Consider the following C++ code snippet:

```
vector<string> myVector(kNumStrings);
for(vector<string>::iterator itr = myVector.begin();
    itr != myVector.end(); ++itr)
    *itr += "Now longer!";
```

Here, we create a vector<string> of a certain size, then iterate over it concatenating "Now longer!" to each of the strings. Code like this is ubiquitous in C++, and initially does not appear all that exciting. However, let's take a closer look at how this code is structured. First, let's look at exactly what operations we're performing on the iterator:

```
vector<string> myVector(kNumStrings);
for(vector<string>::iterator itr = myVector.begin();
    itr != myVector.end(); ++itr)
    *itr += "Now longer!";
```

In this simple piece of code, we're comparing the iterator against myVector.end() using the != operator, incrementing the iterator with the ++ operator, and dereferencing the iterator with the * operator. At a high level, this doesn't seem all that out of the ordinary, since STL iterators are designed to look like regular pointers and these operators are all well-defined on pointers. But the key thing to notice is that STL iterators *aren't* pointers, they're *objects*, and !=, *, and ++ aren't normally defined on objects. We can't write code like ++myVector or *myMap = 137, so why can these operations be applied to vector<string>::iterator?

Similarly, notice how we're concatenating the string "Now longer!" onto the end of the string:

```
vector<string> myVector(kNumStrings);
for(vector<string>::iterator itr = myVector.begin();
    itr != myVector.end(); ++itr)
    *itr += "Now longer!";
```

Despite the fact that string is an object, somehow C++ "knows" what it means to apply += to strings.

All of the above examples are instances of *operator overloading*, the ability to specify how operators normally applicable to primitive types can interact with custom classes. Operator overloading is ubiquitous in professional C++ code and, used correctly, can make your programs more concise, more readable, and more template-friendly.

There are two overarching purposes of operator overloading. First, operator overloading enables your custom classes to act like primitive types. That is, if you have a class like vector that mimics a standard C++ array, you can allow clients to use array notation to access individual elements. Similarly, when designing a class encapsulating a mathematical entity (for example, a complex number), you can let clients apply mathematical operators like +, -, and * to your type as though it were built into the language. Second, operator overloading enables your code to interact correctly with template and library code. For example, you can overload the << operator to make a class compatible with the streams library, or the < operator to interface with STL containers.

This chapter discusses general topics in operator overloading, demonstrating how to overload some of the more common operators. It also includes tricks and pitfalls to be aware of when overloading certain operators.

A Word of Warning

I would be remiss to discuss operator overloading without first prefacing it with a warning: operator overloading is a double-edged sword. When used correctly, operator overloading can lead to intuitive, template-friendly code that elegantly performs complex operations behind the scenes. However, incorrectly overloaded operators can lead to incredibly subtle bugs. Seemingly innocuous code along the lines of *myItr = 5 can cause serious problems if implemented incorrectly, and without a solid understanding of how to overload operators you may find yourself in serious trouble.

There is a pearl of design wisdom that is particularly applicable to operator overloading:

The Principle of Least Astonishment: A function's name should communicate its behavior and should be consistent with other naming conventions and idioms.

The principle of least astonishment should be fairly obvious – you should design functions so that clients can understand what those functions do simply by looking at the functions' names; that is, clients of your code should not be "astonished" that a function with one name does something entirely different. For example, a function named DoSomething violates the principle of least astonishment because it doesn't communicate what it does, and a function called ComputePrimes that reads a grocery list from a file violates the principle because the name of the function is completely different from the operation it performs. However, other violations of the principle of least astonishment are not as blatant. For example, a custom container class whose empty member function erases the contents of the container violates the principle of least astonishment because C++ programmers expect empty to mean "is the container empty?" rather than "empty the container." Similarly, a class that is bitwise const but not semantically const violates the principle, since programmers assume that objects can't be modified by const member functions.

When working with operator overloading, it is crucial to adhere to the principle of least astonishment. C+ + lets you redefine almost all of the built-in operators however you choose, meaning that it's possible to create code that does something completely different from what C++ programmers might expect. For example, suppose that you are working on a group project and that one of your teammates writes a class CustomVector that acts like the STL vector but which performs some additional operations behind the scenes. Your program contains a small bug, so you look over your teammate's code and find the following code at one point:

```
CustomVector one = /* ... */, two = /* ... */;
one %= two;
```

What does the line one \$ = two do? Syntactically, this says "take the remainder when dividing one by two, then store the result back in one." But this makes no sense – how can you divide one CustomVector by another? You ask your teammate about this, and he informs you that the \$ = operator means "remove all elements from one that are also in two." This is an egregious violation of the principle of least astonishment. The code neither communicates what it does nor adheres to existing convention, since the semantics of the \$ = operator are meaningless when applied to linear data structures. This is not to say, of course, that having the ability to remove all elements from one CustomVector that are contained in another is a bad idea – in fact, it can be quite useful – but this functionality should be provided by a properly-named member function rather than a cryptically-overloaded operator. For example, consider the following code:

```
CustomVector one = /* ... */, two = /* ... */;
one.removeAllIn(two);
```

This code accomplishes the same task as the above code, but does so by explicitly indicating what operation is being performed. This code is much less likely to confuse readers and is far more descriptive than before.

As another example, suppose that your teammate also implements a class called CustomString that acts like the standard string type, but provides additional functionality. You write the following code:

```
CustomString one = "Hello", two = " World";
one += two;
cout << one + "!" << endl;</pre>
```

Intuitively, this should create two strings, then concatenate the second onto the end of the first. Next, the code prints out one followed by an exclamation point, yielding "Hello World!" Unfortunately, when you compile this code, you get an unusual error message – for some reason the code one += two compiles correctly, but the compiler rejects the code one + "!". In other words, your teammate has made it legal to concatenate two strings using +=, but not by using +. Again, think back to the principle of least astonishment. Programmers tacitly expect that objects that can be added with + can be added with += and vice-versa, and providing only half of this functionality is likely to confuse code clients.

The moral of this story is simple: when overloading operators, make sure that you adhere to existing conventions. If you don't, you will end up with code that is either incorrect, confusing, or both.

Hopefully this grim introduction has not discouraged you from using operator overloading. Operator overloading is extraordinarily useful and you will not be disappointed with the possibilities that are about to open up to you. With that said, let's begin discussing the mechanics behind this powerful technique.

Defining Overloaded Operators

We introduced operator overloading as a mechanism for redefining how the built-in operators apply to custom classes. Syntactically, how do we communicate to the C++ compiler that we want to redefine these operators? The answer is somewhat odd. Here's the original motivating example we had at the beginning of the chapter:

```
vector<string> myVector(kNumStrings);
for(vector<string>::iterator itr = myVector.begin();
    itr != myVector.end(); ++itr)
    *itr += "Now longer!";
```

When you provide this code to the C++ compiler, it interprets it as follows:

```
vector<string> myVector(kNumStrings);
for(vector<string>::iterator itr = myVector.begin();
    operator!= (itr, myVector.end());
    itr.operator++())
    (itr.operator*()).operator +=("Now longer!");
```

Notice that everywhere we used the built-in operator in conjunction with an object, the compiler reinterpreted the operator as a call to a specially-named function called operator **op**, where **op** is the particular operator we used. Thus itr != myVector.end() translated into operator!= (itr, myVector.end()), ++itr was interpreted as itr.operator++(), etc. Although these functions may have cryptic names, they're just regular functions. Operator overloading is simply *syntax sugar*, a way of rewriting one operation (in this case, function calls) using a different syntax (here, the built-in operators). Overloaded operators are not somehow "more efficient" than other functions simply because the function calls aren't explicit, nor are they treated any different from regular functions. They are special only in that they can are invoked using the built-in operators rather than through an explicit function calls.

If you'll notice, some of the operators used above were translated into member function calls (particularly ++ and *), while others (!=) were translated into calls to free functions. With a few exceptions, any operator can be overloaded as either a free function or a member function. Determining whether to use free functions or member functions for overloaded operators is a bit tricky, and we'll discuss it more as we continue our tour of overloaded operators.

Each of C++'s built-in operators has a certain number of *operands*. For example, the plus operator (a + b) has two operands corresponding to the values on the left- and right-hand sides of the operator. The pointer dereference operator (*itr), on the other hand, takes in only one operand: the pointer to dereference. When defining a function that is an overloaded operator, you will need to ensure that your function has one parameter for each of the operator's operands. For example, suppose that we want to define a type RationalNumber which encapsulates a rational number (a ratio of two integers). Because it's mathematically sound to add two rational numbers, we might want to consider overloading the + operator as applied to RationalNumber so that we can add RationalNumbers using an intuitive syntax. What would such a function look like? If we implement the + operator as a member function of RationalNumber, the syntax would be as follows:

```
class RationalNumber {
  public:
     const RationalNumber operator+ (const RationalNumber& rhs) const;
     /* ... etc. ... */
};
```

(You might be wondering why the return type is const RationalNumber. For now, you can ignore that... we'll pick this up in the next section)

With operator+ defined this way, then addition of RationalNumbers will be translated into calls to the member function operator+ on RationalNumber. For example, the following code:

```
RationalNumber one, two;
RationalNumber three = one + two;
```

will be interpreted by the compiler as

```
RationalNumber one, two;
RationalNumber three = one.operator +(two);
```

Notice that the code one + two was interpreted as one.operator+ (two). That is, the receiver object of the operator+ function is the left-hand operand, while the argument is the right-hand argument. This is not a coincidence, and in fact C++ will guarantee that the relative ordering of the operands is preserved. one + two will never be interpreted as two.operator+ (one) under any circumstance, and our implementation of operator+ can take this into account.

Alternatively, we could consider implementing <code>operator+</code> as a free function taking in two arguments. If we chose this approach, then the interface for <code>RationalNumber</code> would be as follows:

In this case, the code

RationalNumber one, two; RationalNumber three = one + two;

would be interpreted by the compiler as

```
RationalNumber one, two;
RationalNumber three = operator+ (one, two);
```

Again, the relative ordering of the parameters is guaranteed to be stable, and so you can assume that the first parameter to <code>operator+</code> will always be on the left-hand side of the operator.

In some cases, two operators are syntactically identical but have different meanings. For example, the – operator can refer either to the binary subtraction operator (a – b) or the unary negation operator (-a). If overload the – operator, how does the compiler know whether your overloaded operator is the unary or binary version of –? The answer is rather straightforward: if the function operates on two pieces of data, the compiler treats <code>operator-</code> as the binary subtraction operator, and if the function uses just one piece of data it's considered to be the unary negation operator. Let's make this discussion a bit more concrete. Suppose that we want to implement subtraction on the <code>RationalNumber</code> class. Because the binary subtraction operator has two operands, we would provide subtraction as an overloaded operator either as a free function:

or, alternatively, as a member function:

```
class RationalNumber {
  public:
     const RationalNumber operator- (const RationalNumber& rhs) const;
     /* ... etc. ... */
};
```

Notice that both of these functions operate on two pieces of data. In the first case, the function takes in two parameters, and in the second, the receiver object is one piece of data and the parameter is the other. If we now want to provide an implementation of <code>operator-</code> which represents the unary negation operator, we could implement it as a free function with the following signature:

const RationalNumber operator- (const RationalNumber& arg);

Or as a member function of this form:

```
class RationalNumber {
public:
    const RationalNumber operator- () const;
    /* ... etc. ... */
};
```

Again, don't worry about why the return type is a const RationalNumber. We'll address this shortly.

What Operator Overloading Cannot Do

When overloading operators, you cannot define brand-new operators like # or @. After all, C++ wouldn't know the associativity or proper syntax for the operator (is one # two + three interpreted as (one # two) + three or one # (two + three)?) Additionally, you cannot overload any of the following operators:

| Operator | Syntax | Name |
|--|-----------------|---|
| :: | MyClass::value | Scope resolution |
| • | one.value | Member selection |
| ?: | a > b ? -1 : 1 | Ternary conditional |
| •* | a.*myClassPtr; | Pointer-to-member selection (beyond the scope of this text) |
| sizeof | sizeof(MyClass) | Size of object |
| typeid | typeid(MyClass) | Runtime type information operator |
| (T) static_cast dynamic_cast reinterpret_cast const_cast | (int) myClass; | Typecast |

Note that operator overloading only lets you define what built-in operators mean when applied to *objects*. You cannot use operator overloading to redefine what addition means as applied to ints, nor can you change how pointers are dereferenced. Then again, by the principle of least astonishment, you wouldn't want to do this anyway.

Lvalues and Rvalues

Before we begin exploring some of the implementation issues associated with overloaded operators, we need to take a quick detour to explore two concepts from programming language theory called *lvalues* and *rvalues*. Lvalues and rvalues stand for "left values" and "right values" are are so-named because of where they can appear in an assignment statement. In particular, an lvalue is a value that can be on the left-hand side of an assignment, and an rvalue is a value that can only be on the right-hand side of an assignment. For example, in the statement x = 5, x is an lvalue and 5 is an rvalue. Similarly, in *itr = 137, *itr is the lvalue and 137 is the rvalue.

It is illegal to put an rvalue on the left-hand side of an assignment statement. For example, 137 = 42 is illegal because 137 is an rvalue, and GetInteger() = x is illegal because the return value of GetInteger() is an rvalue. However, it *is* legal to put an lvalue on the right-hand side of an assignment, as in x = y or x = *itr.

At this point the distinction between lvalues and rvalues seems purely academic. "Okay," you might say, "some things can be put on the left-hand side of an assignment statement and some things can't. So what?" When writing overloaded operators, the lvalue/rvalue distinction is extremely important. Because operator overloading lets us define what the built-in operators mean when applied to objects of class type, we have to be very careful that overloaded operators return lvalues and rvalues appropriately. For example, by default the + operator returns an rvalue; that is, it makes no sense to write

(x + y) = 5;

Since this would assign the value 5 to the result of adding x and y. However, if we're not careful when overloading the + operator, we might accidentally make the above statement legal and pave the way for nonsensical but legal code. Similarly, it *is* legal to write

myArray[5] = 137;

So the element-selection operator (the brackets operator) should be sure to return an lvalue instead of an rvalue. Failure to do so will make the above code illegal when applied to custom classes.

Recall that an overloaded operator is a specially-named function invoked when the operator is applied to an object of a custom class type. Thus the code

(x + y) = 5;

is equivalent to

```
operator+ (x, y) = 5;
```

if either x or y is an object. Similarly, if myArray is an object, the code

```
myArray[5] = 137;
```

is equivalent to

myArray.operator[](5) = 137;

To ensure that these functions have the correct semantics, we need to make sure that <code>operator+</code> returns an rvalue and that <code>operator[]</code> returns an lvalue. How can we enforce this restriction? The answer has to do with the return type of the two functions. To make a function that returns an lvalue, have that function return a non-const reference. For example, the following function returns an lvalue:

```
string& LValueFunction();
```

Because a reference is just another name for a variable or memory location, this function hands back a reference to an lvalue and its return value can be treated as such. To have a function return an rvalue, have that function return a const object by value. Thus the function

```
const string RValueFunction();
```

returns an rvalue.^{*} The reason that this trick works is that if we have a function that returns a const object, then code like

RValueFunction() = 137;

is illegal because the return value of RValueFunction is marked const.

Lvalues and rvalues are difficult to understand in the abstract, but as we begin to actually overload particular operators the difference should become clearer.

Overloading the Element Selection Operator

Let's begin our descent into the realm of operator overloading by discussing the overloaded element selection operator (the []] operator, used to select elements from arrays). You've been using the overloaded element selection operator ever since you encountered the string and vector classes. For example, the following code uses the vector's overloaded element selection operator:

```
for(int i = 0; i < myVector.size(); ++i)
    myVector[i] = 137;</pre>
```

In the above example, while it looks like we're treating the vector as a primitive array, we are instead calling the a function named operator [], passing i as a parameter. Thus the above code is equivalent to

```
for(int i = 0; i < myVector.size(); ++i)
    myVector.operator [](i) = 137;</pre>
```

To write a custom element selection operator, you write a member function called <code>operator []</code> that accepts as its parameter the value that goes inside the brackets. Note that while this parameter can be of any type (think of the STL map), you can only have a single value inside the brackets. This may seem like an arbitrary restriction, but makes sense in the context of the principle of least astonishment: you can't put multiple values inside the brackets when working with raw C++ arrays, so you shouldn't do so when working with custom objects.

When writing operator [], as with all overloaded operators, you're free to return objects of whatever type you'd like. However, remember that when overloading operators, it's essential to maintain the same functionality you'd expect from the naturally-occurring uses of the operator. In the case of the element selection operator, this means that the return value should be an lvalue, and in particular a reference to some internal class data determined by the index. For example, here's one possible prototype of the C++ string's element selection operator:

```
class string {
public:
    /* ... */
    char& operator [] (size_t position);
};
```

^{*} Technically speaking any non-reference value returned from a function is an rvalue. However, when returning objects from a function, the rvalue/lvalue distinction is blurred because the assignment operator and other operators are member functions that can be invoked regardless of whether the receiver is an rvalue or lvalue. The additional const closes this loophole.

Here, <code>operator[]</code> takes in an int representing the index and returns a reference to the character at that position in the <code>string</code>. If <code>string</code> is implemented as a wrapper for a raw C string, then one possible implementation for <code>operator[]</code> might be

```
char& string::operator[] (size_t index) {
    return theString[index]; // Assuming theString is an array of characters
}
```

Because operator[] returns a reference to an element, it is common to find operator[] paired with a const-overload that returns a const reference to an element in the case where the receiver object is immutable. There are exceptions to this rule, such as the STL map, but in the case of string we should provide a const overload, as shown here:

```
class string {
public:
    /* ... */
        char& operator [] (size_t position);
        const char& operator [] (size_t position) const;
};
```

The implementation of the <code>const operator[]</code> function is identical to the non-const version.

When writing the element selection operator, it's completely legal to modify the receiver object in response to a request. For example, with the STL map, operator[] will silently create a new object and return a reference to it if the key isn't already in the map. This is part of the beauty of overloaded operators – you're allowed to perform any necessary steps to ensure that the operator makes sense.

Unfortunately, if your class encapsulates a multidimensional object, such as a matrix or hierarchical keyvalue system, you cannot "overload the [][] operator." A class is only allowed to overload one level of the bracket syntax; it's not legal to design objects that doubly-overload [].*

Overloading Compound Assignment Operators

The compound assignment operators are operators of the form op= (for example, += and *=) that update an object's value but do not overwrite it. Compound assignment operators are often declared as member functions with the following basic prototype:

```
MyClass& operator += (const ParameterType& param)
```

For example, suppose we have the following class, which represents a vector in three-dimensional space:

```
class Vector3D {
public:
    /* ... */
private:
    static const int NUM_COORDINATES = 3;
    double coordinates[NUM_COORDINATES];
};
```

^{*} There is a technique called *proxy objects* that can make code along the lines of myObject[x][y] legal. The trick is to define an operator[] function for the class that returns another object that itself overloads operator[]. We'll see this trick used in the upcoming chapter on a custom grid class.

It is legal to add two mathematical vectors to one another; the result is the vector whose components are the pairwise sum of each of the components of the source vectors. If we wanted to define a += operator for Vector3D to let us perform this addition, we would modify the interface of Vector3D as follows:

```
class Vector3D {
public:
    /* ... */
    Vector3D& operator+= (const Vector3D& other);
private:
    static const int NUM_COORDINATES = 3;
    double coordinates[NUM_COORDINATES];
};
```

This could then be implemented as

```
Vector3D& Vector3D::operator +=(const Vector3D& other) {
   for(int i = 0; i < NUM_COORDINATES; ++i)
        coordinates[i] += other.coordinates[i];
   return *this;
}</pre>
```

If you'll notice, <code>operator+=</code> returns *this, a reference to the receiver object. Recall that when overloading operators, you should make sure to define your operators such that they work identically to the C++ built-in operators. It turns out that the += operator yields an lvalue, so the code below, though the quintessence of abysmal style, is perfectly legal:

int one, two, three, four; (one += two) += (three += four);

Since overloaded operators let custom types act like primitives, the following code should also compile:

```
Vector3D one, two, three, four;
(one += two) += (three += four);
```

If we expand out the calls to the overloaded += operator, we find that this is equivalent to

```
Vector3D one, two, three, four;
one.operator+=(two).operator +=(three.operator +=(four));
```

Note that the reference returned by one.operator+=(two) then has its own += operator invoked. Since operator += is not marked const, had the += operator returned a const reference, this code would have been illegal. Make sure to have any (compound) assignment operator return *this as a non-const reference.

Unlike the regular assignment operator, with the compound assignment operator it's commonly meaningful to accept objects of different types as parameters. For example, we might want to make expressions like myVector *= 137 for Vector3Ds meaningful as a scaling operation. In this case, we can simply define an operator *= that accepts a double as its parameter. For example:

```
class Vector3D {
public:
    /* ... */
    Vector3D& operator += (const Vector3D& other);
    Vector3D& operator *= (double scaleFactor);
private:
    static const int NUM_COORDINATES = 3;
    double coordinates[NUM_COORDINATES];
};
```

Despite the fact that the receiver and parameter have different types, this is perfectly legal C++. Here's one possible implementation:

```
Vector3D& Vector3D::operator*= (double scaleFactor) {
   for(int k = 0; k < NUM_COORDINATES; ++k)
        coordinates[k] *= scaleFactor;
   return *this;
}</pre>
```

Although we have implemented operator+= and operator*= for the Vector3D class, C++ will not automatically provide us an implementation of operator-= and operator/=, despite the fact that those functions can easily be implemented as wrapped calls to the operators we've already implemented. This might seem counterintuitive, but prevents errors from cases where seemingly symmetric operations are undefined. For example, it is legal to multiply a vector and a matrix, though the division is undefined. For completeness' sake, we'll prototype operator-= and operator/= as shown here:

```
class Vector3D {
public:
    /* ... */
    Vector3D& operator += (const Vector3D& other);
    Vector3D& operator -= (const Vector3D& other);
    Vector3D& operator *= (double scaleFactor);
    Vector3D& operator /= (double scaleFactor);
private:
    static const int NUM_COORDINATES = 3;
    double coordinates[NUM_COORDINATES];
};
```

Now, how might we go about implementing these operators? operator/= is the simplest of the two and can be implemented as follows:

```
Vector3D& Vector3D::operator /= (double scaleFactor) {
    *this *= 1.0 / scaleFactor;
    return *this;
}
```

This implementation, though cryptic, is actually quite elegant. The first line, *this *= 1.0 / scaleFactor, says that we should multiply the receiver object (*this) by the reciprocal of scaleFactor. The *= operator is the compound multiplication assignment operator that we wrote above, so this code invokes operator*= on the receiver. In fact, this code is equivalent to

```
Vector3D& Vector3D::operator /= (double scaleFactor) {
    operator*= (1.0 / scaleFactor);
    return *this;
}
```

Depending on your taste, you might find this particular syntax more readable than the first version. Feel free to use either version.

Now, how would we implement operator-=, which performs a componentwise subtraction of two Vector3Ds? At a high level, subtracting one vector from another is equal to adding the inverse of the second vector to the first, so we might want to write code like this:

```
Vector3D& Vector3D::operator -= (const Vector3D& other) {
    *this += -other;
    return *this;
}
```

That is, we add -other to the receiver object. But this code is illegal because we haven't defined the unary minus operator as applied to Vector3Ds. Not to worry – we can overload this operator as well. The syntax for this function is as follows:

```
class Vector3D {
public:
    /* ... */
    Vector3D& operator += (const Vector3D& other);
    Vector3D& operator -= (const Vector3D& other);
    Vector3D& operator *= (double scaleFactor);
    Vector3D& operator /= (double scaleFactor);
    vector3D& operator /= (double scaleFactor);
    ronst Vector3D operator- () const;

private:
    static const int NUM_COORDINATES = 3;
    double coordinates[NUM_COORDINATES];
};
```

There are four pieces of information about this function that deserve attention:

- The name of the unary minus function is operator -.
- The function takes no parameters. This lets C++ know that the function is the *unary* minus function (I.e. -myVector) rather than the *binary* minus function (myVector myOtherVector).
- The function returns a const Vector3D. The unary minus function returns an *rvalue* rather than an *lvalue*, since code like -x = 137 is illegal. As mentioned above, this means that the return value of this function should be a const Vector3D.
- The function is marked const. Applying the unary minus to an object doesn't change its value, and to enforce this restriction we'll mark operator const.

One possible implementation of operator- is as follows:

```
const Vector3D Vector3D::operator- () const {
    Vector3D result;
    for(int k = 0; k < NUM_COORDINATES; ++k)
        result.coordinates[k] = -coordinates[k];
    return result;
}</pre>
```

Note that the return type of this function is const Vector3D while the type of result inside the function is Vector3D. This isn't a problem, since returning an object from a function yields a new temporary object and it's legal to initialize a const Vector3D using a Vector3D.

When writing compound assignment operators, as when writing regular assignment operators, you must be careful that self-assignment works correctly. In the above example with Vector3D's compound assignment operators we didn't need to worry about this because the code was structured correctly. However, when working with the C++ string's += operator, since the string needs to allocate a new buffer capable of holding the current string appended to itself, it would need to handle the self-assignment case, either by explicitly checking for self-assignment or through some other means.

Overloading Mathematical Operators

In the previous section, we provided overloaded versions of the += family of operators. Thus, we can now write classes for which expressions of the form one += two are valid. However, the seemingly equivalent expression one = one + two will still not compile, since we haven't provided an implementation of the lone + operator. C++ will not automatically provide implementations of related operators given a single overloaded operator, since in some cases this could result in nonsensical or meaningless behavior.

The built-in mathematical operators yield rvalues, so code like (x + y) = 137 will not compile. Consequently, when overloading the mathematical operators, make sure they return rvalues as well by having them return const objects.

Let's consider an implementation of <code>operator +</code> for our <code>Vector3D</code> class. Because the operator yields an rvalue, we're supposed to return a <code>const Vector3D</code>, and based on our knowledge of parameter passing, we know that we should accept a <code>const Vector3D</code> & as a parameter. There's one more bit we're forget-ting, though, and that's to mark the <code>operator +</code> function <code>const</code>, since <code>operator +</code> creates a new object and doesn't modify either of the values used in the arithmetic statement. This results in the following code

```
class Vector3D {
public:
    /* ... */
    Vector3D& operator += (const Vector3D& other);
    const Vector3D operator+ (const Vector3D& other);
    Vector3D& operator -= (const Vector3D& other);
    Vector3D& operator *= (double scaleFactor);
    Vector3D& operator /= (double scaleFactor);
    vector3D& operator /= (double scaleFactor);
    const Vector3D operator- () const;

private:
    static const int NUM_COORDINATES = 3;
    double coordinates[NUM_COORDINATES];
};
```

How are we to implement this function? We could just do a component-by-component addition, but it's actually much easier to just write the function in terms of our <code>operator +=</code>. The full version of this code is shown below:

```
const Vector3D Vector3D::operator +(const Vector3D& other) const {
    Vector3d result = *this; // Make a deep copy of this Vector3D.
    result += other; // Use existing addition code.
    return result;
}
```

Now, all of the code for operator + is unified, which helps cut down on coding errors.

There is an interesting and common case we haven't addressed yet – what if one of the operands isn't of the same type as the class? For example, if you have a Matrix class that encapsulates a 3x3 matrix, as shown here:

```
class Matrix {
public:
    /* ... */
    Matrix& operator *= (double scalar); // Scale all entries
private:
    static const int MATRIX_SIZE = 3;
    double entries[MATRIX_SIZE][MATRIX_SIZE];
};
```

Note that there is a defined *= operator that scales all elements in the matrix by a double factor. Thus code like myMatrix *= 2.71828 is well-defined. However, since there's no defined operator *, currently we cannot write myMatrix = myMatrix * 2.71828.

Initially, you might think that we could define operator * just as we did operator + in the previous example. While this will work in most cases, it will lead to some problems we'll need to address later. For now, however, let's add the member function operator * to Matrix, which is defined as

```
const Matrix Matrix::operator *(double scalar) const {
    MyMatrix result = *this;
    result *= scalar;
    return result;
}
```

Now, we can write expressions like myMatrix = myMatrix * 2.71828. However, what happens if we write code like myMatrix = 2.71828 * myMatrix? This is a semantically meaningful expression, but unfortunately it won't compile. When interpreting overloaded operators, C++ will always preserve the order of values in an expression.* Thus 2.71828 * myMatrix is *not* the same as myMatrix * 2.71828. Remember that the reason that myMatrix * 2.71828 is legal is because it's equivalent to myMatrix.operator *(2.71828). The expression 2.71828 * myMatrix, on the other hand, is illegal because C++ will try to expand it into (2.71828).operator *(myMatrix), which makes no sense.

^{*} One major reason for this is that sometimes the arithmetic operators won't be commutative. For example, given matrices **A** and **B**, **AB** is not necessarily the same as **BA**, and if C++ were to arbitrarily flip parameters it could result in some extremely difficult-to-track bugs.

To fix this, we can make operator * a free function that accepts two parameters, a double and a Matrix, and returns a const Matrix. Thus code like 2.71828 * myMatrix will expand into calls to operator * (2.71828, myMatrix). The new version of operator * is defined below:

```
const Matrix operator * (double scalar, const Matrix& matrix) {
    Matrix result = *matrix;
    matrix *= scalar;
    return result;
}
```

But here we run into the same problem as before if we write myMatrix * 2.71828, since we haven't defined a function accepting a Matrix as its first parameter and an double as its second. To fix this, we'll define a *second* free function operator * with the parameters reversed that's implemented as a call to the other version:

```
const Matrix operator *(const Matrix& matrix, double scalar) {
    return scalar * matrix; // Calls operator* (scalar, matrix)
}
```

As a general rule, mathematical operators like + should always be implemented as free functions. This prevents problems like those described here.

One important point to notice about overloading the mathematical operators versus the compound assignment operators is that it's considerably faster to use the compound assignment operators over the standalone mathematical operators. Not only do the compound assignment operators work in-place (that is, they modify existing objects), but they also return references instead of full objects. From a performance standpoint, this means that given these three strings:

```
string one = "This ";
string two = "is a ";
string three = "string!";
```

Consider these two code snippets to concatenate all three strings:

```
/* Using += */
string myString = one;
myString += two;
myString += three;
/* Using + */
string myString = one + two + three
```

Oddly, the second version of this code is considerably slower than the first because the + operator generates temporary objects. Remember that one + two + three is equivalent to

```
operator +(one, operator +(two, three))
```

Each call to operator + returns a new string formed by concatenating the parameters, so the code one + two + three creates two temporary string objects. The first version, on the other hand, generates no temporary objects since the += operator works in-place. Thus while the first version is less sightly, it is significantly faster than the second.

Overloading ++ and --

Overloading the increment and decrement operators can be a bit tricky because there are two versions of each operator: *prefix* and *postfix*. Recall that x++ and ++x are different operations – the first will evaluate to the value of x, then increment x, while the second will increment x and then evaluate to the updated value of x. You can see this below:

```
int x = 0
cout << x++ << endl; // Prints: 0
cout << x << endl; // Prints: 1
x = 0;
cout << ++x << endl; // Prints: 1
cout << x << endl; // Prints: 1</pre>
```

Although this distinction is subtle, it's tremendously important for efficiency reasons. In the postfix version of ++, since we have to return the value of the variable was before it was incremented, we'll need to make a full copy of the old version and then return it. With the prefix ++, since we're returning the current value of the variable, we can simply return a reference to it. Thus the postfix ++ can be noticeably slower than the prefix version; this is the reason that when advancing an STL iterator it's faster to use the prefix increment operator.

The next question we need to address is how we can legally use ++ and -- in regular code. Unfortunately, it can get a bit complicated. For example, the following code is totally legal:

```
int x = 0;
++++++++++++x; // Increments x seven times.
```

This is legal because it's equivalent to

++(++(++(++(++(++X)))))));

The prefix ++ operator returns the variable being incremented as an *lvalue*, so this statement means "increment x, then increment x again, etc."

However, if we use the postfix version of ++, as seen here:

```
x+++++++++++; // Error
```

We get a compile-time error because x++ returns the original value of x as an *rvalue*, which can't be incremented because that would require putting the rvalue on the left side of an assignment (in particular, x = x + 1).

Now, let's actually get into some code. Unfortunately, we can't just sit down and write <code>operator ++</code>, since it's unclear *which* <code>operator ++</code> we'd be overloading. C++ uses a hack to differentiate between the prefix and postfix versions of the increment operator: when overloading the prefix version of ++ or --, you write <code>operator ++</code> as a function that takes no parameters. To overload the postfix version, you'll overload <code>op-erator ++</code>, but the overloaded operator will accept as a parameter the integer value 0. In code, these two declarations look like

```
class MyClass {
public:
    /* ... */
    MyClass& operator ++(); // Prefix
    const MyClass operator ++(int dummy); // Postfix
private:
    /* ... */
};
```

Note that the prefix version returns a MyClass& as an lvalue and the postfix version a const MyClass as an rvalue.

We're allowed to implement ++ and -- in any way we see fit. However, one of the more common tricks is to write the ++ implementation as a wrapped call to <code>operator +=</code>. Assuming you've provided this function, we can then write the prefix <code>operator ++</code> as

```
MyClass& MyClass::operator ++() {
    *this += 1;
    return *this;
}
```

And the postfix operator ++ as

```
const MyClass MyClass::operator ++(int dummy) {
    MyClass oldValue = *this; // Store the current value of the object.
    ++*this;
    return oldValue;
}
```

Notice that the postfix <code>operator++</code> is implemented in terms of the prefix <code>operator++</code>. This is a fairly standard technique and cuts down on the amount of code that you will need to write for the functions.

In your future C++ career, you may encounter versions of <code>operator++</code> that look like this:

```
const MyClass MyClass::operator ++(int) {
    MyClass oldValue = *this; // Store the current value of the object.
    ++*this;
    return oldValue;
}
```

Although this function takes in an int parameter, that parameter does not have a name. It turns out that it is perfectly legal C++ code to write functions that accept parameters but do not give names to those parameters. In this case, the function acts just like a regular function that accepts a parameter, except that the parameter cannot be used inside of the function. In the case of <code>operator++</code>, this helps give a cue to readers that the integer parameter is not meaningful and exists solely to differentiate the prefix and postfix versions of the function.

Overloading Relational Operators

Perhaps the most commonly overloaded operators (other than operator =) are the relational operators; for example, < and ==. Unlike the assignment operator, by default C++ does not provide relational operators for your objects. This means that you must explicitly overload the == and related operators to use

them in code. The prototype for the relational operators looks like this (written for <, but can be for any of the relational operators):

```
class MyClass {
public:
    /* ... */
    bool operator < (const MyClass& other) const;
private:
    /* ... */
};</pre>
```

You're free to choose any means for defining what it means for one object to be "less than" another. However, when doing so, you must take great care to ensure that your less-than operator defines a *total ordering* on objects of your type. This means that the following must be true about the behavior of the less-than operator:

- **Trichotomy**: For any *a* and *b*, exactly one of *a* < *b*, *a* = *b*, and *b* < *a* is true.
- **Transitivity**: If *a* < *b* and *b* < *c*, then *a* < *c*.

These properties of < are important because they allow the notion of *sorted order* to make sense. If either of these conditions does not hold, then it is possible to encounter strange situations in which a collection of elements cannot be put into ascending order. For example, suppose that we have the following class, which represents a point in two-dimensional space:

```
class Point {
public:
    Point(double x, double y);
    double getX() const;
    void setX(double value);
    double getY() const;
    void setY(double value);
}
```

Now consider the following implementation of a less-than operator for comparing Points:

```
bool operator< (const Point& one, const Point& two) {
    return one.getX() < two.getX() && one.getY() < two.getY();
}</pre>
```

Intuitively, this may seem like a reasonable definition of the < operator: point a is less than point b if both coordinates of a are less than the corresponding coordinates of b. However, this implementation of < is bound to cause problems. In particular, consider the following code:

Point one(1, 0), two(0, 1); cout << (one < two) << endl; cout << (two < one) << endl;</pre>

Here, we create two points called one and two and compare them using the < operator. What will the first line print? Using the above definition of operator<, the comparison one < two will evaluate to false because the x coordinate of one is greater than the x coordinate of two. But what about two < one? In this case, two's x coordinate is less than one's, but its y coordinate is greater than one's. Consequently, we have that two < one also evaluates to false. We have reached a precarious situation. We have found two

values, one and two, such that one and two do not have equal values, but neither is less than the other. This means that we could not possibly sort a list of elements containing both one and two, since neither one precedes the other.

The problem with the above implementation of <code>operator<</code> is that it violates trichotomy. Recall from the above definition of a total ordering that trichotomy means that exactly one of a < b, a = b, a > b must hold for any a and b. Our definition of <code>operator<</code> does not have this property, as illustrated above. Consequently, we have a legal implementation of <code>operator<</code> that is wholly incorrect. We'll need to redefine how <code>operator<</code> works in order to ensure that trichotomy holds.

One common strategy for implementing <code>operator<</code> is to use what's called a *lexicographical ordering*. To illustrate a lexicographically ordering, consider the words **about** and **above** and think about how you would compare them alphabetically. You'd begin by noting that the first letter of each word was the same, as was the second and the third. However, the fourth letter of the words disagree, and in particular the letter **u** from **about** precedes the letter **v** from **above**. Consequently, we would say that **about** comes lexicographically before **above**. Interestingly, though, the last letter of **about** (**t**) comes after the last letter of **above** (**e**). We don't care, though, because we stopped comparing letters as soon as we found the first mismatch in the words.

This strategy has an elegant analog for arbitrary types. Given a type, one way to implement <code>operator<</code> is as follows. Given two objects a and b of that type, check whether the first field of a and b are not the same. If so, say that a is smaller if its first field is smaller than b's first field. Otherwise, look at the second field. If the fields are not the same, then return a if a's second field is smaller than b's and b otherwise. If not, then look at the third field, etc. To give you a concrete example of how this works, consider the following revision to the Point's operator< function:

```
bool operator< (const Point& one, const Point& two) {
    if (one.getX() != two.getX()) return one.getX() < two.getX();
    return one.getY() < two.getY();
}</pre>
```

Here, we first check whether the points disagree in their *x* coordinate. If so, we say that one is less than two only if it has a smaller *x* coordinate. Otherwise, if the points agree in their *x* coordinate, then whichever has the lower *y* coordinate is said to have the smaller value. Amazingly, this implementation strategy results in an ordering that is both trichotic and transitive, exactly the properties we want out of the < operator.

Of course, this strategy works on classes that have more than two fields, provided that you compare each field one at a time. It is an interesting exercise to convince yourself that a lexicographical ordering on any type obeys trichotomy, and that such an ordering obeys transitivity as well.

Once you have a working implementation of <code>operator<</code>, it is possible to define all five other relational operators solely in terms of the <code>operator<</code>. This is due to the following set of relations:

 $A < B \iff A < B$ $A <= B \iff ! (B < A)$ $A == B \iff ! (A < B || B < A)$ $A != B \iff A < B || B < A$ $A >= B \iff ! (A < B)$ $A >= B \iff B < A$

For example, we could implement operator> for the Point class as

```
bool operator> (const Point& one, const Point& two) {
    return two < one;
}</pre>
```

We could similarly implement operator<= for Points as

```
bool operator<= (const Point& one, const Point& two) {
    return !(one < two);
}</pre>
```

This is a fairly standard technique, and it's well worth the effort to remember it.

Storing Objects in STL maps

Up to this point we've avoided storing objects as keys in STL maps. Now that we've covered operator overloading, though, you have the necessary knowledge to store objects in the STL map and set containers.

Internally, the STL map and set are layered on binary trees that use the relational operators to compare elements. Due to some clever design decisions, STL containers and algorithms only require the < operator to compare two objects. Thus, to store a custom class inside a map or set, you simply need to overload the < operator and the STL will handle the rest. For example, here's some code to store a Point struct in a map:

```
struct pointT {
    int x, y;
    bool operator < (const pointT& other) const {
        if(x != other.x)
            return x < other.x;
        return y < other.y;
    }
};
map<pointT, int> myMap; // Now works using the default < operator.</pre>
```

You can use a similar trick to store objects as values in a set.

friend

Normally, when you mark a class's data members private, only instances of that class are allowed to access them. However, in some cases you might want to allow specific other classes or functions to modify private data. For example, if you were implementing the STL map and wanted to provide an iterator class to traverse it, you'd want that iterator to have access to the map's underlying binary tree. There's a slight problem here, though. Although the iterator is an integral component of the map, like all other classes, the iterator cannot access private data and thus cannot traverse the tree.

How are we to resolve this problem? Your initial thought might be to make some public accessor methods that would let the iterator modify the object's internal data representation. Unfortunately, this won't work particularly well, since then *any* class would be allowed to use those functions, something that violates the principle of encapsulation. Instead, to solve this problem, we can use the C++ friend keyword to grant the iterator class access to the map or set's internals. Inside the map declaration, we can write the following:

Now, since iterator is a friend of map, it can read and modify the map's private data members.

Just as we can grant other classes friend access to a class, we can give friend access to global functions. For example, if we had a free function ModifyMyClass that accepted a MyClass object as a reference parameter, we could let ModifyMyClass modify the internal data of MyClass if inside the MyClass declaration we added the line

```
class MyClass {
public:
    /* ... */
    friend void ModifyMyClass(MyClass& param);
};
```

The syntax for friend can be misleading. Even though we're prototyping ModifyMyClass inside the My-Class function, because ModifyMyClass is a friend of MyClass it is **not** a member function of MyClass. After all, the purpose of the friend declaration is to give outside classes and functions access to the MyClass internals.

When using friend, there are two key points to be aware of. First, the friend declaration must precede the actual implementation of the friend class or function. Since C++ compilers only make a single pass over the source file, if they haven't seen a friend declaration for a function or class, when the function or class tries to modify your object's internals, the compiler will generate an error. Second, note that while friend is quite useful in some circumstances, it can quickly lead to code that entirely defeats the purpose of encapsulation. Before you grant friend access to a piece of code, make sure that the code has a legitimate reason to be modifying your object. That is, don't make code a friend simply because it's easier to write that way. Think of friend as a way of extending a class definition to include other pieces of code. The class, together with all its friend code, should comprise a logical unit of encapsulation.

When overloading an operator as a free function, you might want to consider giving that function friend access to your class. That way, the functions can efficiently read your object's private data without having to go through getters and setters.

Unfortunately, friend does not interact particularly intuitively with template classes. Suppose we want to provide a friend function PQueueFriend for a template version of the CS106B/X PQueue. If PQueueFriend is declared like this:

```
template <typename T> void PQueueFriend(const PQueue<T>& pq) {
   /* ... */
}
```

You'll notice that PQueueFriend itself is a template function. This means that when declaring PQueueFriend a friend of the template PQueue, we'll need to make the friend declaration templatized, as shown here:

```
template <typename T> class PQueue {
public:
    /* ... */
    template <typename T> friend PQueueFriend(const PQueue<T>& pq);
};
```

If you forget the template declaration, then your code will compile correctly but will generate a linker error. While this can be a bit of nuisance, it's important to remember since it arises frequently when overloading the stream operators, as you'll see below.

Overloading the Stream Insertion Operator

Have you ever wondered why cout << "Hello, world!" << endl is syntactically legal? It's through the overloaded << operator in conjunction with ostreams.* In fact, the entire streams library can be thought of as a gigantic library of massively overloaded << and >> operators.

The C++ streams library is designed to give you maximum flexibility with your input and output routines and even lets you define your own stream insertion and extraction operators. This means that you are allowed to define the << and >> operators so that expressions like cout << myClass << endl and cin >> m_YClass are well-defined. However, when writing stream insertion and extraction operators, there are huge number of considerations to keep in mind, many of which are beyond the scope of this text. This next section will discuss basic strategies for overloading the << operator, along with some limitations of the simple approach.

As with all overloaded operators, we need to consider what the parameters and return type should be for our overloaded << operator. Before considering parameters, let's think of the return type. We know that it should be legal to chain stream insertions together – that is, code like cout << 1 << 2 << endl should compile correctly. The << operator associates to the left, so the above code is equal to

(((cout << 1) << 2) << endl);

Thus, we need the << operator to return an ostream. Now, we don't want this stream to be const, since then we couldn't write code like this:

cout << "This is a string!" << setw(10) << endl;</pre>

Since if cout << "This is a string!" evaluated to a const object, we couldn't set the width of the next operation to 10. Also, we cannot return the stream by value, since stream classes have their copy functions marked private. Putting these two things together, we see that the stream operators should return a non-const reference to whatever stream they're referencing.

Now let's consider what parameters we need. We need to know what stream we want to write to or read from, so initially you might think that we'd define overloaded stream operators as member functions that look like this:

```
class MyClass {
public:
    ostream& operator << (ostream& input) const; // Problem: Legal but incorrect
};</pre>
```

^{*} As a reminder, the <code>ostream</code> class is the base class for output streams. This has to do with inheritance, which we'll cover in a later chapter, but for now just realize that it means that both <code>stringstream</code> and <code>ofstream</code> are specializations of the more generic <code>ostream</code> class.

Unfortunately, this isn't correct. Consider the following two code snippets:

cout << myClass; myClass << cout;</pre>

The first of these two versions makes sense, while the second is backwards. Unfortunately, with the above definition of <code>operator <<</code>, we've accidentally made the second version syntactically legal. The reason is that these two lines expand into calls to

```
cout.operator <<(myClass);
myClass.operator <<(cout);</pre>
```

The first of these two isn't defined, since cout doesn't have a member function capable of writing our object (if it did, we wouldn't need to write a stream operator in the first place!). However, based on our previous definition, the second version, while semantically incorrect, is syntactically legal. Somehow we need to change how we define the stream operator so that we are allowed to write cout << myClass. To fix this, we'll make the overloaded stream operator a free function that takes two parameters – an ostream to write to and a myClass object to write. The code for this is:

```
ostream& operator << (ostream& stream, const MyClass& mc) {
    /* ... implementation ... */
    return stream;
}</pre>
```

While this code will work correctly, because <code>operator <<</code> is a free function, it doesn't have access to any of the private data members of <code>MyClass</code>. This can be a nuisance, since we'd like to directly write the contents of <code>MyClass</code> out to the stream without having to go through the (possibly inefficient) getters and setters. Thus, we'll declare <code>operator << a friend</code> inside the <code>MyClass</code> declaration, as shown here:

```
class MyClass {
public:
    /* More functions. */
    friend ostream& operator <<(ostream& stream, const MyClass& mc);
};</pre>
```

Now, we're all set to do reading and writing inside the body of the insertion operator. It's not particularly difficult to write the stream insertion operator – all that we need to do is print out all of the meaningful class information with some formatting information. So, for example, given a Point class representing a point in 2-D space, we could write the insertion operator as

```
ostream& operator <<(ostream& stream, const Point& pt) {
    stream << '(' << pt.x << ", " << pt.y << ')';
    return stream;
}</pre>
```

While this code will work in most cases, there are a few spots where it just won't work correctly. For example, suppose we write the following code:

```
cout << "01234567890123456789" << endl; // To see the number of characters.
cout << setw(20) << myPoint << endl;</pre>
```

Looking at this code, you'd expect that it would cause myPoint to be printed out and padded with space characters until it is at least twenty characters wide. Unfortunately, this isn't what happens. Since operator << writes the object one piece at a time, the output will look something like this:

01234567890123456789

(0, 4)

That's nineteen spaces, followed by the actual Point data. The problem is that when we invoke operator <<<, the function writes a single (character to stream. It's this operation, not the Point as a whole, that will get aligned to 20 characters. There are many ways to circumvent this problem, but perhaps the simplest is to buffer the output into a stringstream and then write the contents of the stringstream to the destination in a single operation. This can get a bit complicated, especially since you'll need to copy the stream formatting information over.

Writing a correct stream extraction operator (operator >>) is complicated. For more information on writing stream extraction operators, consult a reference.

Overloading * and ->

Consider the following code snippet:

```
for(set<string>::iterator itr = mySet.begin(); itr != mySet.end(); ++itr)
        cout << *itr << " has length " << itr->length() << endl;</pre>
```

Here, we traverse a set<string> using iterators, printing out each string and its length. Interestingly, even though set iterators are not raw pointers (they're objects capable of traversing binary trees), thanks to operator overloading, they can respond to the * and -> operators as though they were regular C++ pointers.

If you create a custom class that acts like a C++ pointer (perhaps a custom iterator or "smart pointer," a topic we'll return to later), you can provide implementations of the pointer dereference and member selection operators * and -> by overloading their respective operator functions. The simpler of these two functions is the pointer dereference operator. To make an object that can be dereferenced to yield an object of type T, the syntax for its * operator is

```
class PointerClass {
public:
    T& operator *() const;
    /* ... */
};
```

You can invoke the <code>operator *</code> function by "dereferencing" the custom pointer object. For example, the following code:

*myCustomPointer = 137;

is completely equivalent to

```
myCustomPointer.operator *() = 137;
```

Because we can assign a value to the result of operator *, the operator * function should return an lvalue (a non-const reference).

There are two other points worth noting here. First, how can C++ distinguish this <code>operator *</code> for pointer dereference from the <code>operator *</code> used for multiplication? The answer has to do with the number of parameters to the function. Since a pointer dereference is a unary operator, the function prototype for the pointer-dereferencing <code>operator *</code> takes no parameters. Had we wanted to write <code>operator *</code> for multiplication.

plication, we would have written a function operator * that accepts a parameter (or a free function accepting two parameters). Second, why is operator * marked const? This has to do with the difference between const pointers and pointers-to-const. Suppose that we have a const instance of a custom pointer class. Since the pointer *object* is const, it acts as though it is a const pointer rather than a pointer-to-const. Consequently, we should be able to dereference the object and modify its stored pointer without affecting its constness.

The arrow operator <code>operator -></code> is slightly more complicated than <code>operator *</code>. Initially, you might think that <code>operator -></code> would be a binary operator, since you use the arrow operator in statements like <code>myClassPtr->myElement</code>. However, C++ has a rather clever mechanism for <code>operator -></code> that makes it a unary operator. A class's <code>operator -></code> function should return a pointer to the object that the arrow operator should actually be applied to. This may be a bit confusing, so an example is in order. Suppose we have a class <code>CustomStringPointer</code> that acts as though it's a pointer to a C++ <code>string</code> object. Then if we have the following code:

```
CustomStringPointer myCustomPointer;
cout << myCustomPointer->length() << endl;</pre>
```

This code is equivalent to

```
CustomStringPointer myCustomPointer;
cout << (myCustomPointer.operator ->())->length() << endl;</pre>
```

In the first version of the code, we treated the myCustomPointer object as though it was a real pointer by using the arrow operator to select the length function. This code expands out into two smaller steps:

- 1. The CustomStringPointer's operator -> function is called to determine which pointer the arrow should be applied to.
- 2. The returned pointer then has the -> operator applied to select the length function.

Thus when writing the <code>operator -></code> function, you simply need to return the pointer that the arrow operator should be applied to. If you're writing a custom iterator class, for example, this is probably the element being iterator over.

We'll explore one example of overloading these operators in a later chapter.

List of Overloadable Operators

The following table lists the most commonly-used operators you're legally allowed to overload in C++, along with any restrictions about how you should define the operator.

| Operator | Yields | Usage |
|-------------------|--------|---|
| = | Lvalue | MyClass& operator =(const MyClass& other); |
| | | See the the earlier chapter for details. |
| += -= *= /= %= | Lvalue | MyClass& operator +=(const MyClass& other); |
| (etc.) | | When writing compound assignment operators, make sure that you correctly handle "self-compound-assignment." |

| + - * / % | Rvalue | <pre>const MyClass operator + (const MyClass& one,</pre> |
|--------------------|-----------------------------------|--|
| (etc.) | | These operator should be defined as a free functions. |
| < <= == > >= != | Rvalue | <pre>bool operator < (const MyClass& other) const; bool operator < (const MyClass& one,</pre> |
| | | If you're planning to use relational operators only for the STL container classes, you just need to overload the < operator. Otherwise, you should overload all six so that users aren't surprised that one $!= two$ is illegal while $! (one == two)$ is defined. |
| [] | Lvalue | ElemType& operator [](const KeyType& key); const ElemType& operator [](const KeyType& key) const; |
| | | Most of the time you'll need a const-overloaded version of the bracket operator. Forgetting to provide one can lead to a real headache! |
| ++ | Prefix: Lvalue Postfix: Rvalue | <pre>Prefix version: MyClass& operator ++(); Postfix version: const MyClass operator ++(int dummy);</pre> |
| - | Rvalue | const MyClass operator -() const; |
| * | Lvalue | <pre>ElemType& operator *() const;</pre> |
| | | With this function, you're allowing your class to act as though it's a pointer. The return type should be a reference to the object it's "pointing" at. This is how the STL iterators and smart pointers work. Note that this is the unary * operator and is not the same as the * multiplicative operator. |
| -> | Lvalue | <pre>ElemType* operator ->() const;</pre> |
| | | If the -> is overloaded for a class, whenever you write <code>myClass->myMember</code> , it's equivalent to <code>myClass.operator ->()->myMember</code> . Note that the function should be <code>const</code> even though the object returned can still modify data. This has to do with how pointers can legally be used in C++. For more information, refer to the chapter on <code>const</code> . |
| << >> | Lvalue | <pre>friend ostream& operator << (ostream& out,</pre> |
| () | Varies | See the chapter on functors. |

Extended Example: grid

The STL encompasses a wide selection of associative and sequence containers. However, one useful data type that did not find its way into the STL is a multidimensional array class akin to the CS106B/X Grid. In this extended example, we will implement an STL-friendly version of the CS106B/X Grid class, which we'll call grid, that will support STL-compatible iterators, intuitive element-access syntax, and relational operators. Once we're done, we'll have an industrial-strength container class we will use later in this book to implement more complex examples.

Implementing a fully-functional grid may seem daunting at first, but fortunately it's easy to break the work up into several smaller steps that culminate in a working class.

Step 0: Implement the Basic grid Class.

Before diving into some of the grid's more advanced features, we'll begin by implementing the grid basics. Below is a partial specification of the grid class that provides core functionality:

Figure 0: Basic (incomplete) interface for the grid class

```
template <typename T> class grid {
public:
    /* Constructors, destructors. */
                                           // Create empty grid
    grid();
    grid(size t rows, size t cols);
                                        // Construct to specified size
    /* Resizing operations. */
    void clear();
                                            // Empty the grid
    void resize(size_t rows, size_t cols); // Resize the grid
    /* Query operations. */
    size t numRows() const;
                                          // Returns number of rows in the grid
    size_t numRows() const;
size_t numCols() const;
bool_empty() const;
                                          // Returns number of columns in the grid
                                         // Returns whether the grid is empty
   bool empty() const;
                                         // Returns the number of elements
    size_t size() const;
    /* Element access. */
          T& getAt(size t row, int col); // Access individual elements
    const T& getAt(int row, int col) const; // Same, but const
};
```

These functions are defined in greater detail here:

| grid(); | Constructs a new, empty grid. |
|--|---|
| <pre>grid(size_t rows, size_t cols);</pre> | Constructs a new grid with the specified number of rows and columns. Each element in the grid is initialized to its default value. |
| <pre>void clear();</pre> | Resizes the grid to 0x0. |
| <pre>void resize(size_t rows, size_t cols);</pre> | Discards the current contents of the grid and res- izes the grid to the specified size. Each element in the grid is initialized to its default value. |
| <pre>size_t numRows() const; size_t numCols() const;</pre> | Returns the number of rows and columns in the grid. |
| <pre>bool empty() const;</pre> | Returns whether the grid contains no elements. This is true if either the number of rows or columns is zero. |
| <pre>size_t size() const;</pre> | Returns the number of total elements in the grid. |
| <pre>T& getAt(size_t row, size_t col); const T& getAt(size_t row, size_t col) const;</pre> | Returns a reference to the element at the specified position. This function is const-overloaded. We won't worry about the case where the indices are out of bounds. |

Because grids can be dynamically resized, we will need to back grid with some sort of dynamic memory management. Because the grid represents a two-dimensional entity, you might think that we need to use

a dynamically-allocated multidimensional array to store grid elements. However, working with dynamically-allocated multidimensional arrays is tricky and greatly complicates the implementation. Fortunately, we can sidestep this problem by implementing the two-dimensional grid object using a single-dimensional array. To see how this works, consider the following 3x3 grid:

| 0 | 1 | 2 |
|---|---|---|
| 3 | 4 | 5 |
| 6 | 7 | 8 |

We can represent all of the elements in this grid using a one-dimensional array by laying out all of the elements sequentially, as seen here:

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|---|---|---|---|---|---|---|---|---|
| | | | | | | | | 1 |

If you'll notice, in this ordering, the three elements of the first row appear in order as the first three elements, then the three elements of the second row in order, and finally the three elements of the final row in order. Because this one-dimensional representation of a two-dimensional object preserves the ordering of individual rows, it is sometimes referred to as *row-major order*.

To represent a grid in row-major order, we need to be able to convert between grid coordinates and array indices. Given a coordinate (*row, col*) in a grid of dimensions (*nrows, ncols*), the corresponding position in the row-major order representation of that grid is given by *index* = *col* + *row* * *ncols*. The intuition behind this formula is that because the ordering within any row is preserved, each horizontal step in the grid translates into a single step forward or backward in the row-major order representation of the grid. However, each vertical step in the grid requires us to advance forward to the next row in the linearized grid, skipping over *ncols* elements.

Using row-major order, we can back the grid class with a regular STL vector, as shown here:

```
template <typename T> class grid {
public:
    grid();
    grid(size_t rows, size_t cols);
    void clear();
    void resize(size t rows, size t cols);
    size t numRows() const;
    size t numCols() const;
    bool empty() const;
    size t size() const;
          T& getAt(size_t row, size_t col);
    const T& getAt(size t row, size t col) const;
private:
    vector<T> elems;
    size_t rows;
    size_t cols;
};
```

Serendipitously, implementing the grid with a vector allows us to use C++'s automatically-generated copy constructor and assignment operator for grid. Since vector already manages its own memory, we don't need to handle it manually.

Note that we explicitly keep track of the number of rows and columns in the grid even though the vector stores the total number of elements. This is necessary so that we can compute indices in the row-major ordering for points in two-dimensional space.

The above functions have relatively straightforward implementations that are given below:

```
template <typename T> grid<T>::grid() : rows(0), cols(0) {
}
template <typename T>
grid<T>::grid(size t rows, size t cols)
 : elems(rows * cols), rows(rows), cols(cols) {
}
template <typename T> void grid<T>::clear() {
   resize(0, 0);
}
template <typename T> void grid<T>::resize(size t rows, size t cols) {
    /* See below for assign */
    elems.assign(rows * cols, ElemType());
    /* Explicit this-> required since parameters have same name as members. */
    this->rows = rows;
   this->cols = cols;
}
template <typename T> size t grid<T>::numRows() const {
   return rows;
}
template <typename T> size t grid<T>::numCols() const {
   return cols;
}
template <typename T> bool grid<T>::empty() const {
   return size() == 0;
}
template <typename T> size t grid<T>::size() const {
   return numRows() * numCols();
}
/* Use row-major ordering to access the proper element of the vector. */
template <typename T> T& grid<T>::getAt(size t row, size t col) {
    return elems[col + row * cols];
}
template <typename T> const T& grid<T>::getAt(size t row,size t col) const {
   return elems[col + row * cols];
}
```

Most of these functions are one-liners and are explained in the comments. The only function that you may find interesting is resize, which uses the vector's assign member function. assign is similar to resize in that it changes the size of the vector, but unlike resize assign discards all of the current vector contents and replaces them with the specified number of copies of the specified element. The use of ElemType() as the second parameter to assign means that we will fill the vector with copies of the default value of the type being stored (since ElemType() uses the temporary object syntax to create a new ElemType).

Step 1: Add Support for Iterators

Now that we have the basics of a grid class, it's time to add iterator support. This will allow us to plug the grid directly into the STL algorithms and will be invaluable in a later chapter.

Like the map and set, the grid does not naturally lend itself to a linear traversal – after all, grid is two-dimensional – and so we must arbitrarily choose an order in which to visit elements. Since we've implemented the grid in row-major order, we'll have grid iterators traverse the grid row-by-row, top to bottom, from left to right. Thus, given a 3x4 grid, the order of the traversal would be

| 0 | 1 | 2 |
|---|----|----|
| 3 | 4 | 5 |
| 6 | 7 | 8 |
| 9 | 10 | 11 |

This order of iteration maps naturally onto the row-major ordering we've chosen for the grid. If we consider how the above grid would be laid out in row-major order, the resulting array would look like this:

|--|

Thus this iteration scheme maps to a simple linear traversal of the underlying representation of the grid. Because we've chosen to represent the elements of the grid using a vector, we can iterate over the elements of the grid using vector iterators. We thus add the following definitions to the grid class:

```
template <typename T> class grid {
public:
    grid();
    grid(size t rows, size t cols);
    void clear();
    void resize(size t rows, size t cols);
    size t numRows() const;
    size t numCols() const;
    bool empty() const;
    size t size() const;
    T& getAt(size t row, size t col);
    const T& getAt(size_t row, size_t col) const;
    typedef typename vector<T>::iterator iterator;
    typedef typename vector<T>::const iterator const iterator;
private:
    vector<T> elems;
    size t rows;
    size t cols;
};
```

Now, clients of grid can create grid<int>::iterators rather than vector<int>::iterators. This makes the interface more intuitive and increases encapsulation; since iterator is a typedef, if we later decide to replace the underlying representation with a dynamically-allocated array, we can change the typedefs to

typedef ElemType* iterator; typedef const ElemType* const iterator;

And clients of the grid will not notice any difference.

Notice that in the above typedefs we had to use the typename keyword to name the type vector<Elem-Type>::iterator. This is the pesky edge case mentioned in the chapter on templates and somehow manages to creep into more than its fair share of code. Since iterator is a nested type inside the template type vector<ElemType>, we have to use the typename keyword to indicate that iterator is the name of a type rather than a class constant.

We've now defined an iterator type for our grid, so what functions should we export to the grid clients? We'll at least want to provide support for begin and end, as shown here:

```
template <typename T> class grid {
public:
    grid();
    grid(size t rows, size t cols);
    void clear();
    void resize(size t rows, size t cols);
    size t numRows() const;
    size t numCols() const;
    bool empty() const;
    size t size() const;
    T& getAt(size t row, size t col);
    const T& getAt(size_t row, size_t col) const;
    typedef typename vector<T>::iterator iterator;
    typedef typename vector<T>::const iterator const iterator;
          iterator begin();
    const iterator begin() const;
          iterator end();
    const iterator end() const;
private:
    vector<T> elems;
    size t rows;
    size t cols;
};
```

We've provided two versions of each function so that clients of a const grid can still use iterators. These functions are easily implemented by returning the value of the underlying vector's begin and end functions, as shown here:

```
template <typename T> typename grid<T>::iterator grid<T>::begin() {
    return elems.begin();
}
```

Notice that the return type of this function is typename grid<ElemType>::iterator rather than just iterator. Because iterator is a nested type inside grid, we need to use grid<ElemType>::iterator to specify which iterator we want, and since grid is a template type we have to use the typename keyword to indicate that iterator is a nested type. Otherwise, this function should be straightforward.

The rest of the functions are implemented here:

```
template <typename T> typename grid<T>::const_iterator grid<T>::begin() const {
    return elems.begin();
}
template <typename T> typename grid<T>::iterator grid<T>::end() {
    return elems.end();
}
template <typename T> typename grid<T>::const_iterator grid<T>::end() const {
    return elems.end();
}
```

Because the grid is implemented in row-major order, elements of a single row occupy consecutive locations in the vector. It's therefore possible to return iterators delineating the start and end of each row in the grid. This is useful functionality, so we'll provide it to clients of the grid through a pair of member functions row_begin and row_end (plus const overloads). These functions are declared here:

```
template <typename T> class grid {
public:
    grid();
    grid(size t rows, size t cols);
    void clear();
    void resize(size t rows, size t cols);
    size t numRows() const;
    size t numCols() const;
    bool empty() const;
    size t size() const;
    T& getAt(size t row, size t col);
    const T& getAt(size t row, size t col) const;
    typedef typename vector<ElemType>::iterator iterator;
    typedef typename vector<ElemType>::const iterator const iterator;
          iterator begin();
    const iterator begin() const;
          iterator end();
    const iterator end() const;
          iterator row begin(size t row);
    const_iterator row_begin(size_t row) const;
          iterator row_end(size_t row);
    const iterator row end(size t row) const;
private:
    vector<T> elems;
    size t rows;
    size t cols;
};
```

Before implementing these functions, let's take a minute to figure out exactly where the iterations we return should point to. Recall that the element at position (*row*, 0) in a grid of size (*rows*, *cols*) can be found at position *row* * *cols*. We should therefore have $row_begin(row)$ return an iterator to the row * *cols* element of the vector. Since there are *cols* elements in each row and row_end should return an iterator to one position past the end of the row, this function should return an iterator to the position *cols* past the location returned by row_begin . Given this information, we can implement these functions as shown here:

```
template <typename T> typename grid<T>::iterator grid<T>::row_begin(int row) {
    return begin() + numCols() * row;
}
template <typename T>
    typename grid<T>::const_iterator grid<T>::row_begin(int row) const {
    return begin() + numCols() * row;
}
```

```
template <typename T> typename grid<T>::iterator grid<T>::row_end(int row) {
    return row_begin(row) + numCols();
}
template <typename T>
    typename grid<T>::const_iterator grid<T>::row_end(int row) const {
    return row_begin(row) + numCols();
}
```

We now have an elegant iterator interface for the grid class. We can iterate over the entire container as a whole, just one row at a time, or some combination thereof. This enables us to interface the grid with the STL algorithms. For example, to zero out a grid<int>, we can use the fill algorithm, as shown here:

fill(myGrid.begin(), myGrid.end(), 0);

We can also sort the elements of a row using sort:

```
sort(myGrid.row begin(0), myGrid.row end(0));
```

With only a handful of functions we're now capable of plugging directly into the full power of the algorithms. This is part of the beauty of the STL – had the algorithms been designed to work on containers rather than iterator ranges, this would not have been possible.

Step 2: Add Support for the Element Selection Operator

When using regular C++ multidimensional arrays, we can write code that looks like this:

int myArray[137][42]; myArray[2][4] = 271828; myArray[9][0] = 314159;

However, with the current specification of the grid class, the above code would be illegal if we replaced the multidimensional array with a grid<int>, since we haven't provided an implementation of operator [].

Adding support for element selection to linear classes like the vector is simple – we simply have the brackets operator return a reference to the proper element. Unfortunately, it is much trickier to design grid such that the bracket syntax works correctly. The reason is that if we write code that looks like this:

```
grid<int> myGrid(137, 42);
int value = myGrid[2][4];
```

By replacing the bracket syntax with calls to operator [], we see that this code expands out to

```
grid<int> myGrid(137, 42);
int value = (myGrid.operator[] (2)).operator[] (4);
```

Here, there are *two* calls to operator [], one invoked on myGrid and the other on the value returned by myGrid.operator[](2). To make the above code compile, the object returned by the grid's operator[] must *itself* define an operator [] function. It is this returned object, rather than the grid itself, which is responsible for retrieving the requested element from the grid. Since this temporary object is used to perform a task normally reserved for the grid, it is sometimes known as a *proxy object*.

How can we implement the grid's operator [] so that it works as described above? First, we will need to define a new class representing the object returned by the grid's operator []. In this discussion, we'll call it MutableReference, since it represents an object that can call back into the grid and mutate it. For simplicity and to maximize encapsulation, we'll define MutableReference inside of grid. This results in the following interface for grid:

```
template <typename T> class grid {
public:
    /* ... previously-defined functions ... */
    class MutableReference {
    public:
        friend class grid;
        T& operator[] (size t col);
    private:
        MutableReference(grid* owner, size t row);
        grid* const owner;
        const size t row;
    };
private:
    vector<T> elems;
    size t rows;
    size t cols;
};
```

The MutableReference object stores some a pointer to the grid that created it, along with the index passed in to the grid's operator [] function when the MutableReference was created. That way, when we invoke the MutableReference's operator [] function specifying the *col* coordinate of the grid, we can pair it with the stored *row* coordinate, then query the grid for the element at (*row, col*). We have also made grid a friend of MutableReference so that the grid can call the private constructor necessary to initialize a MutableReference.

We can implement MutableReference as follows:

```
template <typename T>
    grid<T>::MutableReference::MutableReference(grid* owner, int row) :
        owner(owner), row(row) {
    template <typename T>
        T& grid<T>::MutableReference::operator[] (int col) {
        return owner->getAt(row, col);
    }
```

Notice that because MutableReference is a nested class inside grid, the implementation of the MutableReference functions is prefaced with grid<ElemType>::MutableReference instead of just MutableReference. However, in this particular case the pesky typename keyword is not necessary because we are prototyping a function inside MutableReference rather than using the type MutableReference in an expression.

Now that we've implemented MutableReference, we'll define an operator [] function for the grid class that constructs and returns a properly-initialized MutableReference. This function accepts an *row*

coordinate, and returns a MutableReference storing that row number and a pointer back to the grid. That way, if we write

```
int value = myGrid[1][2];
```

The following sequences of actions occurs:

- 1. myGrid.operator[] is invoked with the parameter 1.
- 2. myGrid.operator[] creates a MutableReference storing the *row* coordinate 1 and a means for communicating back with the myGrid object.
- 3. myGrid.operator[] returns this MutableReference.
- 4. The returned MutableReference then has its operator[] function called with parameter 2.
- 5. The returned MutableReference then calls back to the myGrid object and asks for the element at position (1, 2).

This sequence of actions is admittedly complex, but is transparent to the client of the grid class and runs efficiently.

operator[] is defined and implemented as follows:

```
template <typename T> class grid {
public:
    /* ... previously-defined functions ... */
    class MutableReference {
    public:
        friend class grid;
        T& operator[] (size t col);
    private:
        MutableReference(grid* owner, size t row);
        grid* const owner;
        const size t row;
    };
    MutableReference operator[] (int row);
private:
    vector<T> elems;
    size t rows;
    size t cols;
};
template <typename T>
    typename grid<T>::MutableReference grid<T>::operator[] (int row) {
    return MutableReference(this, row);
}
```

Notice that we've only provided an implementation of the non-const version of operator[]. But what if we want to use operator[] on a const grid? We would similarly need to return a proxy object, but that object would need to guarantee that grid clients could not write code like this:

```
const grid<int> myGrid(137, 42);
myGrid[0][0] = 2718; // Ooops! Modified const object!
```

To prevent this sort of problem, we'll have the const version of operator[] return a proxy object of a different type, called ImmutableReference which behaves similarly to MutableReference but which returns const references to the elements in the grid. This results in the following interface for grid:

```
template <typename T> class grid {
public:
    /* ... previously-defined functions ... */
    class MutableReference {
    public:
        friend class grid;
        T& operator[] (size t col);
    private:
        MutableReference(grid* owner, size t row);
        grid* const owner;
        const size_t row;
    };
    MutableReference operator[] (int row);
    class ImmutableReference {
    public:
        friend class grid;
        const T& operator[] (size t col) const;
    private:
        MutableReference(const grid* owner, size t row);
        const grid* const owner;
        const size_t row;
    };
    ImmutableReference operator[] (size t row) const;
private:
    vector<T> elems;
    size t rows;
    size t cols;
};
```

ImmutableReference and the const version of operator[] are similar to MutableReference and the non-const version of operator[], and to save space we won't write it here. The complete listing of the grid class at the end of this chapter contains the implementation if you're interested.

Step 3: Define Relational Operators

Now that our grid has full support for iterators and a nice bracket syntax that lets us access individual elements, it's time to put on the finishing touches. As a final step in the project, we'll provide implementations of the relational operators for our grid class. We begin by updating the grid interface to include the following functions:

```
template <typename T> class grid {
public:
    /* ... previously-defined functions ... */
    bool operator < (const grid& other) const;
    bool operator <= (const grid& other) const;
    bool operator == (const grid& other) const;
    bool operator != (const grid& other) const;
    bool operator >= (const grid& other) const;
};
```

Note that of the six operators listed above, only the == and != operators have intuitive meanings when applied to grids. However, it also makes sense to define a < operator over grids so that we can store them in STL map and set containers, and to ensure consistency, we should define the other three operators as well.

Because there is no natural interpretation for what it means for one grid to be "less than" another, we are free to implement these functions in any way that we see fit, provided that we obey transitivity and trichotomy. As mentioned earlier it is possible to implement all six of the relational operators in terms of the less-than operator. One strategy for implementing the relational operators is thus to implement just the less-than operator and then to define the other five as wrapped calls to <code>operator <.</code> But what is the best way to determine whether one <code>grid</code> compares less than another? One general approach is to define a *lexicographical ordering* over <code>grids</code>. We will compare each field one at a time, checking to see if the fields are equal. If so, we move on to the next field. Otherwise, we immediately return that one <code>grid</code> is less than another without looking at the remaining fields. If we go through every field and find that the <code>grids</code> are equal, then we can return that neither grid is less than the other. This is similar to the way that we might order words alphabetically – we find the first mismatched character, then return which word compares first. We can begin by implementing operator < as follows:

```
template <typename T> bool grid<T>::operator < (const grid& other) const {
    /* Compare the number of rows and return if there's a mismatch. */
    if(rows != other.rows)
        return rows < other.rows;
    /* Next compare the number of columns the same way. */
    if(cols != other.cols)
        return cols < other.cols;
    /* ... */
}</pre>
```

Here, we compare the rows fields of the two objects and immediately return if they aren't equal. We can then check the cols fields in the same way. Finally, if the two grids have the same number of rows and columns, we need to check how the elements of the grids compare. Fortunately, this is straightforward thanks to the STL lexicographical_compare algorithm. lexicographical_compare accepts four iterators delineating two ranges, then lexicographically compares the elements in those ranges and returns if the first range compares lexicographically less than the second. Using lexicographical_compare, we can finish our implementation of operator < as follows:

```
template <typename T> bool grid<T>::operator < (const grid& other) const {
    /* Compare the number of rows and return if there's a mismatch. */
    if(rows != other.rows)
        return rows < other.rows;
    /* Next compare the number of columns the same way. */
    if(cols != other.cols)
        return cols < other.cols;
    return lexicographical_compare(begin(), end(), other.begin(), other.end());
}</pre>
```

All that's left to do now is to implement the other five relational operators in terms of <code>operator</code> <. This is done below:

```
template <typename T> bool grid<T>::operator >=(const grid& other) const {
    return !(*this < other);
}
template <typename T> bool grid<T>::operator ==(const grid& other) const {
    return !(*this < other) && !(other < *this);
}
template <typename T> bool grid<T>::operator !=(const grid& other) const {
    return (*this < other) || (other < *this);
}
template <typename T> bool grid<T>::operator > (const grid& other) const {
    return other < *this;
}
template <typename T> bool grid<T>::operator > (const grid& other) const {
    return other < *this;
}
template <typename T> bool grid<T>::operator <=(const grid& other) const {
    return other < *this;
}
</pre>
```

At this point we're done! We now have a complete working implementation of the grid class that supports iteration, element access, and the relational operators. To boot, it's implemented on top of the vector, meaning that it's slick and efficient. This class should be your one-stop solution for applications that require a two-dimensional array.

More to Explore

Operator overloading is an enormous topic in C++ and there's simply not enough space to cover it all in this chapter. If you're interested in some more advanced topics, consider reading into the following:

- Overloaded new and delete: You are allowed to overload the new and delete operators, in case you want to change how memory is allocated for your class. Note that the overloaded new and delete operators simply change how memory is allocated, not what it means to write new MyClass. Overloading new and delete is a complicated task and requires a solid understanding of how C++ memory management works, so be sure to consult a reference for details.
- 2. **Conversion functions**: In an earlier chapter, we covered how to write conversion constructors, functions that convert objects of other types into instances of your new class. However, it's possible to use operator overloading to define an implicit conversion from objects of your class into objects of other types. The syntax is <code>operator Type()</code>, where <code>Type</code> is the data type to convert your object to. Many professional programmers advise against conversion functions, so make sure that they're really the best option before proceeding.

Practice Problems

Operator overloading is quite difficult because your functions must act as though they're the built-in operators. Here are some practice problems to get you used to overloading operators:

- 1. What is an overloaded operator?
- 2. What is an lvalue? An rvalue? Does the + operator yield an lvalue or an rvalue? How about the pointer dereference operator?
- 3. Are overloaded operators inherently more efficient than regular functions?
- 4. Explain how to implement operator + in terms of operator +=.
- 5. What is the signature of an overloaded operator for subtraction? For unary negation?
- 6. How do you differentiate between the prefix and postfix versions of the ++ operator?
- 7. What does the -> operator return?
- 8. What is a friend function? How do you declare one?
- 9. How do you declare an overloaded stream insertion operator?
- 10. What is trichotomy and why is it important to C++ programmers?
- 11. What is transitivity and why is it important to C++ programmers?
- 12. In Python, it is legal to use negative array indices to mean "the element that many positions from the end of the array." For example, myArray[-1] would be the last element of an array, myArray[-2] the penultimate element, etc. Using operator overloading, it's possible to implement this functionality for a custom array class. Do you think it's a good idea to do so? Why or why not? Think about the principle of least astonishment when answering.

- 13. Why is it better to implement + in terms of += instead of += in terms of +? (*Hint: Think about the number of objects created using += and using +.*)
- 14. Consider the following definition of a Span struct:

```
struct Span {
    int start, stop;
};
```

The Span struct allows us to define the range of elements from [start, stop) as a single variable. Given this definition of Span and assuming start and stop are both non-negative, provide another bracket operator for our Vector class that selects a range of elements.

15. Consider the following interface for a class that iterates over a container of ElemTypes:

```
class iterator {
public:
    bool operator== (const iterator& other);
    bool operator!= (const iterator& other);
    iterator operator++ ();
    ElemType* operator* () const;
    ElemType* operator-> () const;
};
```

There are several mistakes in the definition of this iterator. What are they? How would you fix them?

16. The implementation of the grid class's operator== and operator!= functions implemented those operators in terms of the less-than operator. This is somewhat inefficient, since it's more direct to simply check if the two grids are equal or unequal rather than to use the comparison operators. Rewrite the grid's operator== function to directly check whether the grids are identical. Then rewrite operator!= in terms of operator==.