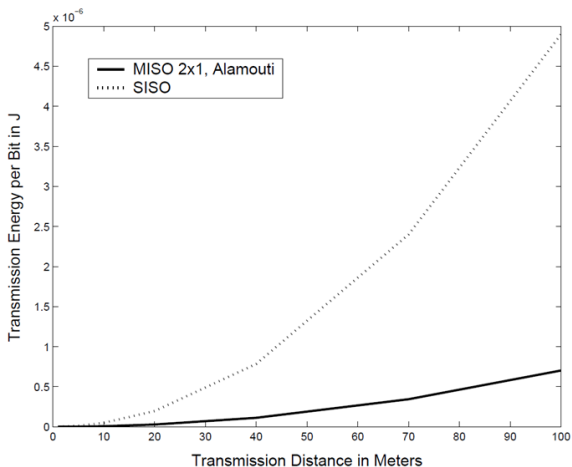


Figure: Transmission energy consumption per bit over  $d$ , MISO v.s. SISO

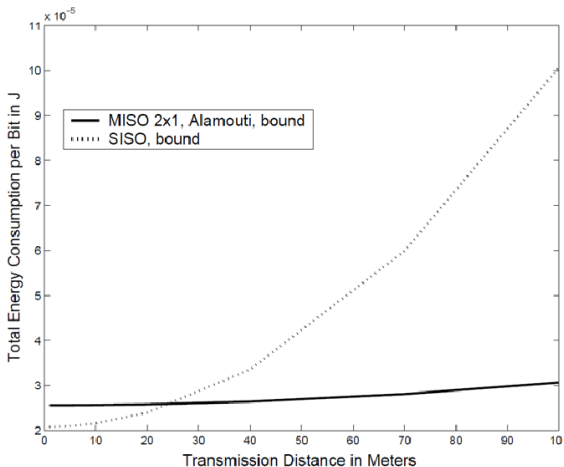


Figure: Transmission energy consumption per bit over  $d$ , MISO bound v.s. SISO bound

# Fixed-rate System with BPSK Modulation: Alamouti $2 \times 2$

- ▶  $\mathbf{H} = \begin{bmatrix} h_{11} & h_{21} \\ h_{12} & h_{22} \end{bmatrix}$
- ▶ Diversity order: 4; Array gain: 2.

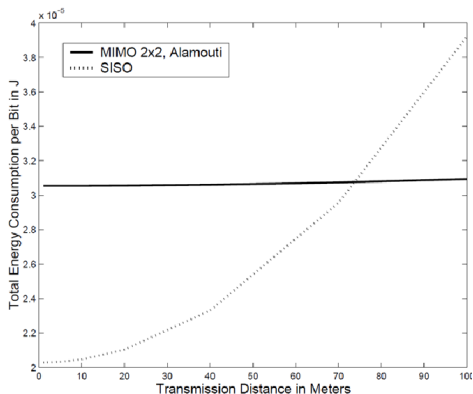


Figure: Total energy consumption over  $d$ , MIMO v.s. SISO

# Variable-rate Systems

- ▶ Optimal strategy: Operate on a multi-mode basis
- ▶ Deployment of sleep mode
- ▶ Optimize transceiver spends time  $T_{on} \leq T$
- ▶ In MQAM,  $b = \frac{L}{BT_{on}}$
- ▶ Large constellation sizes allow us to decrease  $T_{on}$  to reduce the circuit energy consumption  $E_c = P_c T_{on}$ .

$$\bar{P}_b \approx \mathbf{E}_H \left[ \frac{4}{b} \left( 1 - \frac{1}{2^{\frac{b}{2}}} \right) Q \left( \sqrt{\frac{3b}{M-1}} \gamma_b \right) \right] \quad \text{for } b \geq 2 \quad (9)$$

$$\approx \mathbf{E}_H \left[ Q \left( \sqrt{2\gamma_b} \right) \right] \quad \text{for } b = 1 \quad (10)$$

where  $M = 2^b$ . Similar with the fixed-rate system, we have

$$E_{bt} = (P_{PA} + P_c)/R_b \quad (11)$$

$$= (1 + \alpha) \bar{E}_b \times \frac{(4\pi d)^2}{G_t G_r \lambda^2} M_l N_f + P_c T_{on}/L \quad (12)$$

$$\leq \frac{2}{3} (1 + \alpha) \left( \frac{\bar{P}_b}{4} \right)^{-\frac{1}{M_t}} \frac{2^b - 1}{b^{\frac{1}{M_t} + 1}} M_t N_0 \frac{(4\pi d)^2}{G_t G_r \lambda^2} M_l N_f + \frac{P_c T_{on}}{L} \quad (13)$$

where  $T_{on} = \frac{L}{bB}$

# Optimized Alamouti $2 \times 1$

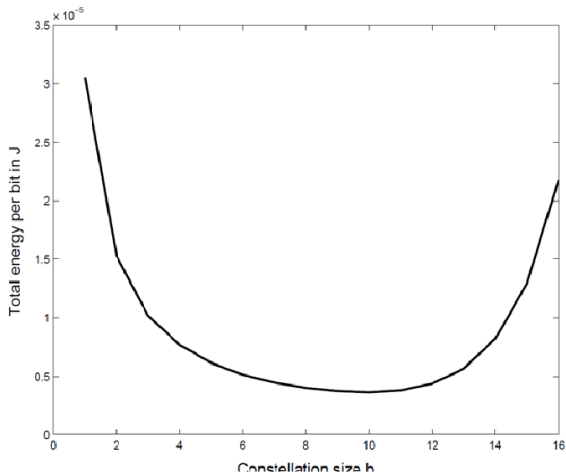


Figure: Total Energy consumption over  $b$ , MISO  $2 \times 1$



# Optimized Alamouti $2 \times 1$

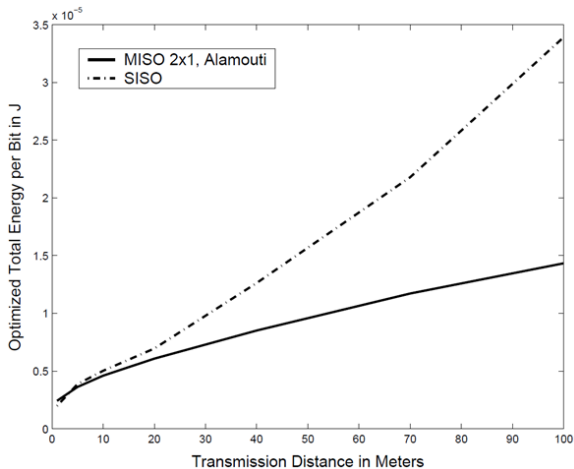


Figure: Optimized total energy consumption over  $d$ , MISO v.s. SISO

# Optimized Alamouti $2 \times 2$

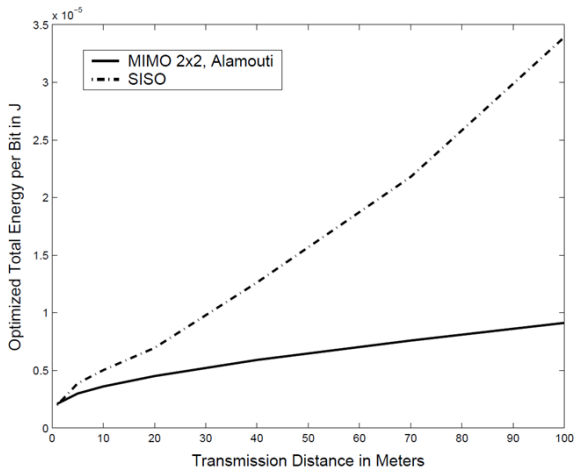


Figure: Optimized total energy consumption over  $d$ , MIMO v.s. SISO

# Optimized Alamouti $2 \times 2$

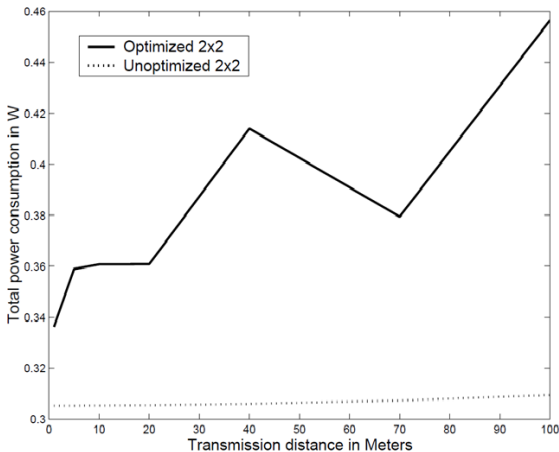


Figure: Total power consumption over  $d$ , the optimized system v.s. the unoptimized system

# MIMO with Multi-node Cooperation

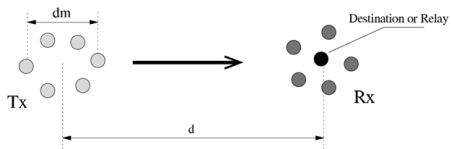


Figure: Information Flow in a sensor network

Trade-off:

- ▶ Local data exchange
- ▶ Transmission delay

- ▶  $M_t$  transmitting nodes and each has  $N_i$  bits to transmit
- ▶  $M_r$  receiving nodes (one destination node and  $M_r - 1$  assisting nodes)
- ▶ The energy cost per bit or local information flow on the Tx side is  $E_i^t$
- ▶ The energy cost per bit or local information flow on the Rx side is  $E_i^r$
- ▶ The energy cost per bit for the MIMO long-haul transmission is  $E_b^r$
- ▶ The energy cost per bit for the SISO long-haul transmission in non-cooperative approach is  $E_i^0$

# Total Energy

The total energy consumption for the non-cooperative approach:

$$E_{tra} = \sum_{i=1}^{M_t} N_i E_i^0 \quad (14)$$

The energy of cooperative approach:

$$E_{MIMO} = \sum_{i=1}^{M_t} N_i E_i^t + E_b^r \sum_{i=1}^{M_t} N_i + \sum_{j=1}^{M_r-1} E_j^r n_r N_s \quad (15)$$

where  $N_s = \frac{\sum_{i=1}^{M_t} N_i}{b_m}$

# Total Delay

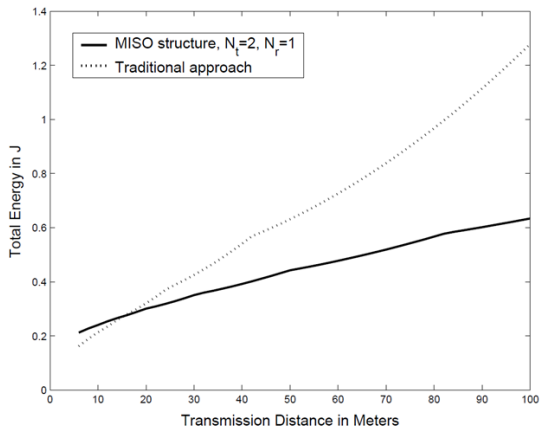
For non-cooperative approach:

$$T_{tra} = \sum_{i=1}^{M_t} \frac{N_i}{b_i^0} T_s \quad (16)$$

where  $T_s \approx 1/B$ . For cooperative approach:

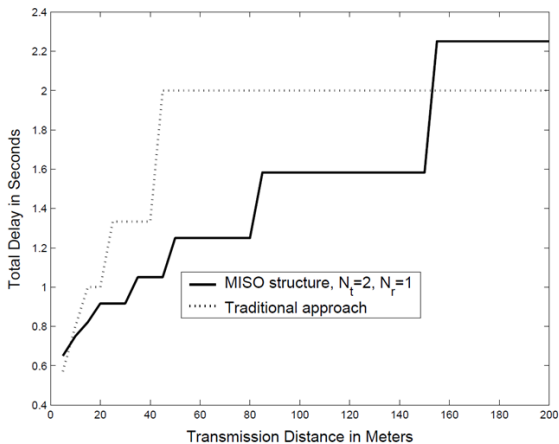
$$T_{MIMO} = T_s \left( \sum_{i=1}^{M_t} \frac{N_i}{b_i^t} + \frac{\sum_{i=1}^{M_t} N_i}{b_m} + \sum_{j=1}^{M_r-1} \frac{n_r N_s}{b_j^r} \right) \quad (17)$$

## MISO case

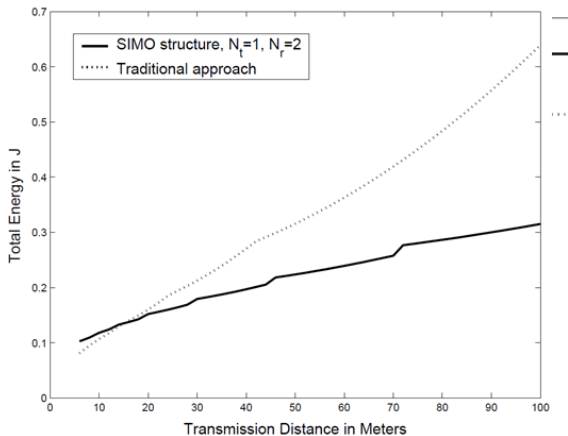
Figure: Total energy consumption over  $d$  (MISO)



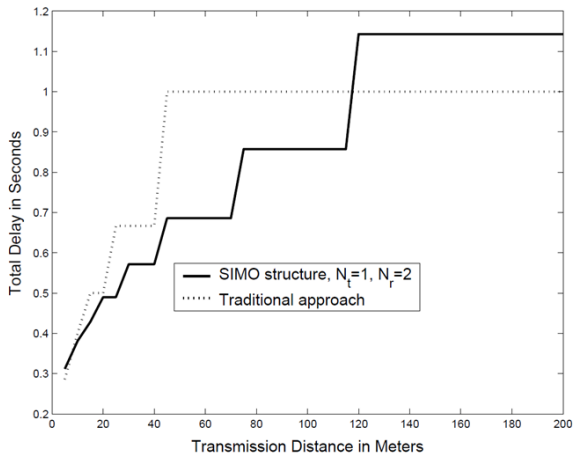
## MISO case

Figure: Total delay over  $d$  (MISO)

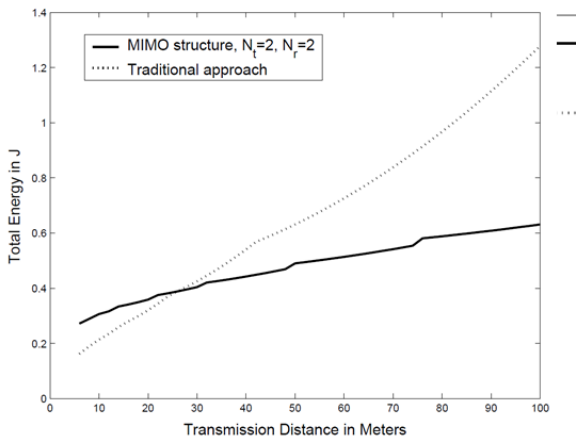
## SIMO case

Figure: Total energy consumption over  $d$  (SIMO)

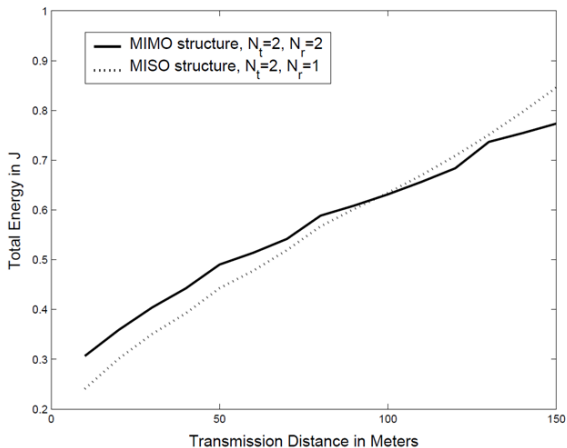
## SIMO case

Figure: Total delay over  $d$  (SIMO)

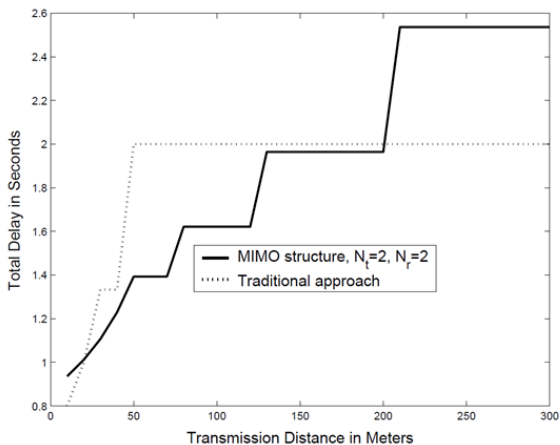
## MIMO case

Figure: Total energy consumption over  $d$  (MIMO)

## MIMO case

Figure: Total energy consumption over  $d$  (MIMO v.s. MISO)

## MIMO case

Figure: Total delay over  $d$  (MIMO)

# Conclusion

- ▶ Traditional view that MIMO are more energy-efficient than SISO is misleading when we consider both the transmission energy and the circuit energy consumptions.
- ▶ In short range, the SISO systems outperform MIMO system on the respect of energy efficiency.
- ▶ With the optimization of constellation size, MIMO can achieve better performances on the total energy consumption and the total delay.