

Increasing your confidence

~~Proving that data is  
single molecule~~

Chem 184 Lecture  
David Altman  
5/27/08

# OUTLINE

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- Brief discussion/review of single molecule fluorescence
- Statistical analysis of your fluorescence data
- Where could we go from here

# Single molecule studies come in all flavors

		technique	experimental observable	resolution of experimental observable	time resolution
structure	(local) orientation	polarization	polarization or anisotropy	> 5	ms
	short distance	quenching, ET, optical switch	intensity lifetime	< 30 Å	ms
	long distance	magnetic tweezer	force	> sub pN	ms
molecular forces/potential		optical tweezer	force	> sub pN	μs
		AFM	force	> pN	ms
		FRET	intensity lifetime	30 – 100 Å	ms
binding and assembly		FCS	correlation function	ns	ns
		coincidence	coincidence	---	ms
position/movement		particle tracking	PSF	> 1 nm	> ms

# Why single molecules?

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1. For your system, you gather a distribution as opposed to an ensemble average.
  - gives you information about inhomogeneities in your system, including the “nanoenvironment”
2. No need to synchronize a system when you are measuring a time dependent process.
3. Can observe new effects.

# Important moments in single molecule optical detection

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T. Hirschfield, Appl. Opt. 15, 2965 (1976).

Detected a single antibody labeled with 80-100 fluorophores

Moerner and Kador, Phys Rev Lett. 62, 2535 (1989).

M. Orrit and J. Bernard, Phys. Rev. Lett. 65, 2716 (1990).

Detection of a single dopant molecules in a host molecular crystal at cryogenic temperatures - pentacene in p-terphenyl crystals.

Moerner et al - absorbance

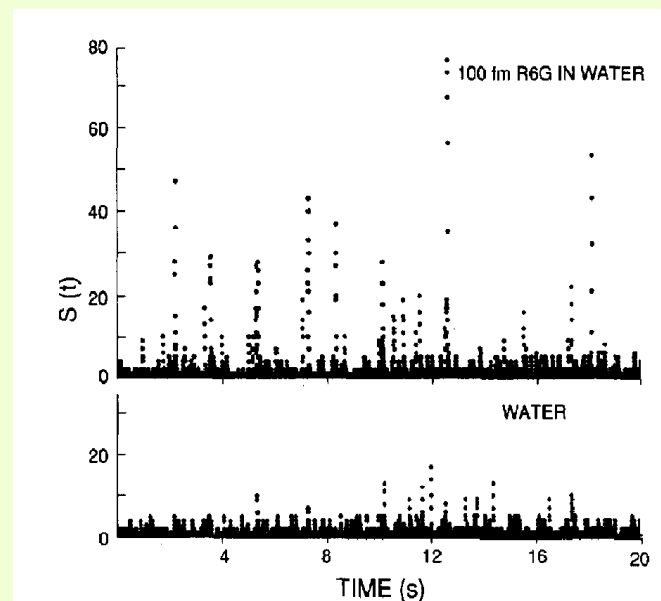
Orrit et al - fluorescence

# Important moments in single molecule optical detection

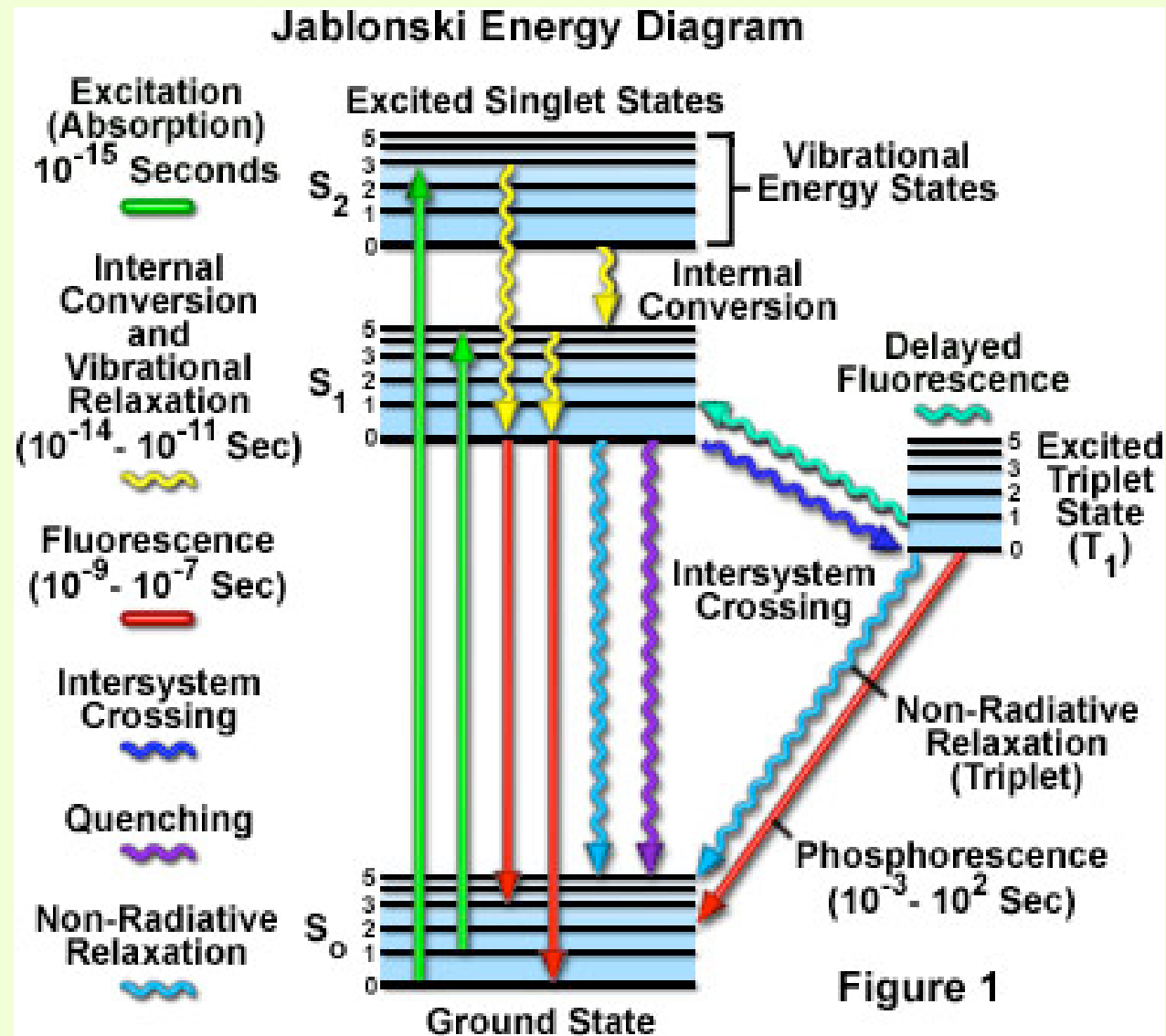
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E. B. Shera, N. K. Seizinger, L. M. Davis, R.A. Keller and S.A. Soper, *Chem. Phys. Lett.* 174, 553 (1990).

Observed Rhodamine-6G in aqueous solution at room temperature using a pulsed laser



# Single molecule fluorescence



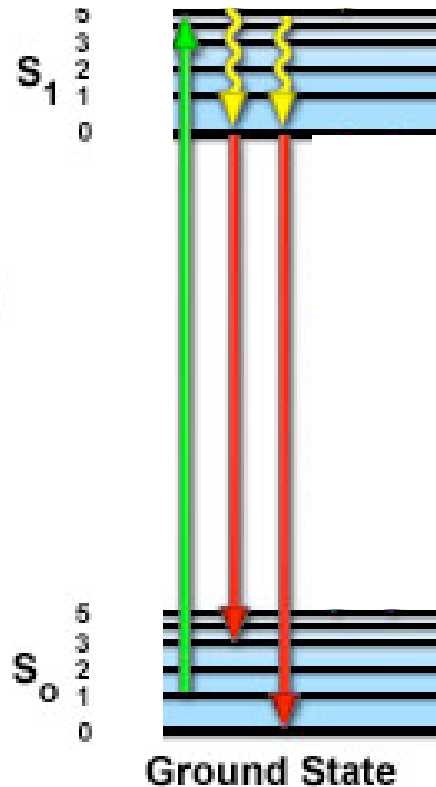
# Single molecule fluorescence

## Jablonski Energy Diagram

Excitation  
(Absorption)  
 $10^{-15}$  Seconds



Fluorescence  
( $10^{-9}$  -  $10^{-7}$  Sec)



***The rate and number of photons emitted by a fluorophore is limited.***

Figure 1

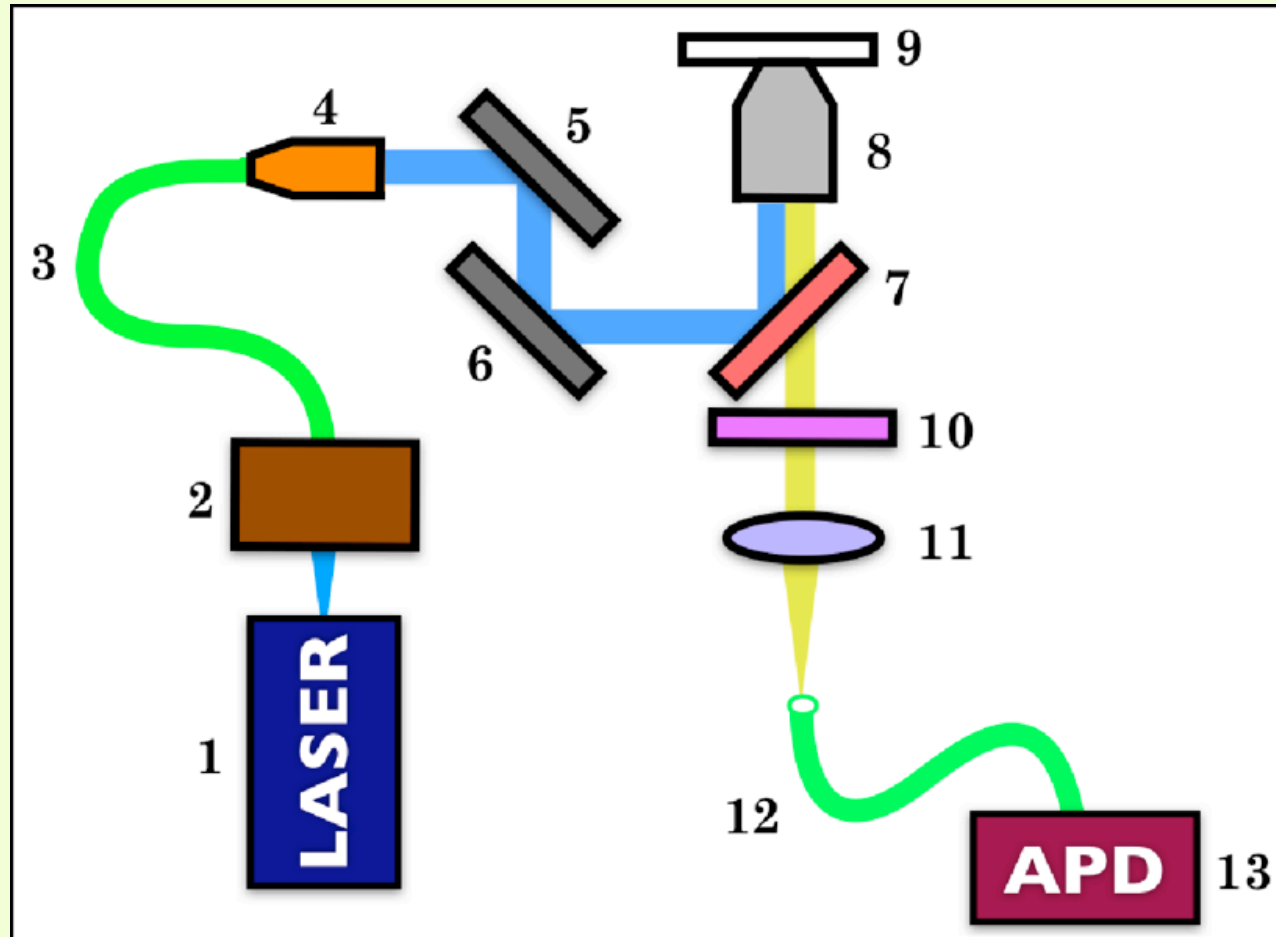


# How to make single molecule fluorescence possible

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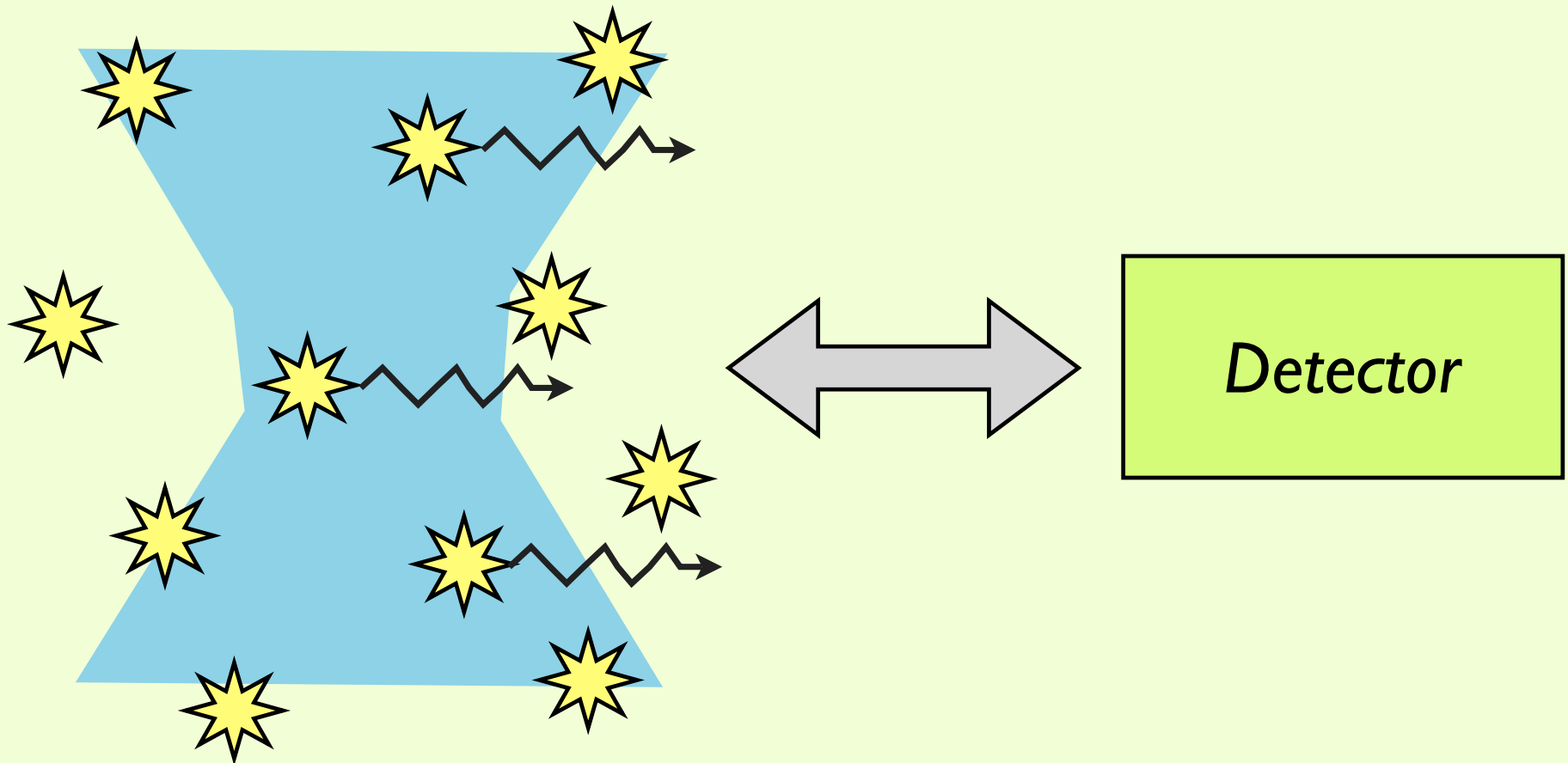
- High-efficiency, low background fluorescence detection
  - *APD single photon counting module.*
- Bright (high quantum efficiency) dyes
  - *Alexa 488 dye.*
- High efficiency optics (objectives, filters, lenses) - remove Raman scattering and scattered excitation light
  - *Nikon optics, Chroma filters.*
  - *High numerical aperture objectives collect a significant number of the emitted photons.*
- Minimal detection volume (*Background photons are a function of the detection volume*)
  - *Confocal microscopy*

# Your experimental setup

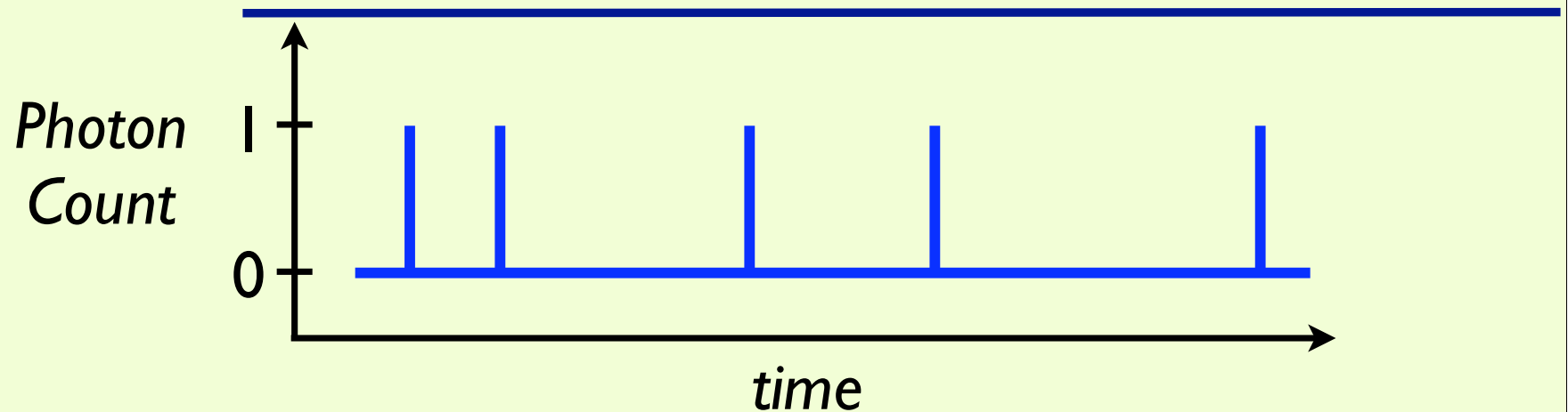


# Your experimental setup

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## Experimental time trace



What affects the frequency of photon counts?

1. How often a fluorophore enters the confocal volume.
2. How often a fluorophore absorbs and emits a photons.
3. How often a fluorophore exits the confocal volume.
4. Background - *“Dark counts” from detection device, light from the room, scattered light.*

## We assume these are Poisson processes

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*Random independent process - the occurrence of one event has no effect on the occurrence of another.*

- $N$  events are detected in measurement time interval  $dT$ .
- The expected rate of a Poisson process is  $\mu$ .

$$\left\langle \frac{N}{dT} \right\rangle = \mu$$

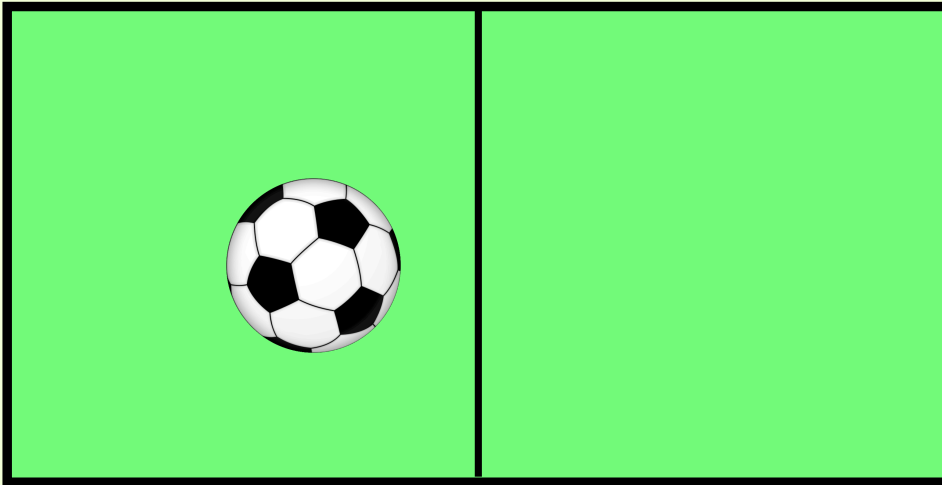
**How can you tell whether a process is Poissonian?**

Measure  $N/dT$  again and again.

Does the rate of occurrence change?

# The time scale is important

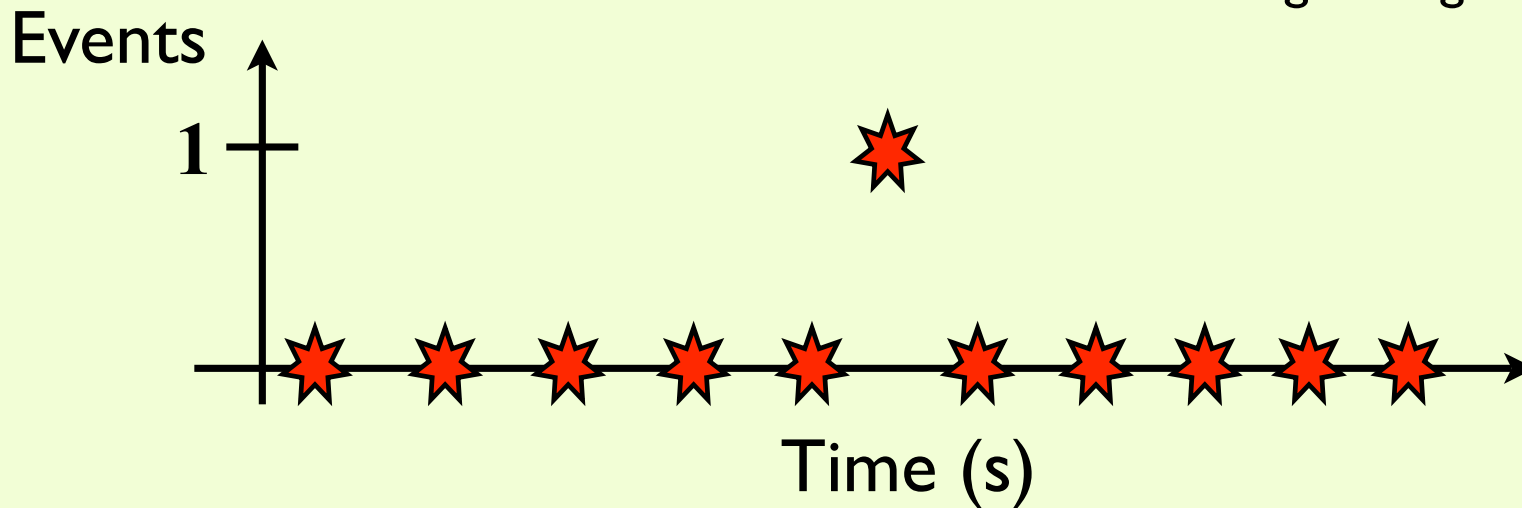
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Soccer game analogy redux:

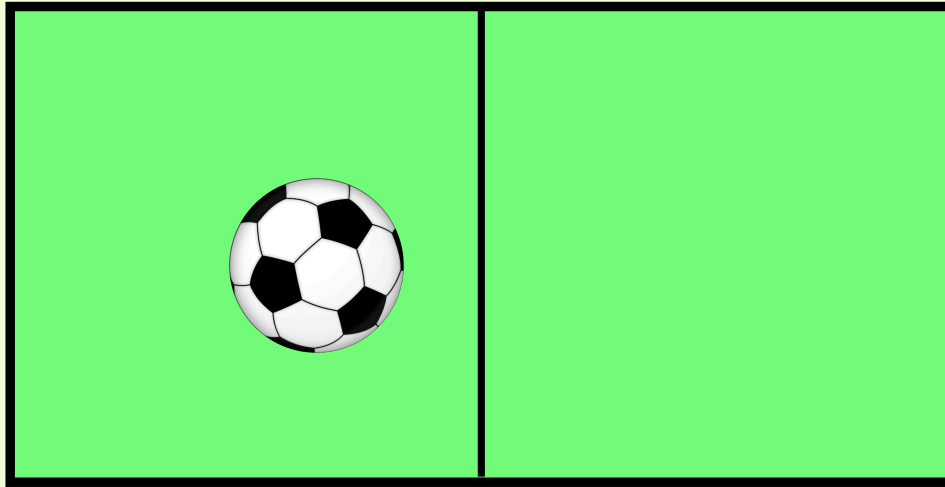
EVENT = soccer ball  
crosses the center line

*Appears Poissonian if you  
look long enough.*



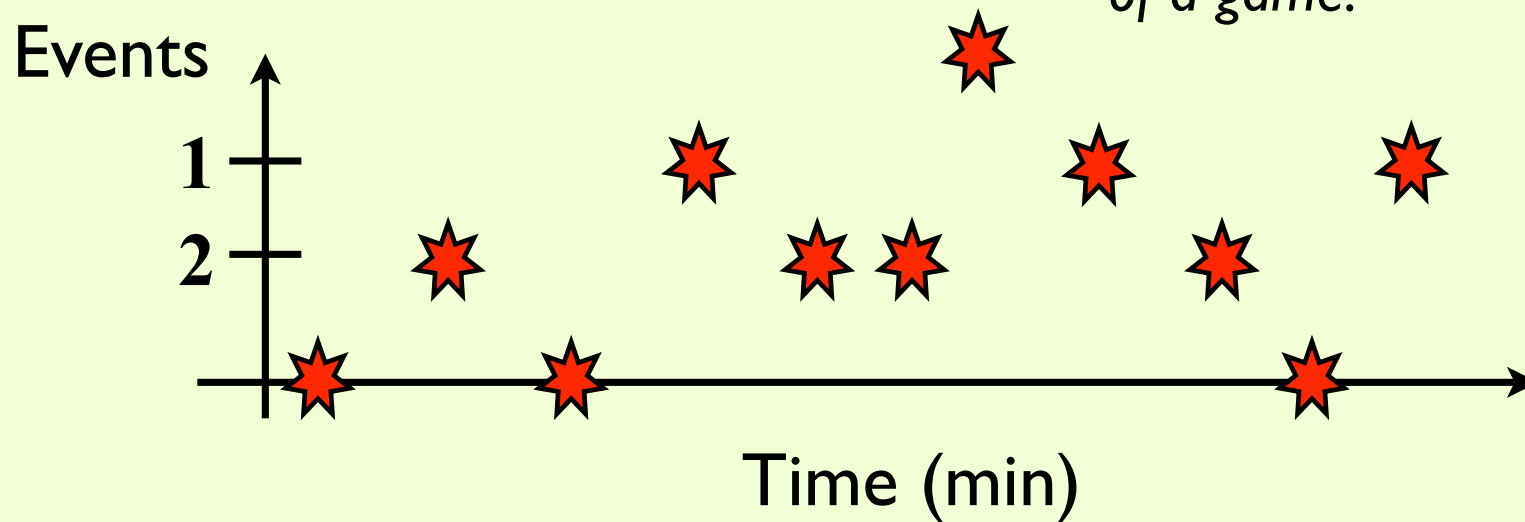
# The time scale is important

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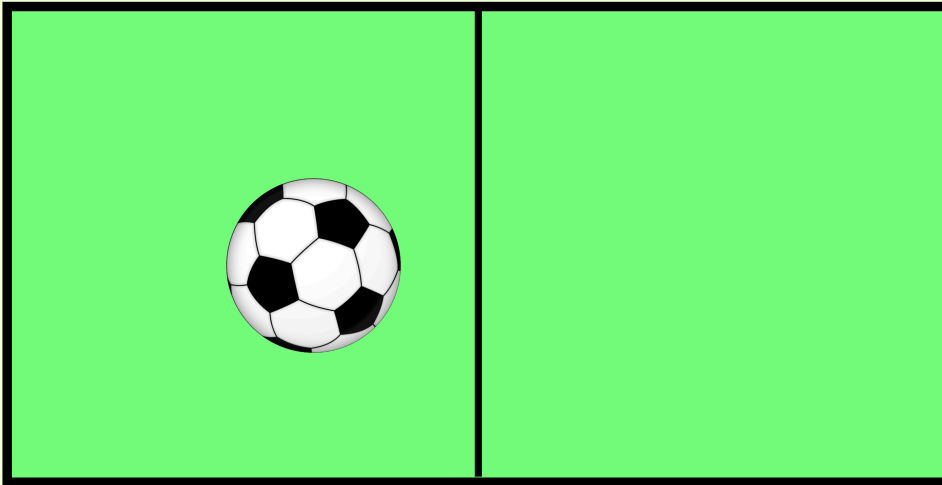
Soccer game analogy redux:  
How often does the ball  
cross the center line?

*No longer appears  
Poissonian when you  
reach half-time or the end  
of a game.*

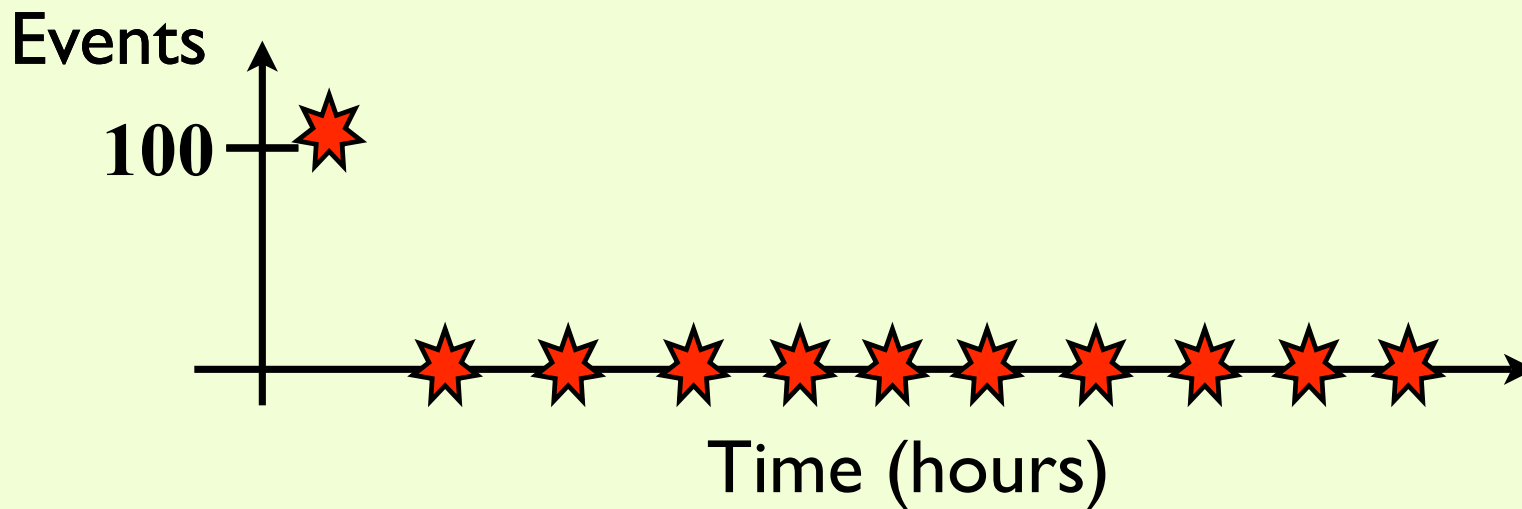


# The time scale is important

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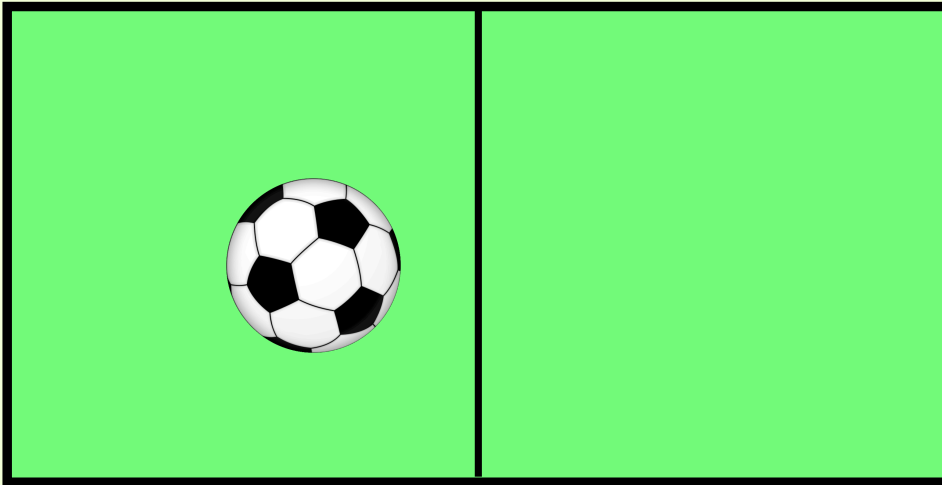
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How often does the ball  
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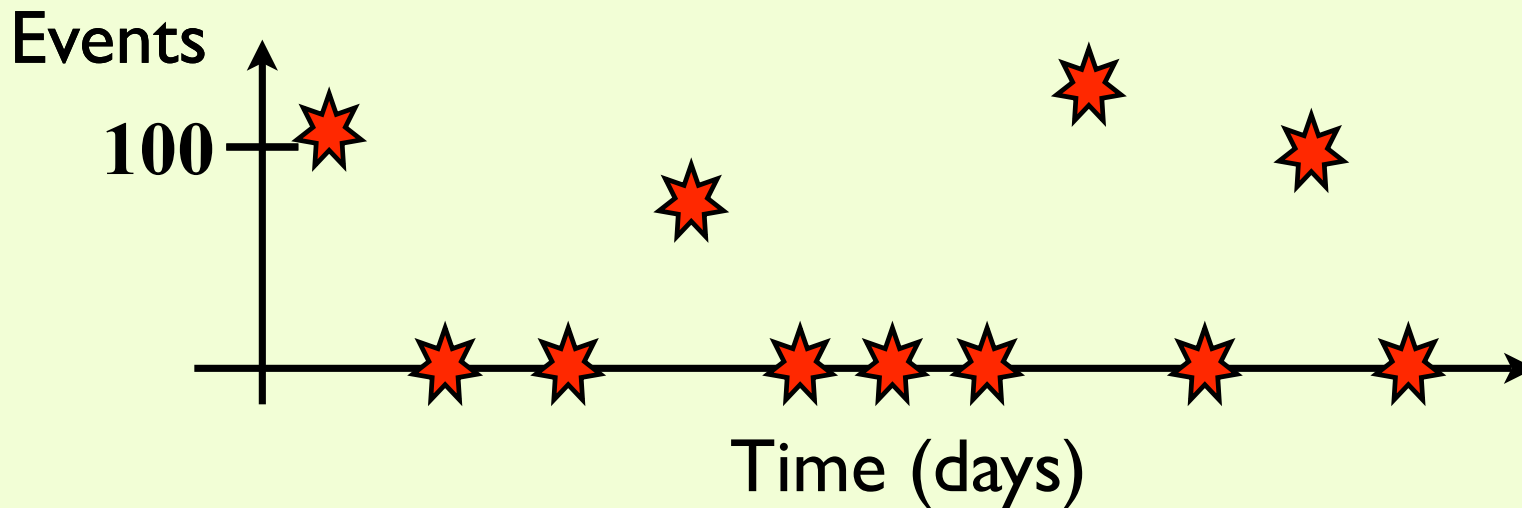
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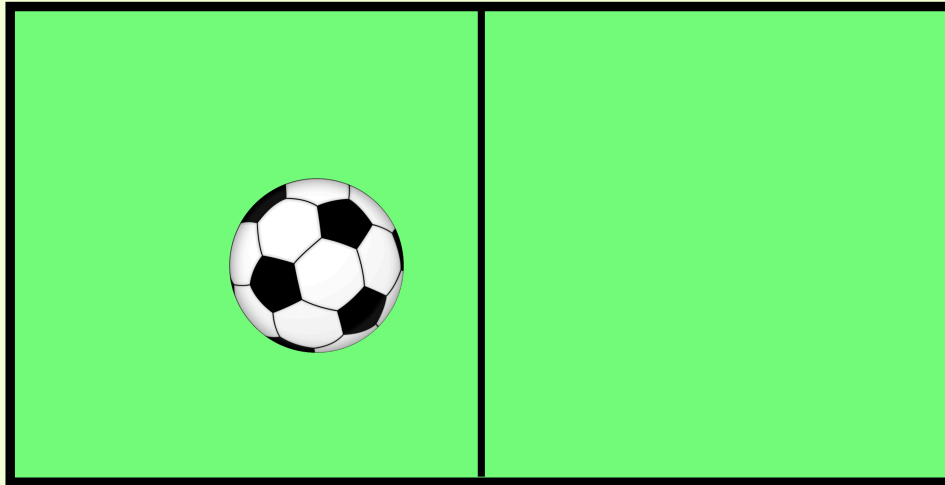
Soccer game analogy redux:  
How often does the ball  
cross the center line?

*No longer appears  
Poissonian when you  
change seasons.*



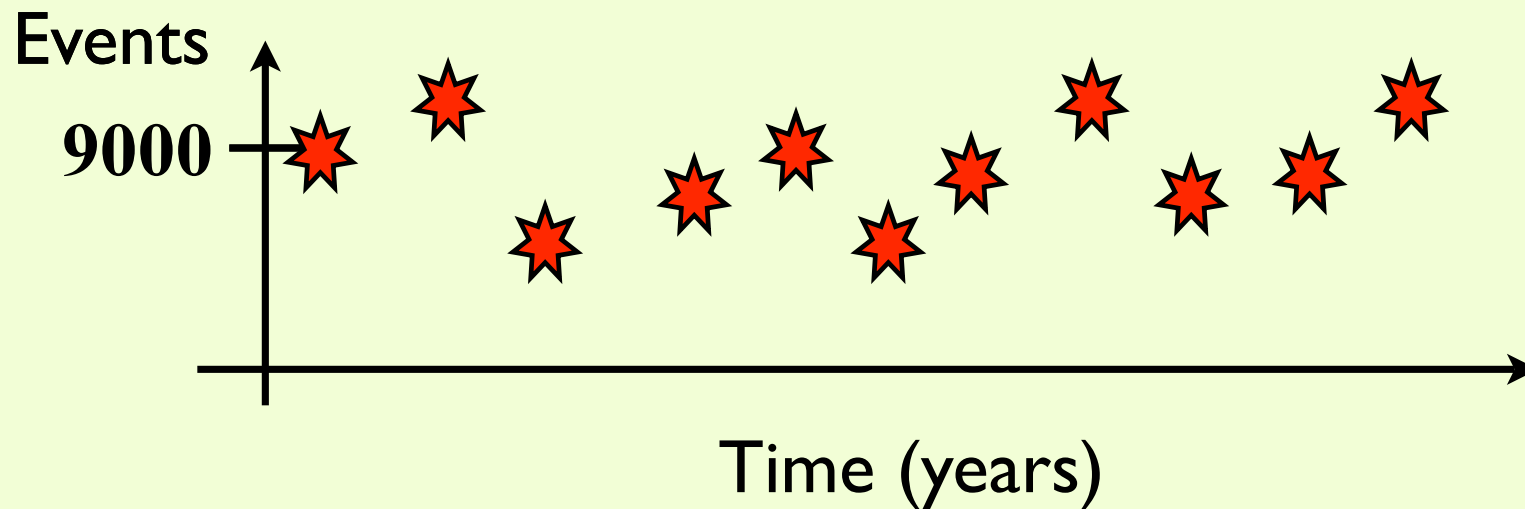
# The time scale is important

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Soccer game analogy redux:  
How often does the ball  
cross the center line?

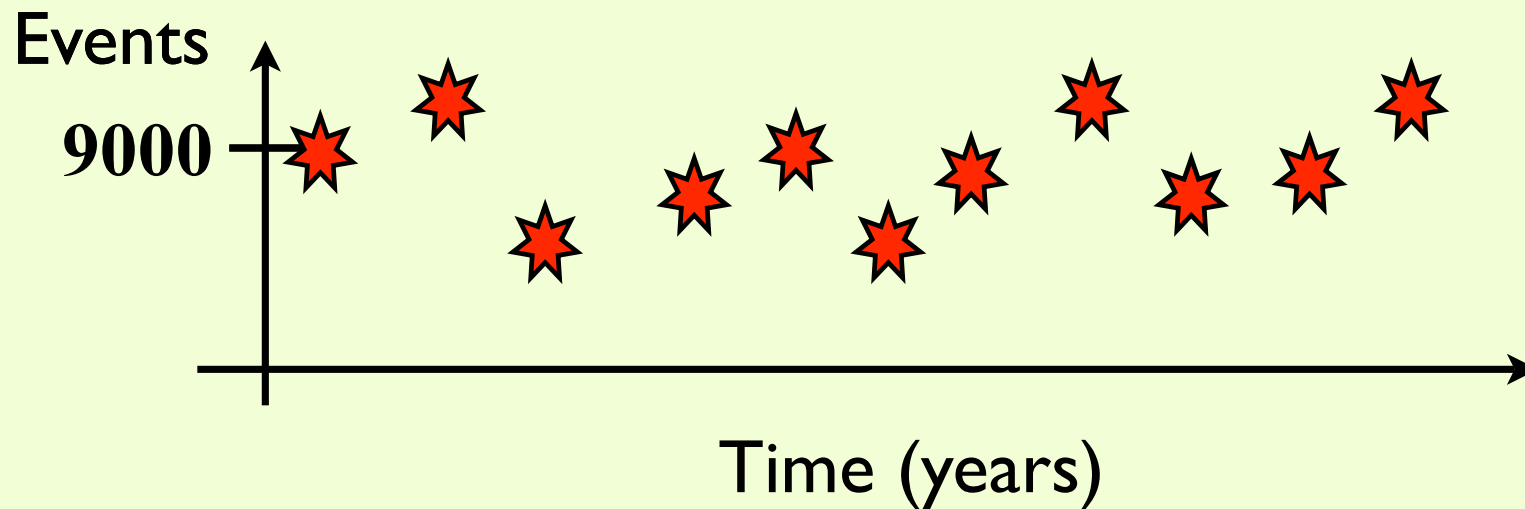
*No longer appears  
Poissonian when you the  
zombies take over.*



## What is the probability of a particular value of $N$ ?

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Even though the rate appears constant over time, the value of  $N$  is not always the same.



# Poisson processes

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$k$  - number of events occurring during  $dt$

$P(k)$  - probability of  $k$  events during  $dt$

$dT$  - measurement time interval

$$P(k) = \frac{e^{-\mu} \mu^k}{k!}$$

$$\left\langle \frac{N}{dT} \right\rangle = \mu$$

variance = mean

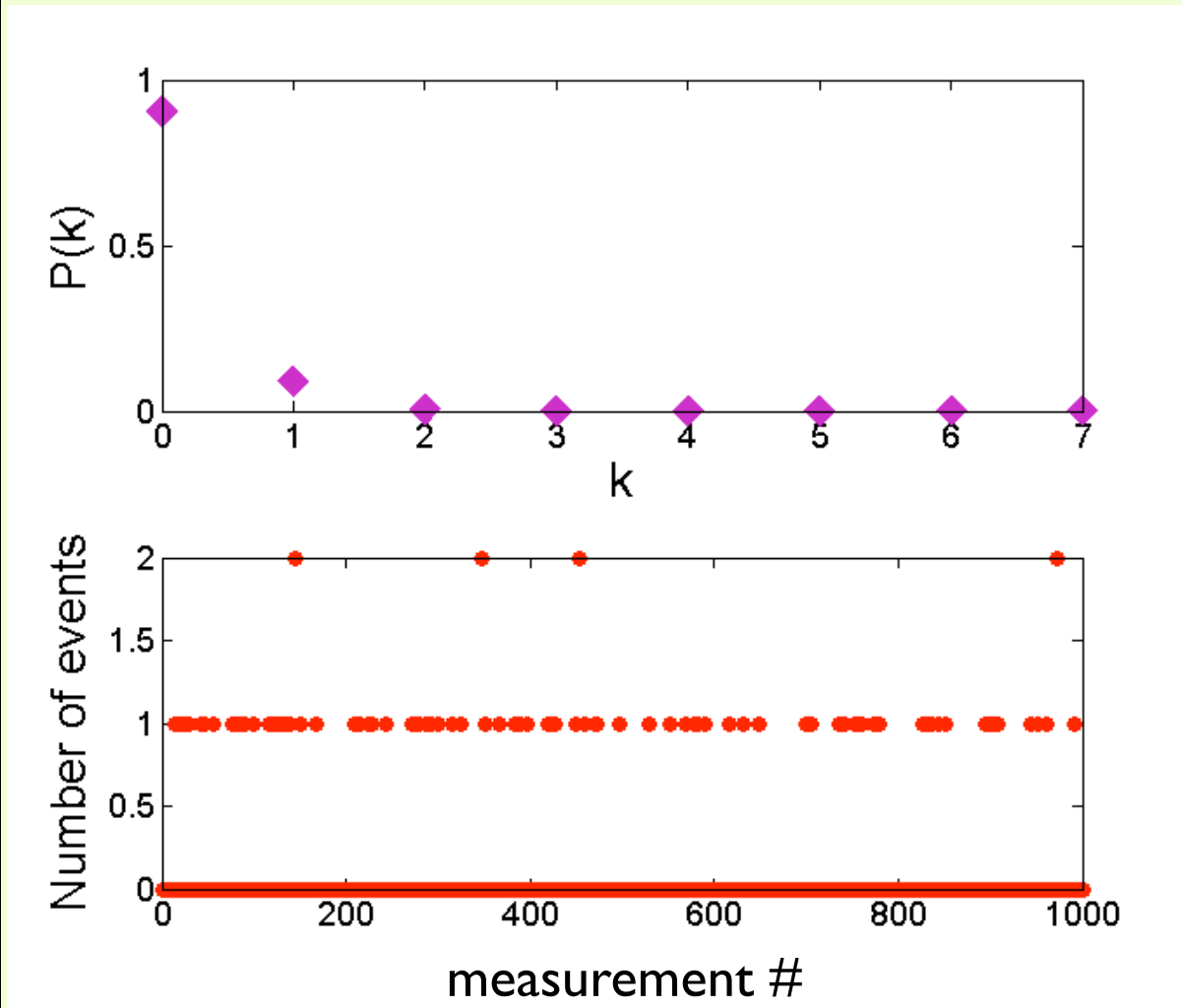


*Siméon Poisson*

*"Research on the Probability of Judgments in Criminal and Civil Matters"*

# Sampling bin is an important variable

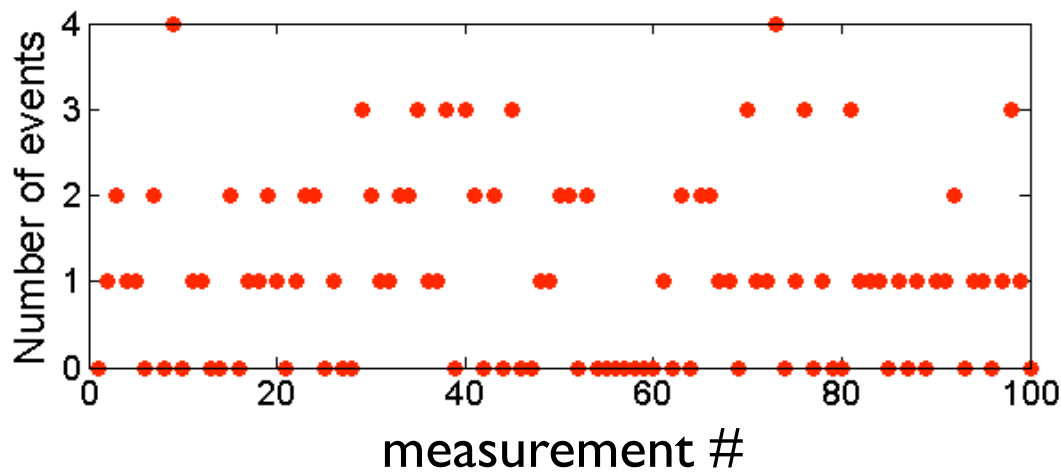
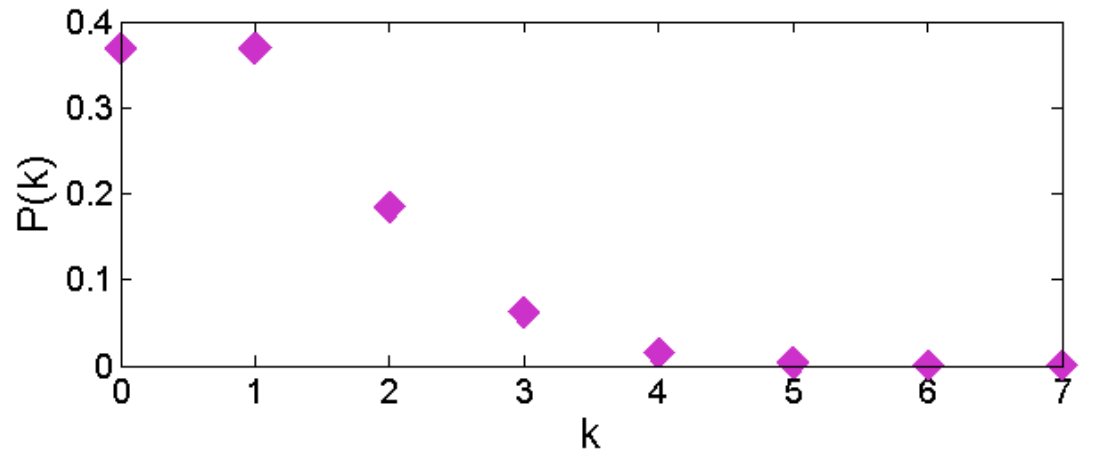
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$\lambda = 1$  event every  $1 \mu\text{s}$   
 $dT = 100 \text{ ns}$

Total time =  $100 \mu\text{s}$

# Sampling bin is an important variable



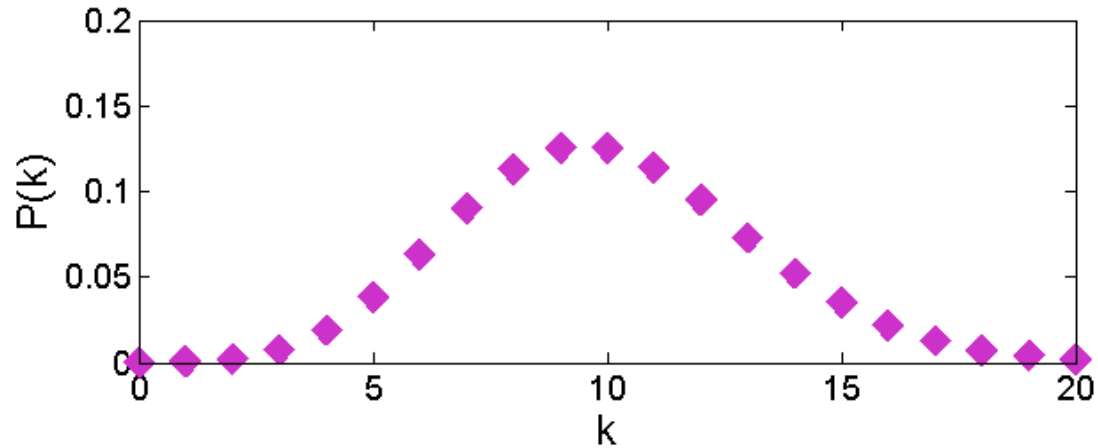
$\lambda = 1$  event every  $1 \mu\text{s}$

$dT = 1000 \text{ ns}$

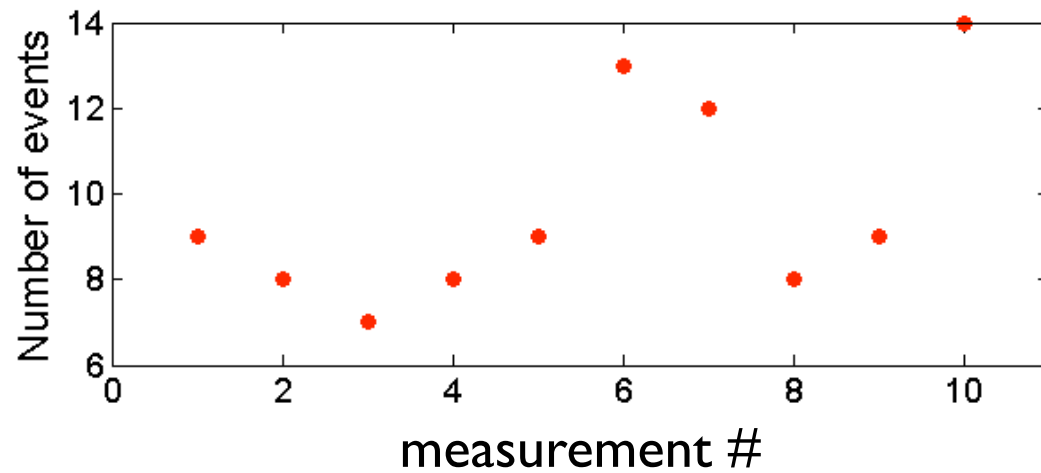
Total time =  $100 \mu\text{s}$

# Sampling bin is an important variable

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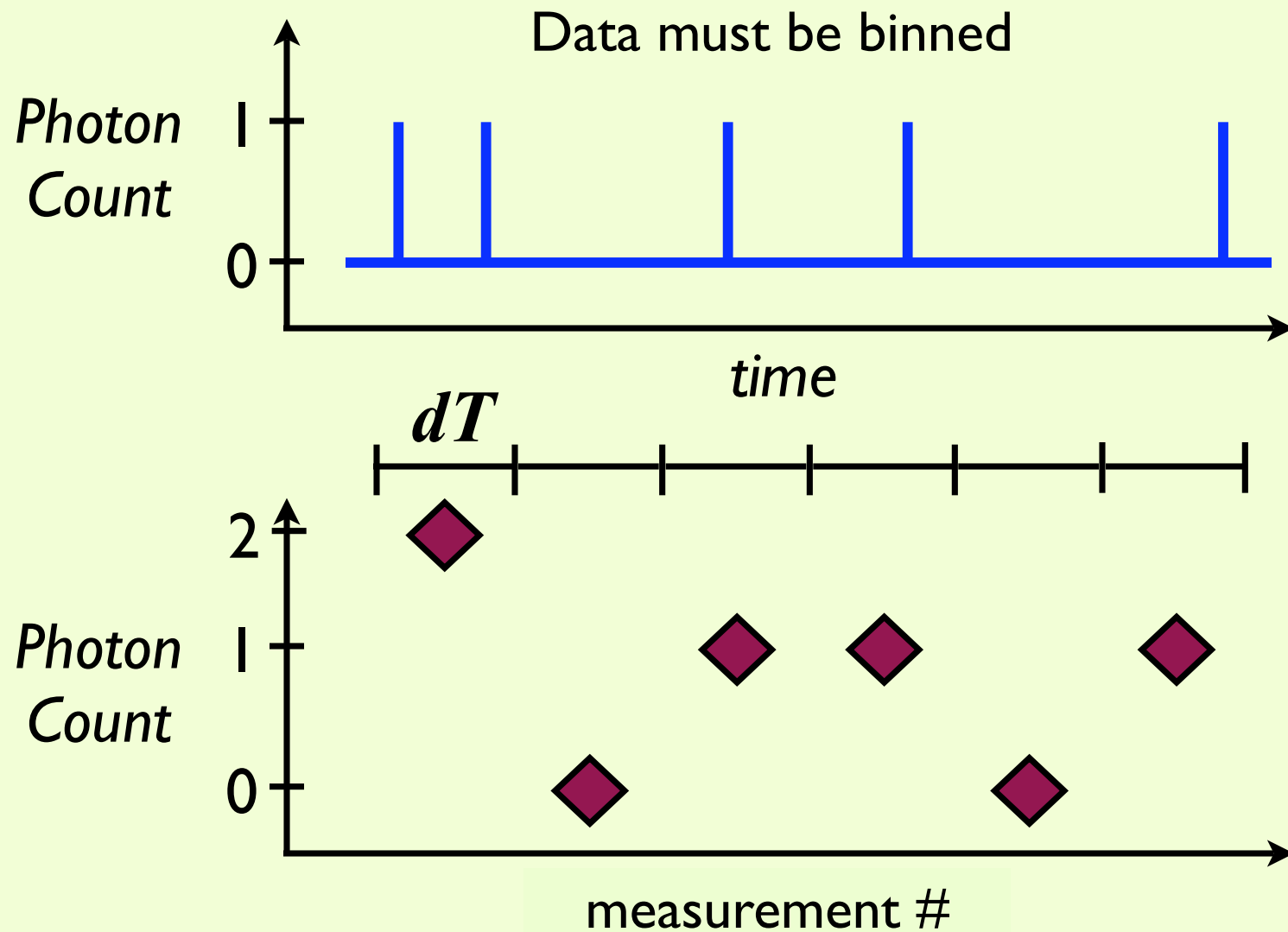


$\lambda = 1$  event every  $1 \mu\text{s}$   
 $dt = 10,000 \text{ ns}$



Total time =  $100 \mu\text{s}$

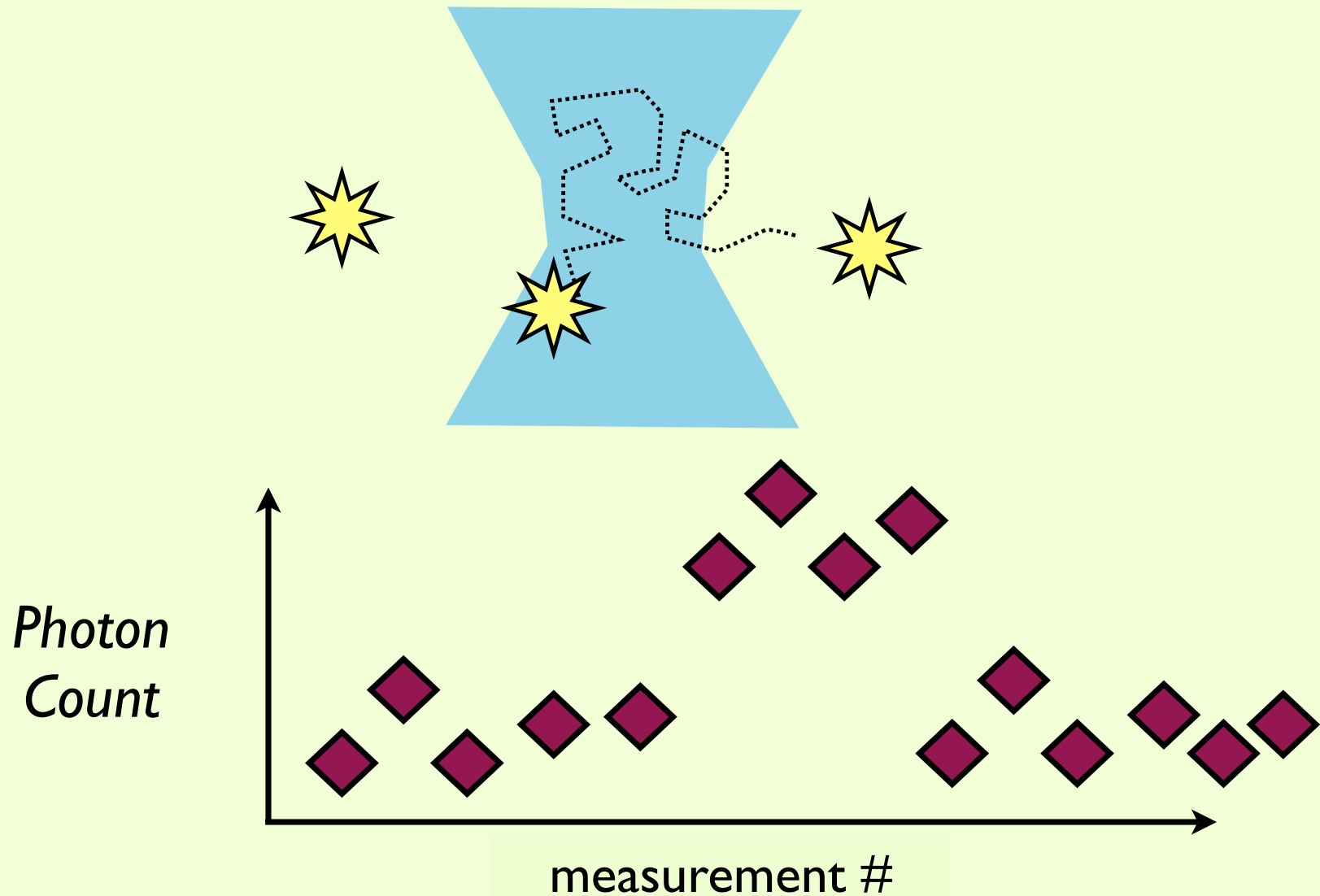
# Modeling our data as multiple poisson processes





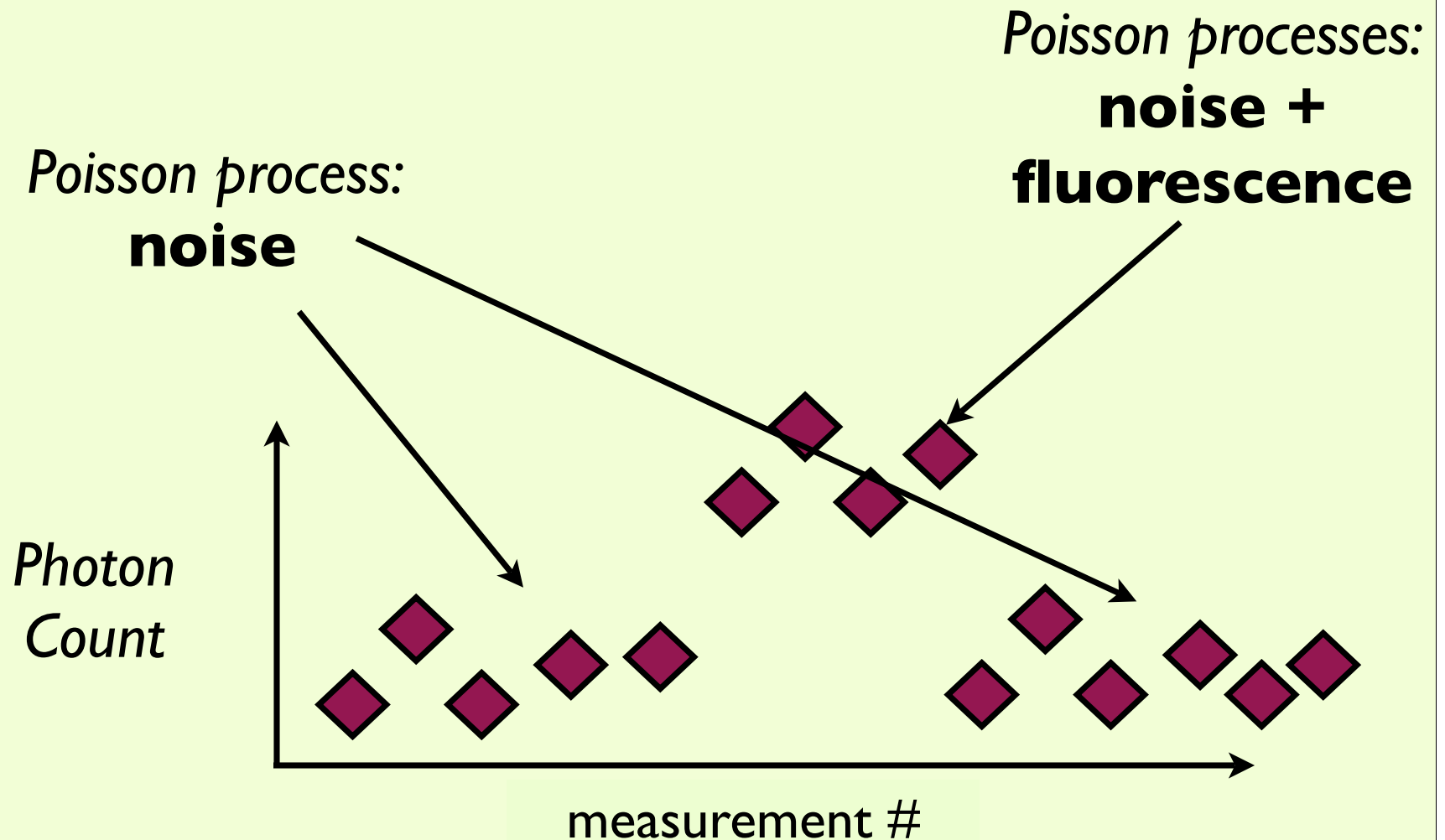
We would like information about how long the fluorophore stays in the confocal volume

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We would like information about how long the fluorophore stays in the confocal volume

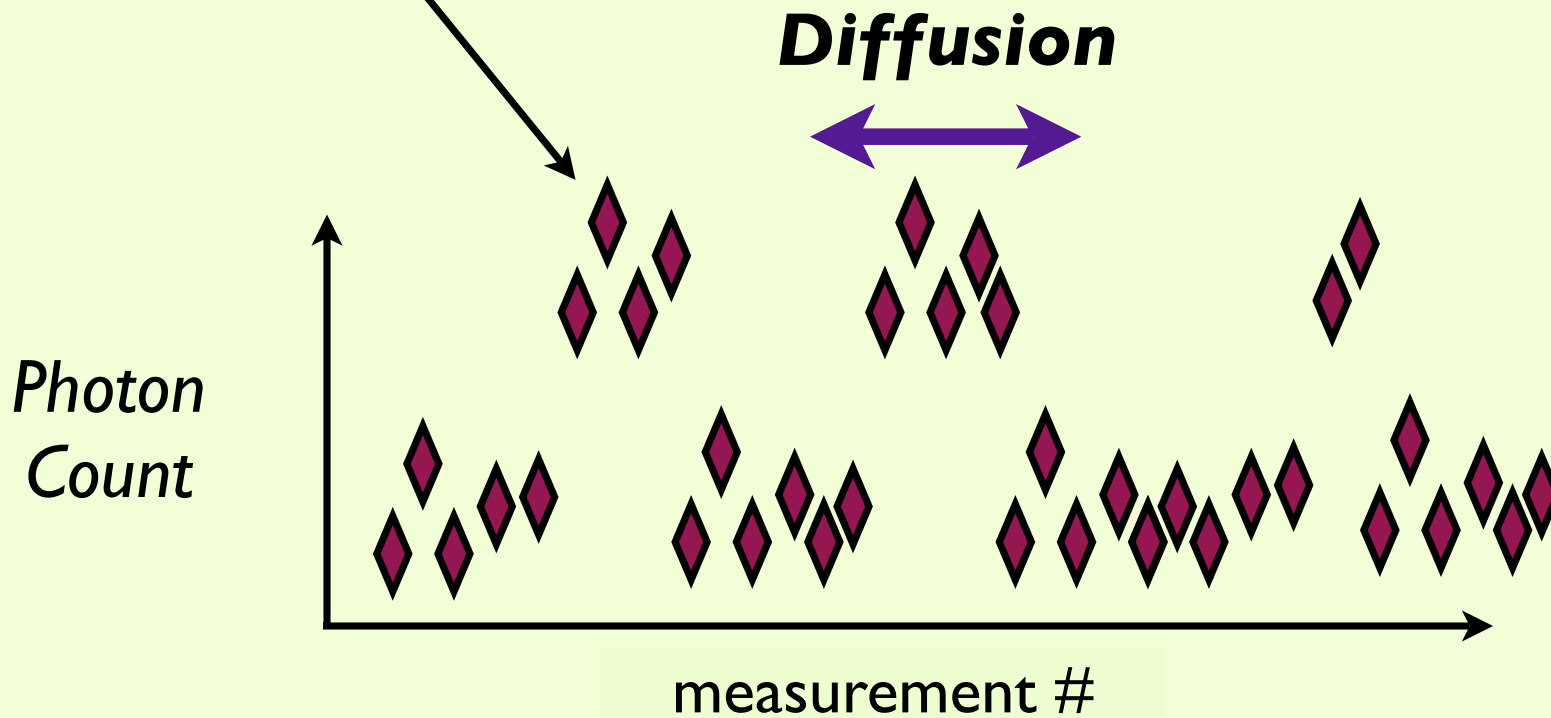
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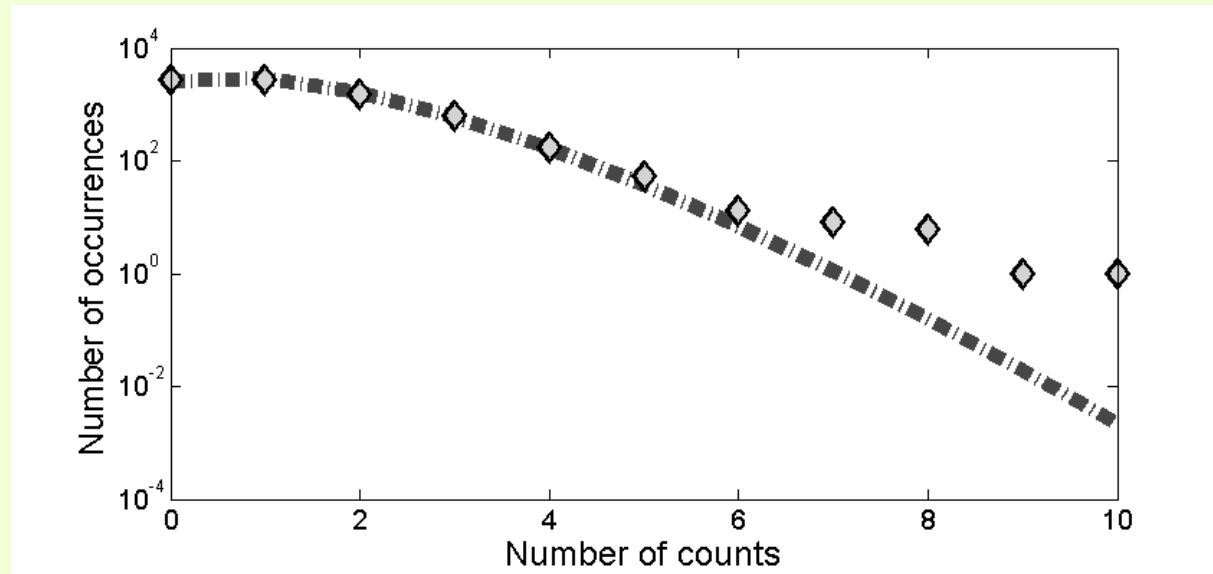
We would like information about how long the fluorophore stays in the confocal volume

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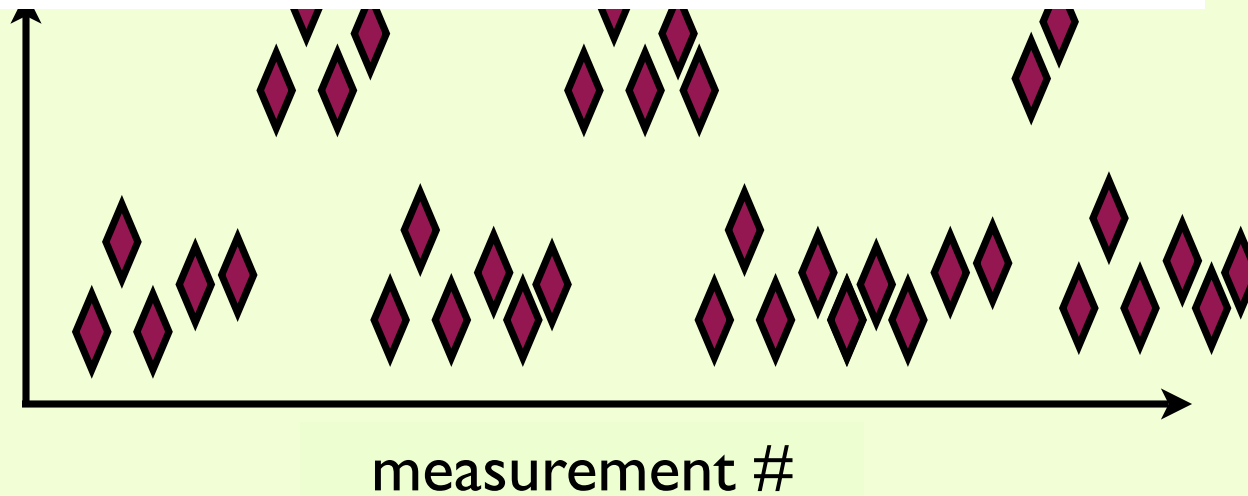
*Poisson process:*  
**frequency of events**



# Our simplistic approach: can our data be described by a single Poisson distribution?

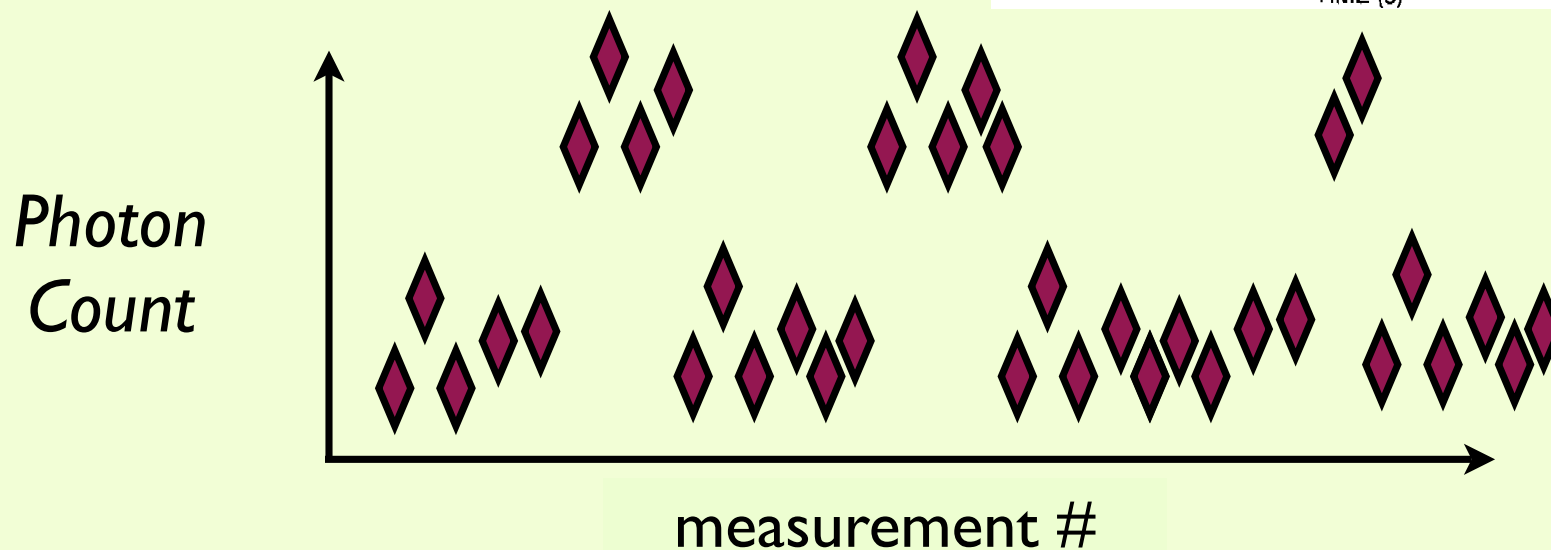
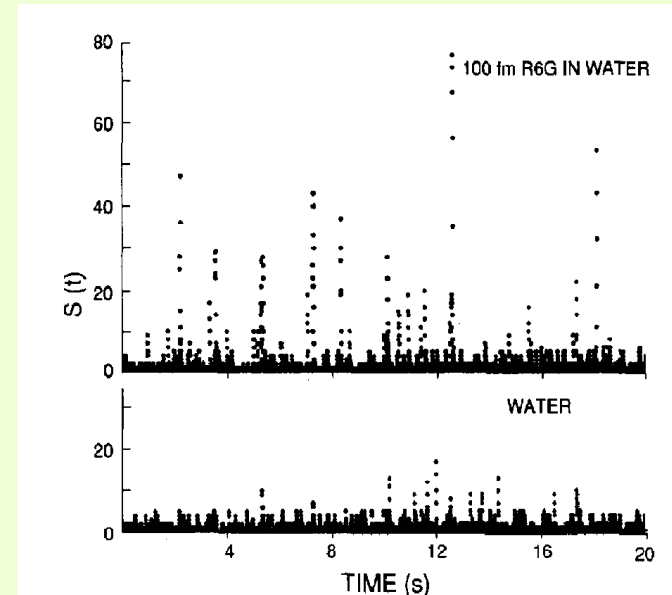


*Photon  
Count*

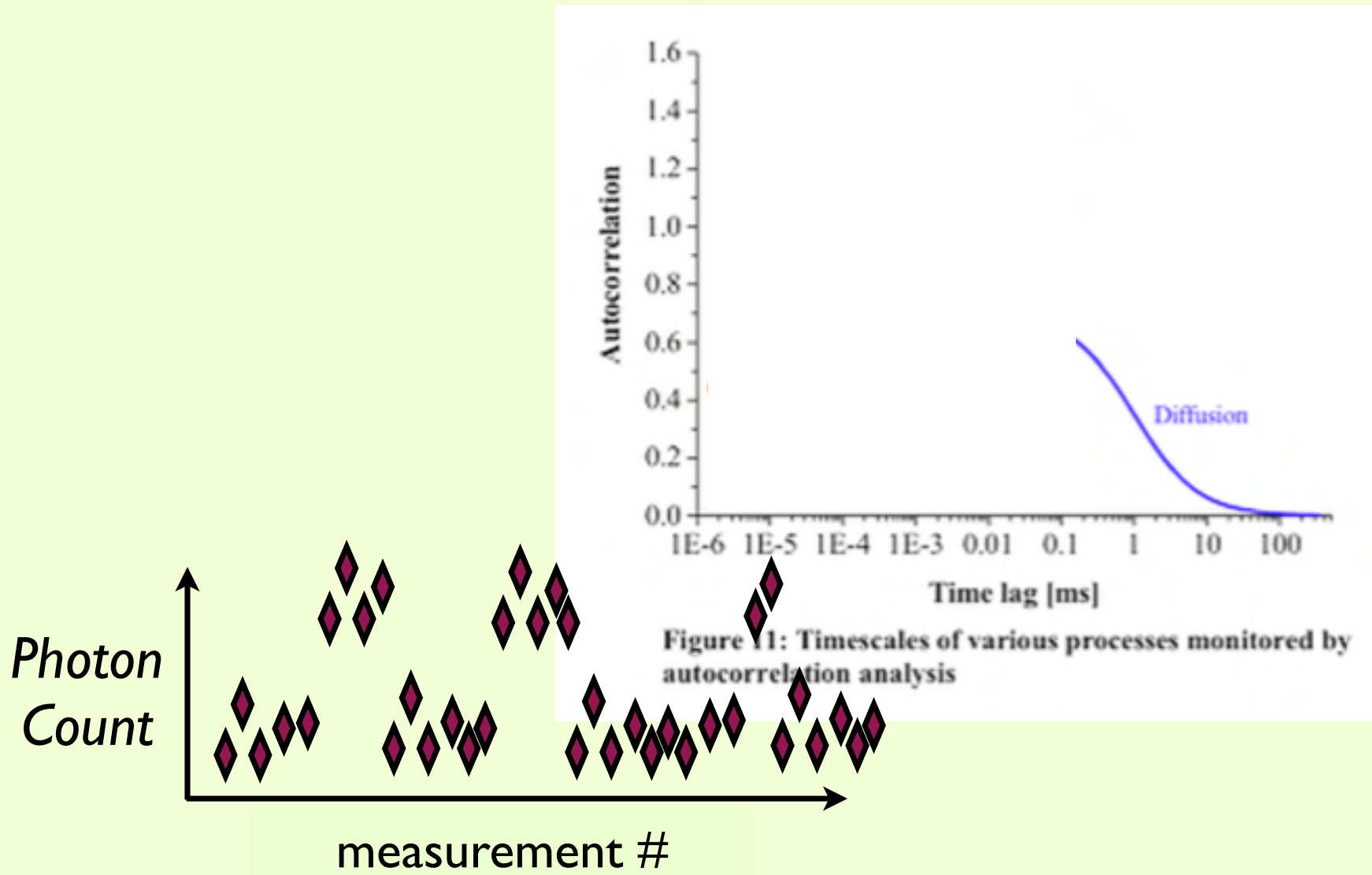


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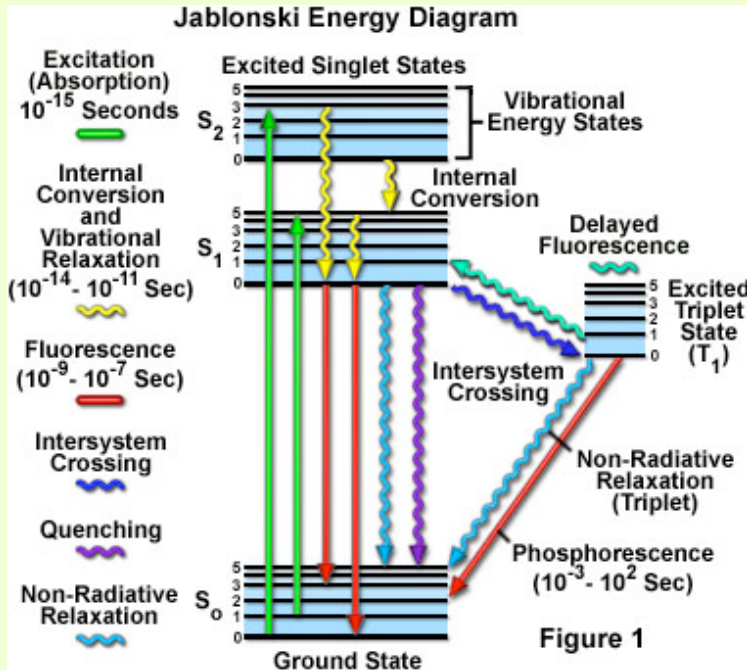
E. B. Shera, N. K. Seizinger, L. M. Davis, R.A. Keller and S.A. Soper, *Chem. Phys. Lett.* 174, 553 (1990).



# What are we missing?

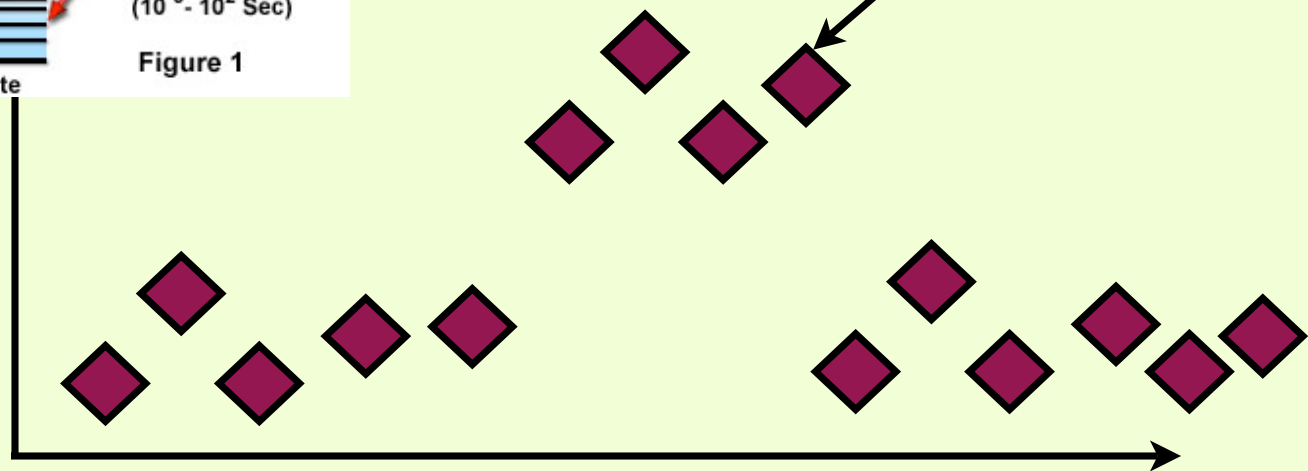


# What are we missing?



Poisson processes:  
**noise + fluorescence**

Photon  
Count



measurement #