

# A nonlinear model for DTI reconstruction with locally low-rank regularization

YUXIN HU<sup>1</sup>, QIYUAN TIAN<sup>2</sup>, GRANT YANG<sup>1</sup>,  
JENNIFER A MCNAB<sup>3</sup>, BRUCE L. DANIEL<sup>3, 4</sup>, AND  
BRIAN HARGREAVES<sup>1, 3, 4</sup>

*<sup>1</sup>Department of Electrical Engineering, Stanford University, Stanford, CA, United States*

*<sup>2</sup>Athinoula A. Martinos Center for Biomedical Imaging,  
Department of Radiology, Massachusetts General Hospital,  
Harvard Medical School, Boston, MA, United States*

*<sup>3</sup>Department of Radiology, Stanford University, Stanford, CA, United States*

*<sup>4</sup>Department of Bioengineering, Stanford University, Stanford, CA, United States*

# Declaration of Financial Interests or Relationships

Speaker Name: Yuxin Hu

I have the following financial interest or relationship to disclose with regard to the subject matter of this presentation:

Company Name: GE Healthcare

Type of Relationship: Research Support

## Diffusion-weighted imaging

Multi-shot:

- High resolution/reduced distortion

Multi-direction:

- Fiber direction

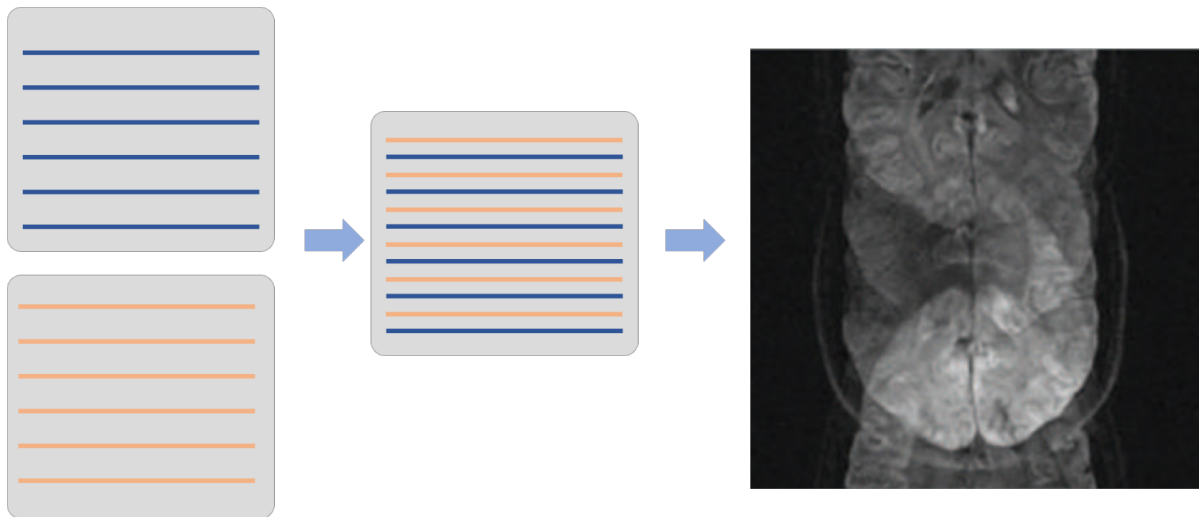
How to use the correlations between both different **shots** and different **directions** to help with reconstruction?

$$\min_{m, \theta} \sum_{d=1}^{ND} \sum_{s=1}^{NS} \frac{1}{2} \left\| E_{d,s} F S (m_d \cdot e^{j\theta_{d,s}}) - y_{d,s} \right\|_2^2 + \lambda_1 \sum_{d=1}^{ND} \|R_d m\|_*$$

## Diffusion-weighted imaging

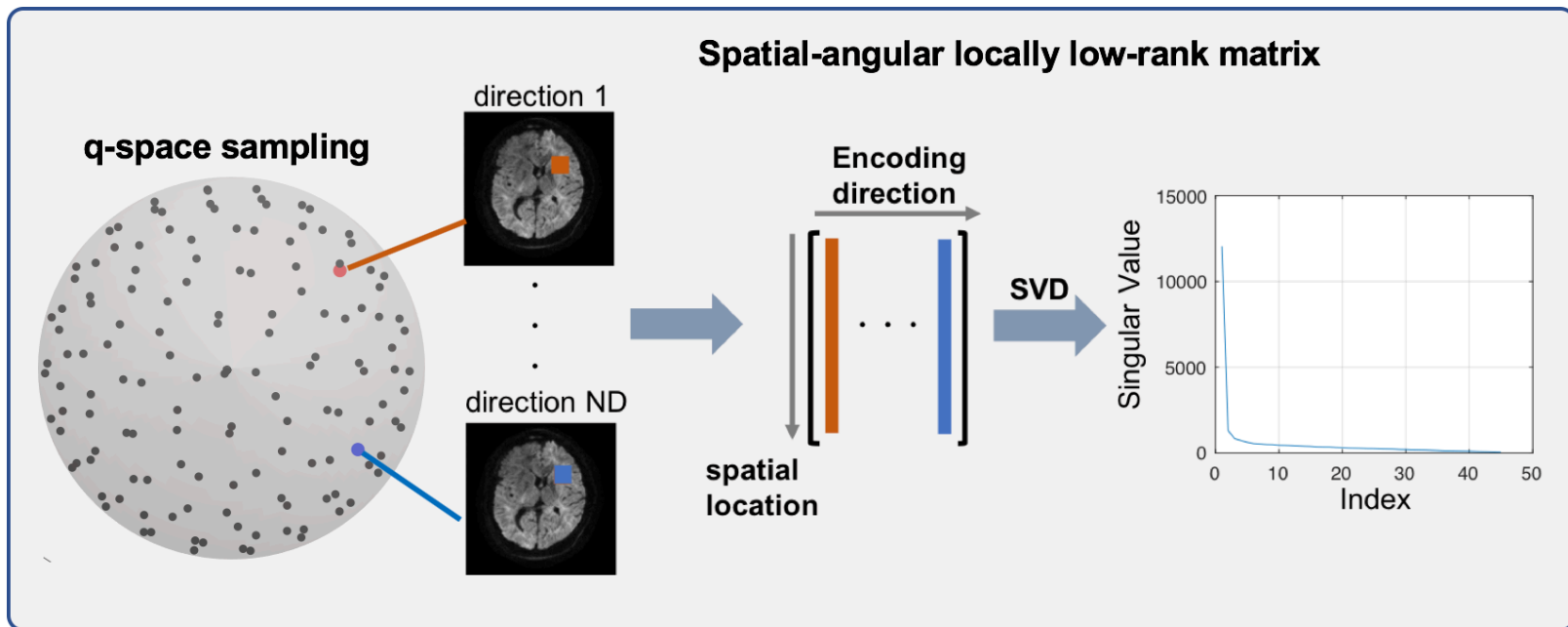
- Motion-induced phase variations:

$$\min_{m, \theta} \sum_{d=1}^{ND} \sum_{s=1}^{NS} \frac{1}{2} \left\| E_{d,s} F S (m_d \cdot e^{j\theta_{d,s}}) - y_{d,s} \right\|_2^2 + \lambda_1 \sum_{s=1}^{NS} \|R_s m\|_*$$



## LLR in multi-direction DWI

- Using locally-low rank to implicitly utilize relationships between different diffusion encoding directions

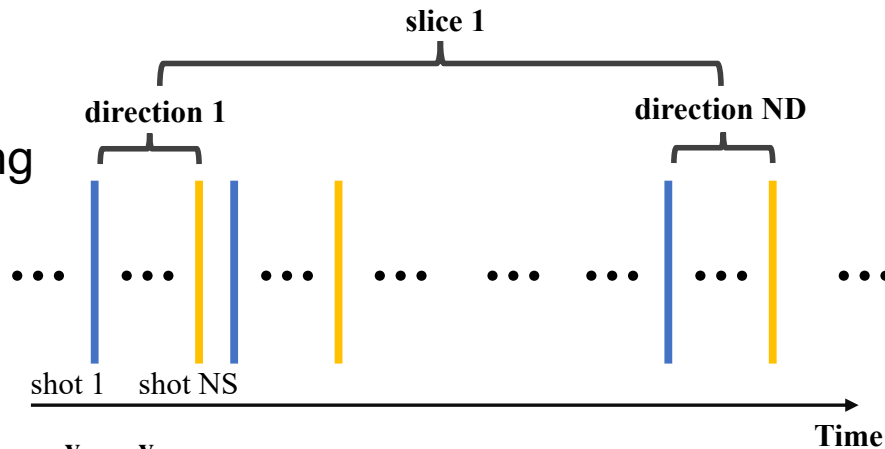


## Non-linear model

- Data consistency term (multi-dir, multi-shot data) + LLR

$$\min_{m, \theta} \sum_{d=1}^{ND} \sum_{s=1}^{NS} \frac{1}{2} \left\| E_{d,s} F S \boxed{m_d \cdot e^{j\theta_{d,s}}} - y_{d,s} \right\|_2^2 + \lambda_1 \sum_{l \in \Omega} \|R_l m\|_*$$

E: sampling pattern  
F: Fourier transform  
S: sensitivity encoding



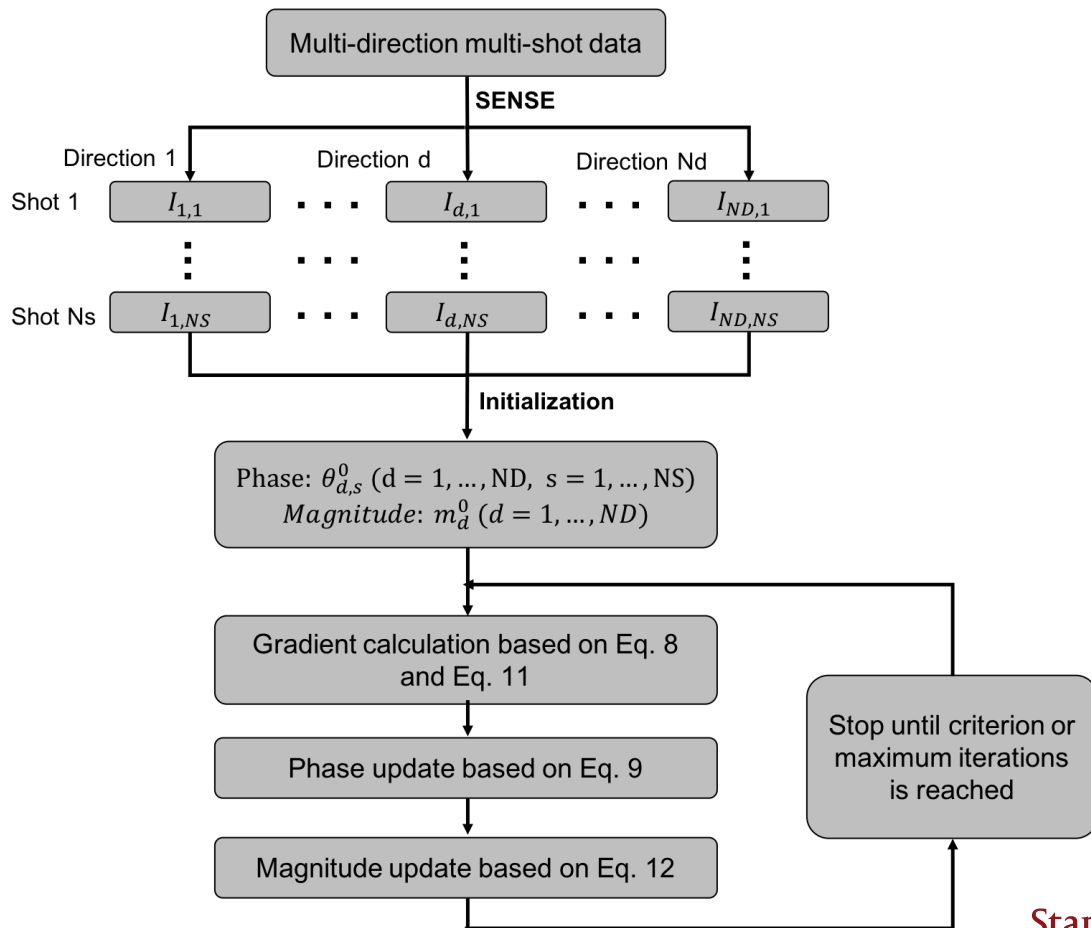
Acquired data

$y_{1,1}$   $y_{1,NS}$

Phase & Mag to be reconstructed

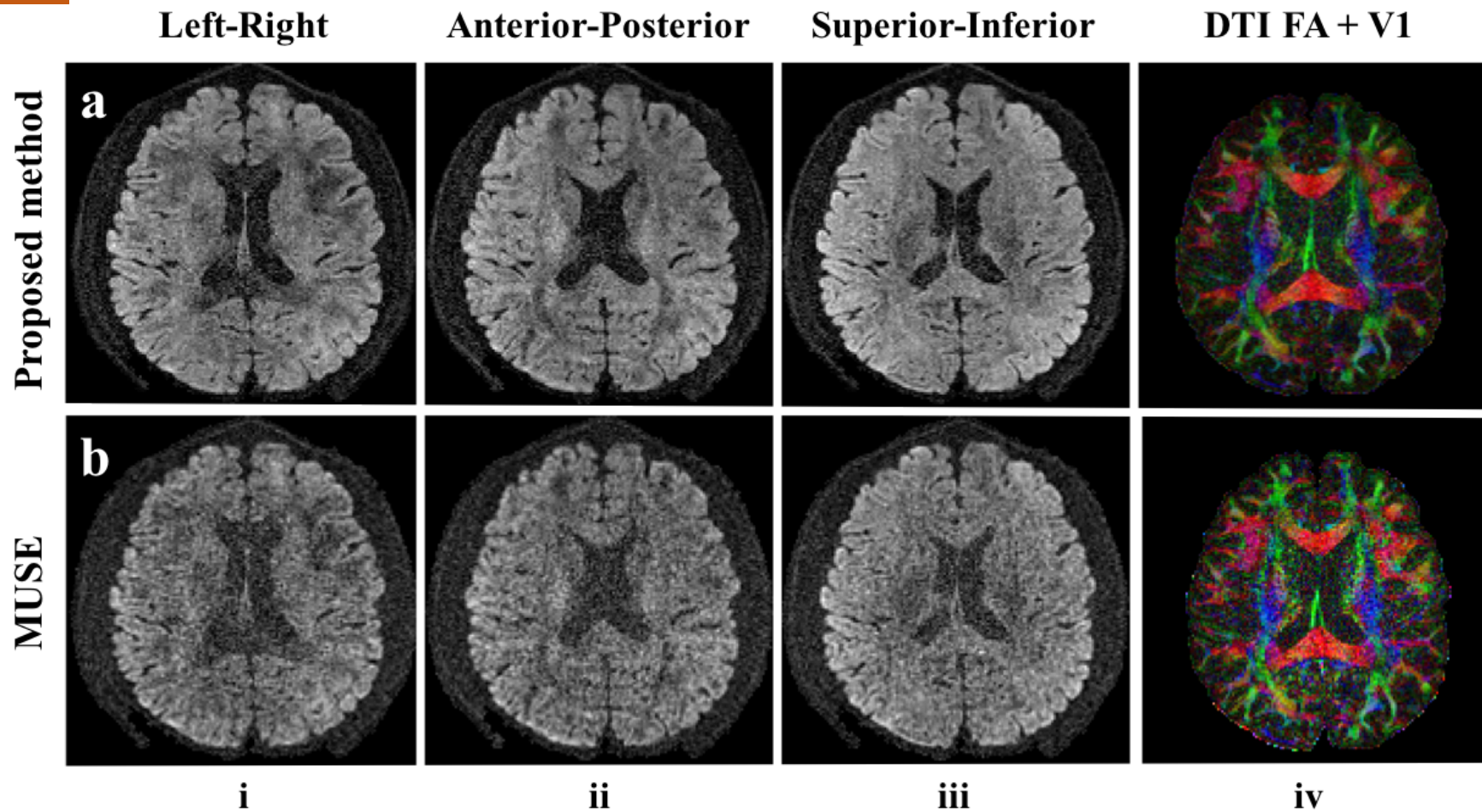
$\theta_{1,1}, \theta_{1,NS}, m_1$

## SENSE initialized joint reconstruction of multi-direction DWI with simultaneous magnitude and phase update

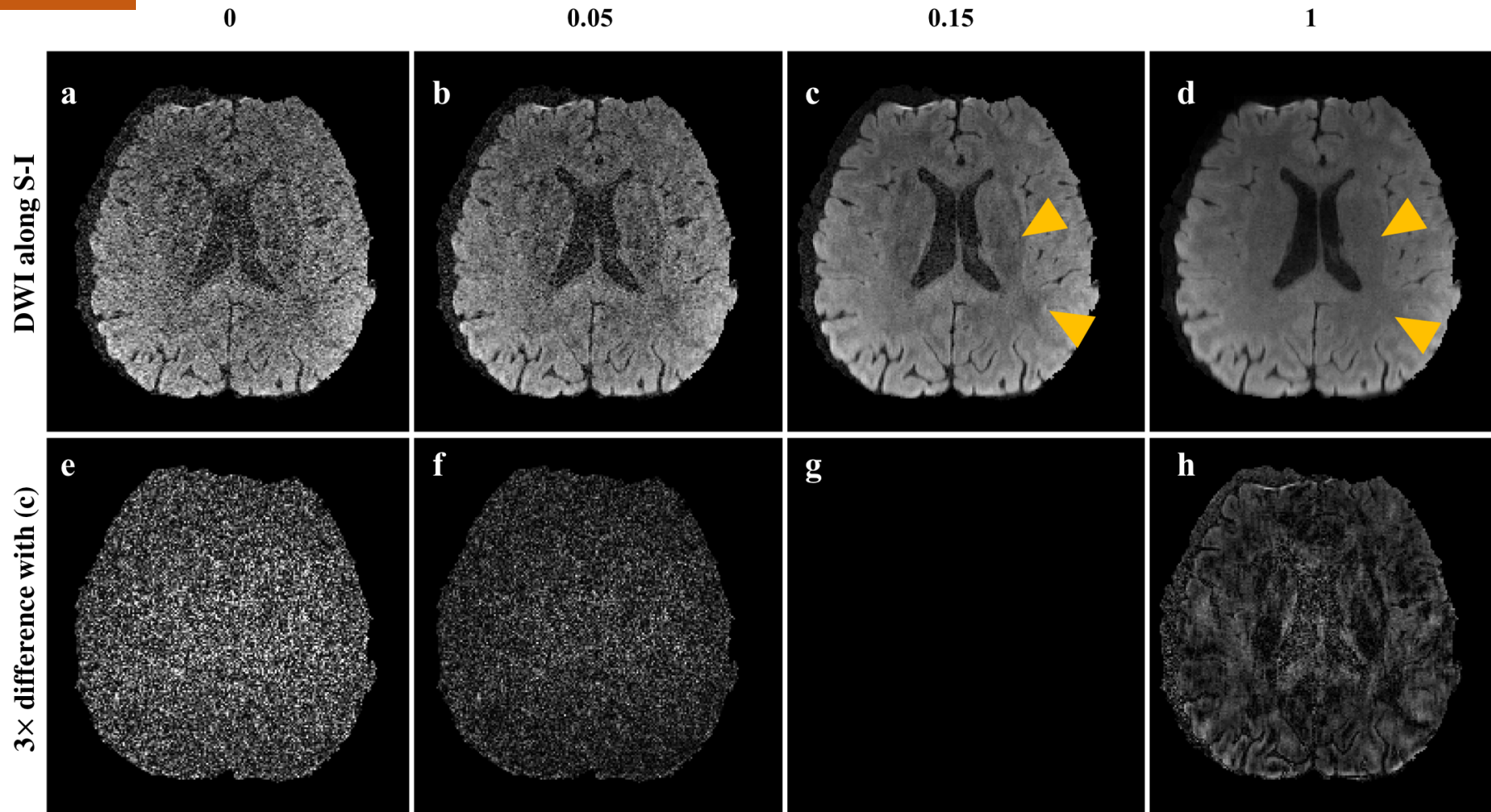


Parameters	Ex0 (to validate the method)	Ex1 (parameter selection)	Ex2 4-shot vs single-shot (R = 3)		Ex3 (different resolutions)	Ex4 (more directions)	Ex5 (high b-value)
TR/TE	2515/59.3	3375/49.7	2278/51.4	2478/63.5	2627/52.8, 2759/54.4, 2993/56.7	2853/53.1	2908/59.2
scan time	05:14	08:09	22:58	24:58	13:21, 14:01, 15:13	28:46	14:47
in-plane resolution/mm	1.2	0.9	1		0.9, 0.8, 0.7	0.9	1
slice thickness/mm	1.2	0.9	1		0.9, 0.8, 0.7	0.9	1
FOV/cm	20	20	18.4		20	20	20
#slices	12	14	10		11	12	10
partial Fourier factor	0.86	0.61	0.67	0.75	0.64, 0.63, 0.61	0.64	0.66
#directions	30	30	150		75	150	75
nex	1	1	1	4	1	1	1
b-value	1000	1000	1000		1000	1000	2000
#subjects	1	1	1		1	2	2





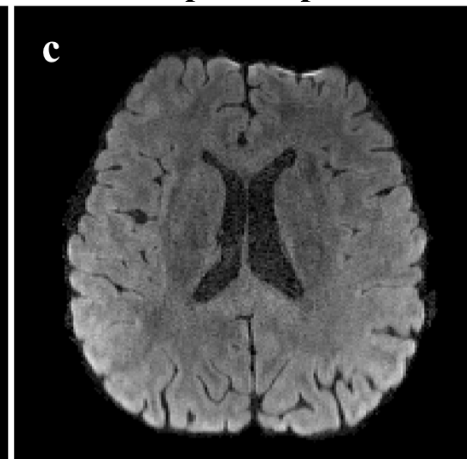
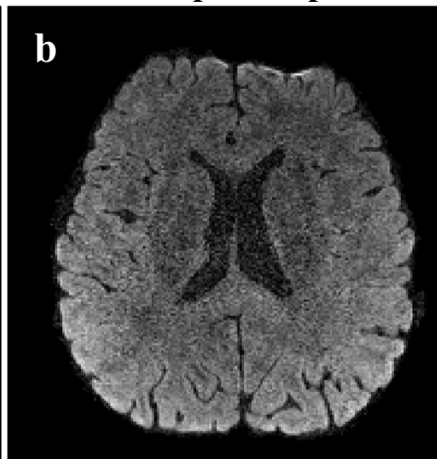
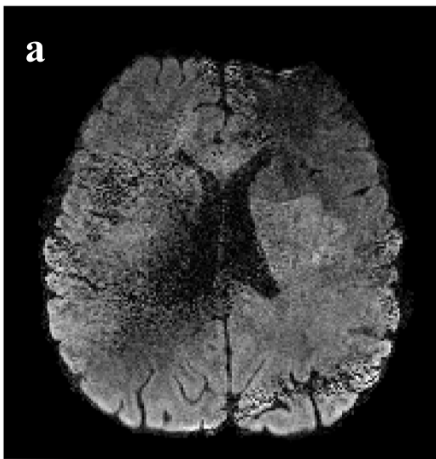
## Reconstructed DWI with different regularization parameters



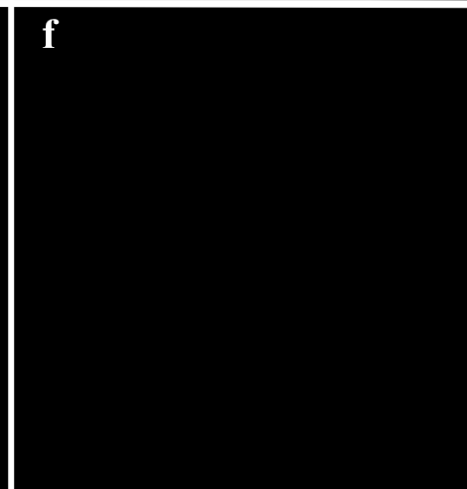
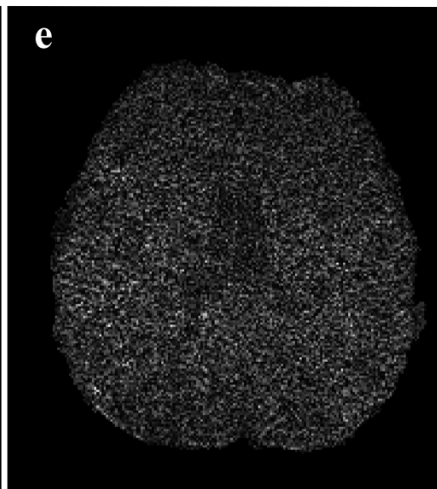
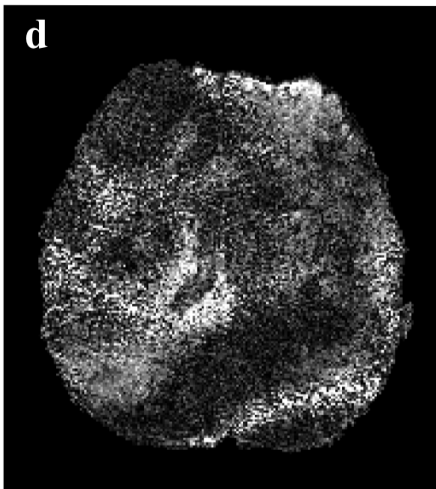
0 initialization

SENSE initialization  
without phase updateSENSE initialization  
with phase update

DWI along S-I

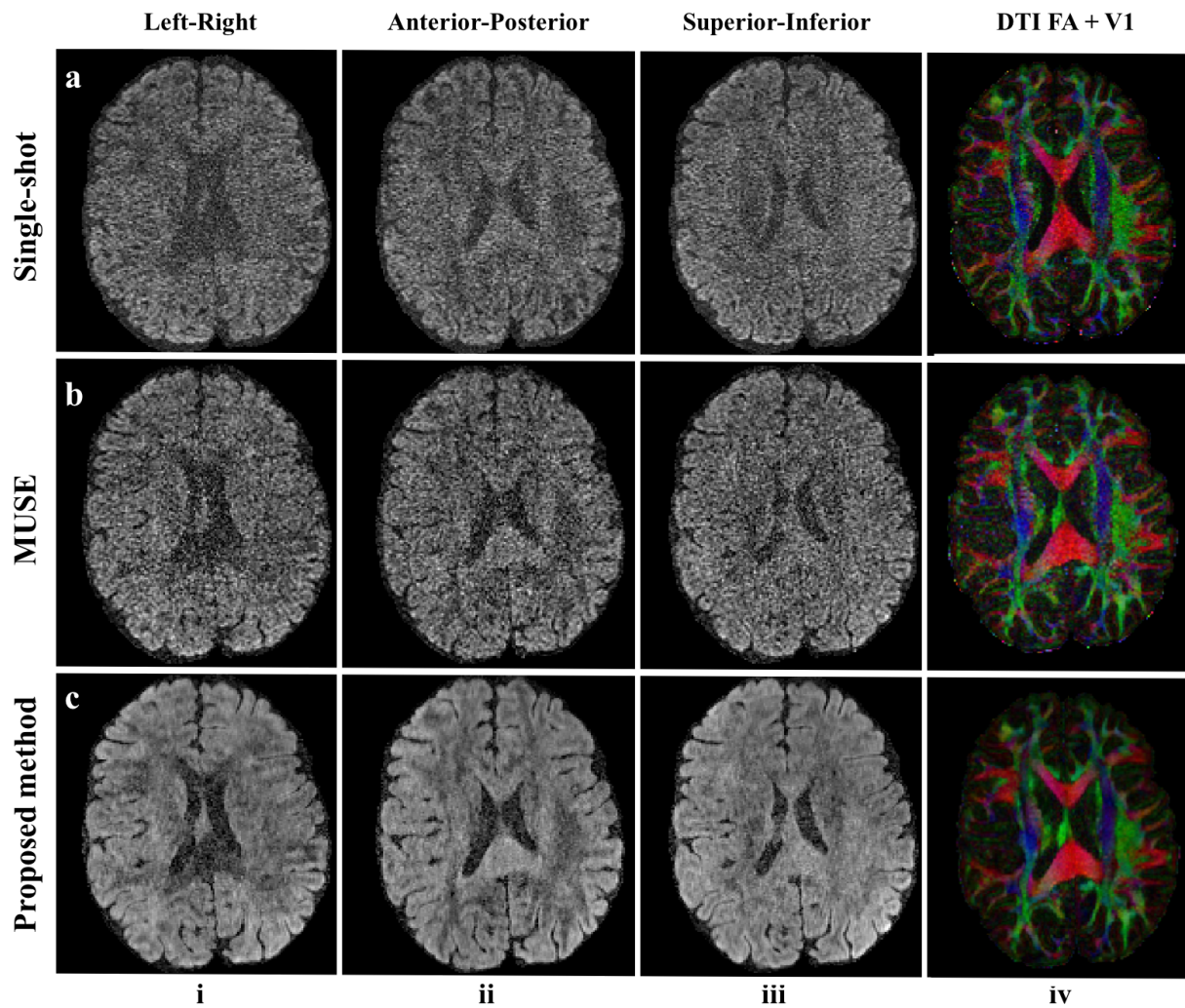


3× difference with (c)

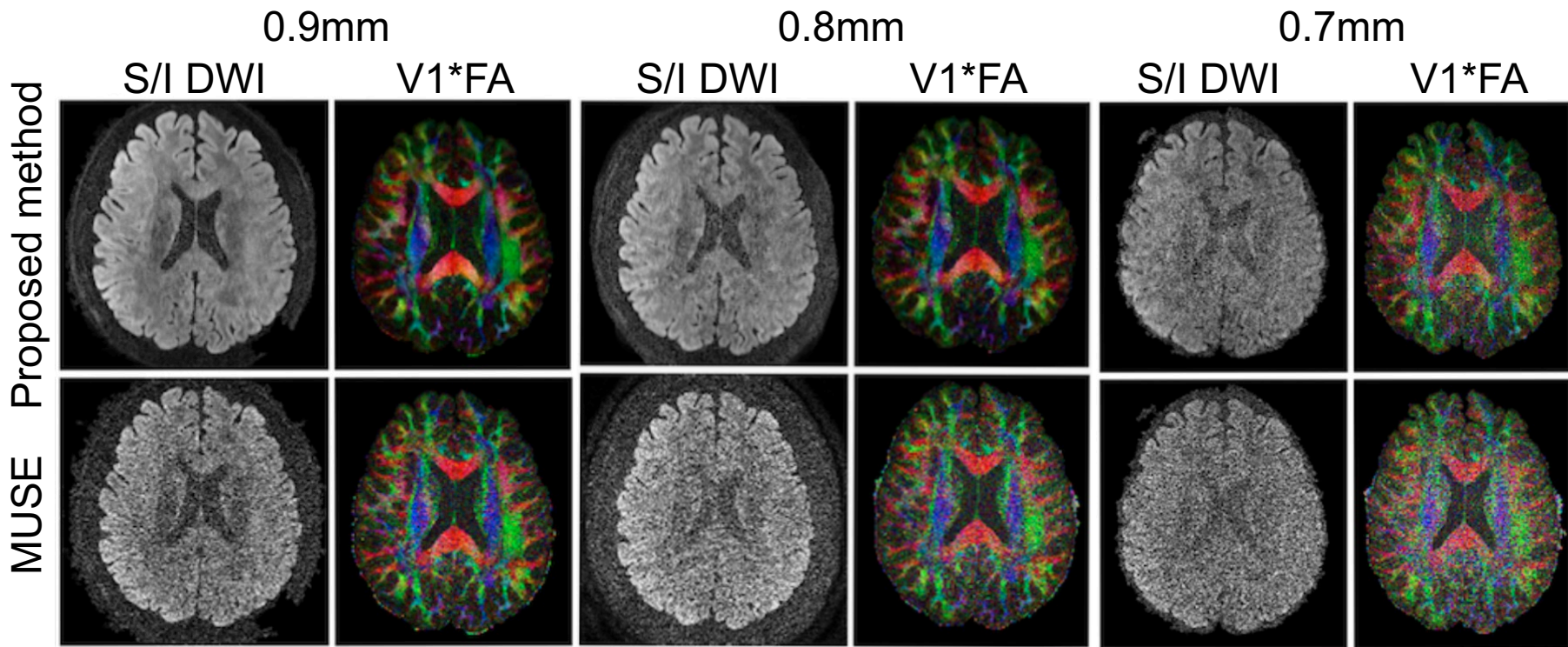


## Reconstruction parameter

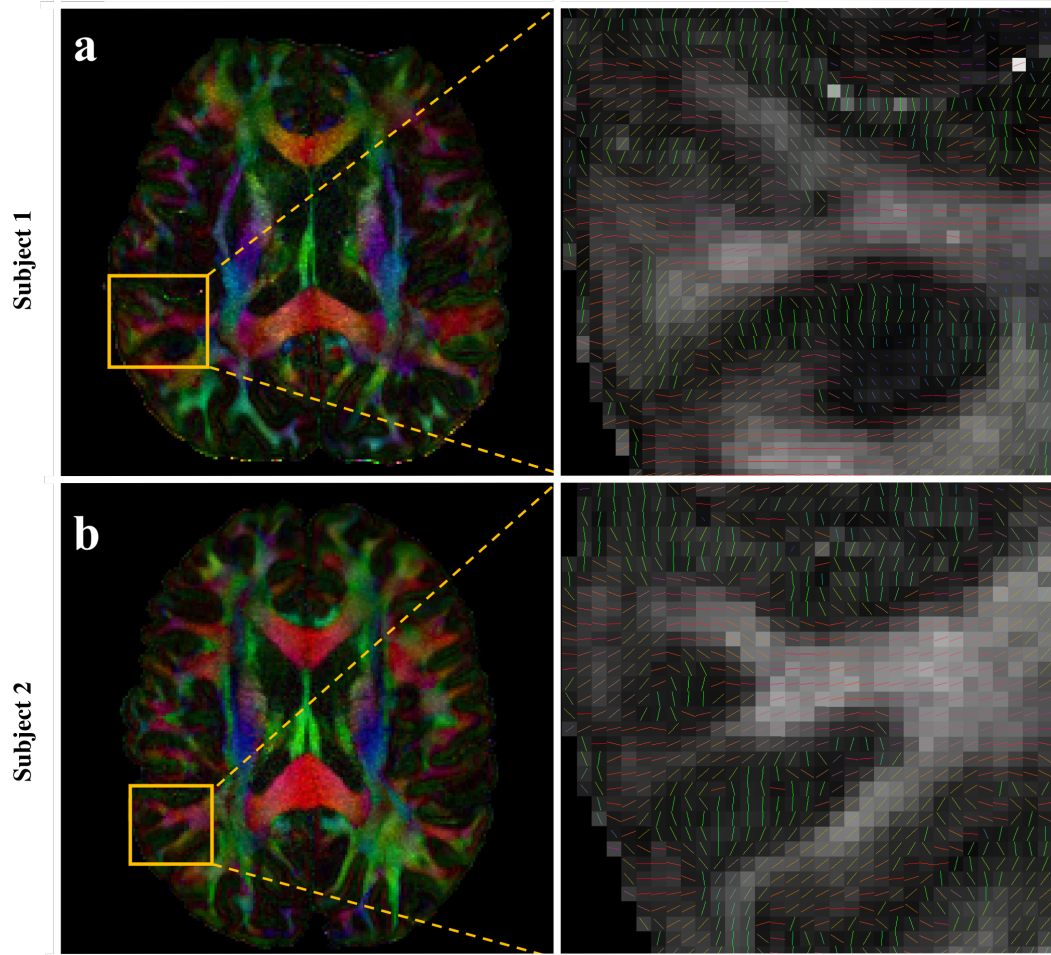
Parameters	Values
#iterations	100
Initialization of phase	hanning window (width = $\frac{1}{2}$ matrix size)
Step size for phase	0.9
Step size for magnitude	0.9
Regularization parameter for LLR	0.12 ~ 0.18
Block size	8
Phase update	Y



## Results: proposed method vs MUSE



- *Ex3: 75 directions,  $b = 1000 \text{ s/mm}^2$ , 13-15min Scan*



- *Ex4: 0.9 isotropic mm, 150 directions,  $b = 1000 \text{ s/mm}^2$ , 28min Scan*

Left-Right

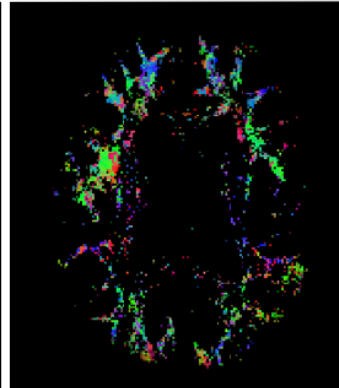
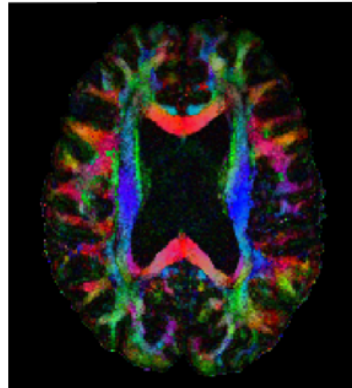
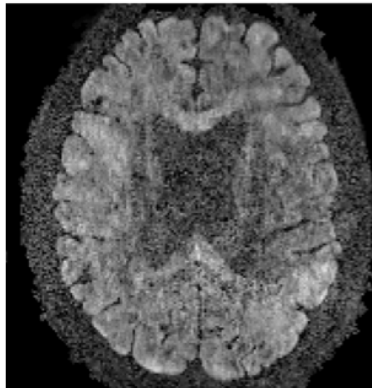
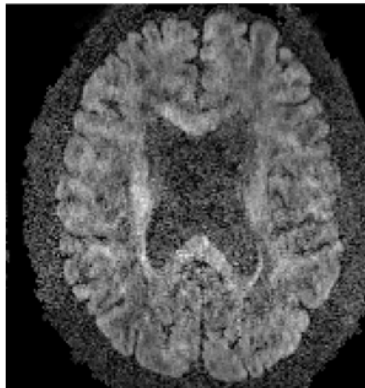
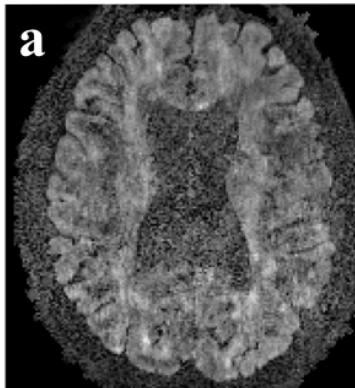
Anterior-Posterior

Superior-Inferior

BEDPOSTX  
f1 + Dyads1BEDPOSTX  
f2 + Dyads2

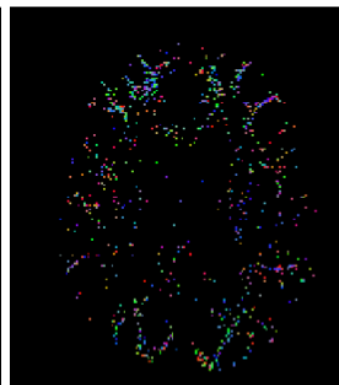
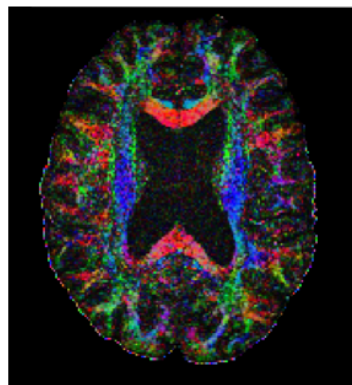
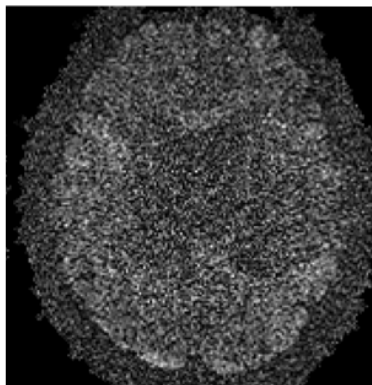
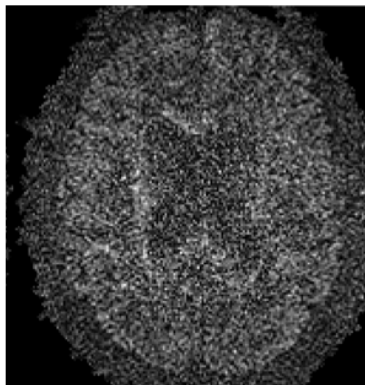
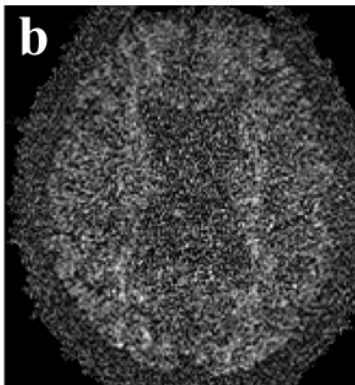
Proposed method

a



MUSE

b



i

ii

iii

iv

v



## Summary

Two contributions for multi-direction multi-shot DWI reconstruction:

- Non-convex model with simultaneous phase and magnitude updates
- LLR to utilize angular correlation