# MS\&E 246: Game Theory with Engineering Applications 

Lecture 1
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## Outline

- Administrative stuff
- Course introduction
- A game


## Administrative details

- My e-mail: ramesh.j ohari@stanford. edu
- Course assistant:

Christina Aperjis, caperjis@stanford.edu

- Website: eeclass. stanford. edu/ msande246 All students must sign up there, and keep up with announcements


## Administrative details

- 6-7 problem sets

Assigned Thursday, due following
Thursday in box outside Terman 319
No late assignments accepted

- Midterm to be held February 8 (in class)


## Big picture

Economics and engineering are tied together more than ever

Game theory provides a set of tools we can use to study problems at this interface

## Motivating examples

- Electronic marketplaces
- eBay auctions:

Fixed termination time

- Amazon auctions

Terminate after 10 minutes of inactivity

Which yields higher revenue?

## Motivating examples

- Internet resource allocation
- TCP: regulates flow of packets through the Internet
- Malicious users can grab much more than "fair" share
- How do we design "fair", "efficient" allocation protocols that are robust to gaming?


## Motivating examples

- Electricity markets
- Electricity can't be stored, and must be reliable
- Market failure is disastrous (e.g., California in 2000)
- How do we design efficient, sustainable markets?


## Internet provider competition

- Internet $=1000$ s of ASes (autonomous systems)
- Bilateral contracts between ASes:

- Transit vs. peer contracts


## ISP contracts

- Transit vs. peer contracts
- Transit:

If A pays B, then
A agrees to carry all traffic to/ from B

- Peer:

A and $B$ are of similar size, and agree to exchange traffic terminating in each other's network

## Problems in the ISP industry

- In 2002, seven dominant players:
- Sprint
- AT\&T
- MCI/ UUnet
- Qwest
- C\&W
- Level3
- Genuity


## Problems in the ISP industry

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(subsidized by wireless)
ACQUIRED (SBC)
ACQUIRED (Verizon)
\$18B debt
R.I.P. (in U.S.)
(merged w/ Genuity)
ACQUIRED (Level3)


## Econ 101, pt. 1: war of attrition

- Pricing below marginal cost
$\Rightarrow$ War of attrition (repeated game):

Lose money now in hopes of being last firm standing

## Econ 101, pt. 2: Bertrand

- Example:

- If $p_{1}<p_{2}$, then ISP 2's profit $=$ zero


## The future

- Econ 101 captures the essence:
- cutthroat pricing
- massive financial losses
- "Iast firm standing" mentality
- Question:

Is a regulated monopoly the only endgame?

## Engineering

What is the problem in Bertrand example?
ISP 2 receives no credit for the value generated.

Current protocols don't expedite transmission of value information.
$\Rightarrow$ How do we build economically robust, informative protocols?

## This course

We will develop the basics of noncooperative game theory...
.. but with an eye towards connection with engineering applications.

## Our first game

Two players each have a budget of $\$ 4.00$.
I have \$8. 00.
Each player $i$ puts $\$ w_{i}$ in an envelope.
I give player $i$ a fraction $w_{i} /\left(w_{1}+w_{2}\right)$ of the $\$ 8.00$ that I have.

Whatever they did not put in the envelope, they keep for themselves.

## Reasoning about the game

- What is the "best" a player can do?
- What is the best they can do together?
- Should they ever bid zero?
- Is there any bid a player should never make?
- What is the minimum a player can guarantee himself or herself?
- What will happen when the game is played?


## Reasoning about the game

Player 1's payoff $=8 \times w_{1} /\left(w_{1}+w_{2}\right)+4-w_{1}$

|  |  | Player 2's bid |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | \$0 | \$1 | \$2 | \$3 | \$4 |
| 믈 | \$0 | \$4.00 | \$4.00 | \$4.00 | \$4.00 | \$4.00 |
| $\stackrel{\sim}{\sim}$ | \$1 | \$11.00 | \$7.00 | \$5.67 | \$5.00 | \$4.60 |
| $\stackrel{\overline{0}}{\square}$ | \$2 | \$10.00 | \$7.33 | \$6.00 | \$5.20 | \$4.67 |
| 진 | \$3 | \$9.00 | \$7.00 | \$5.80 | \$5.00 | \$4.43 |
|  | \$4 | \$8.00 | \$6.40 | \$5.33 | \$4.57 | \$4.00 |

## Reasoning about the game

Note that bidding $\$ 2$ is always better than bidding \$0, \$3, or \$4:

Player 2's bid


## Reasoning about the game

If we anticipate player 2 will not bid $\$ 0$, \$3, or \$4...

Player 2's bid

|  |  | \$p | \$1 | \$2 | \$3 | \$4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| - | +0 | \$4.0 | \$4.00 | .00 | 94.0 | 4 |
| $\stackrel{\sim}{-1}$ | \$1 | \$11.0p | \$7.00 | \$5.67 | \$5.0] | \$4.65 |
| $\stackrel{\bar{\omega}}{ }$ | \$2 | \$10.0 | \$7.33 | \$6.00 | \$5.2 | \$4.67 |
| 줌 | \$2 | +00] | \$7.00 | \$5.00 | \$5.0 |  |
|  | + |  | \$0.40 |  |  |  |

## Reasoning about the game

..then we should always bid $\$ 2 . .$.


## Reasoning about the game

.. and so should player 2.


## Reasoning about the game

- Does this way of reasoning about the game make sense?
- Thought experiments: What if the budgets are different? What if the size of the common pool is different?

