# Improving Subseasonal Forecasting in the Western U.S.

Paulo Orenstein March 22, 2019



Photo credit: IIP Photo Archive

Joint work with Jessica Hwang, Lester Mackey, Judah Cohen, Karl Pfeiffer

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Improving Subseasonal Forecasting

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  - ensembling

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- Encourage you to improve on our results!

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- Can statistical/ML/non-physics models extend the forecast horizon beyond shortterm prediction?

Introduction			

"During the past eight years, every state in the Western United States has experienced drought that has affected the economy both locally and nationally through impacts to agricultural production, water supply, and energy."

David Raff, USBR

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- Can we do better?

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Subseasona	al Climate Forecast Re	odeo		

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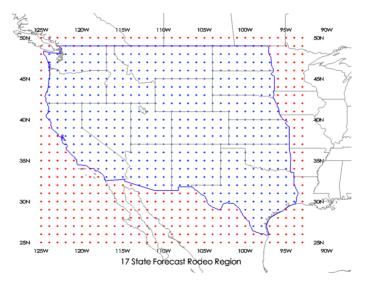
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- ▶ Region: 17 states in western US, G = 514 grid points

Forecast Rodeo	

# Forecast Rodeo region



Forecast Rodeo		Conclusion

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Forecast Rodeo		

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  - observed average temperature or total precipitation:  $\mathbf{y}_t \in \mathbf{R}^G$
  - *climatology* for a month-day combination *d*:

$$\mathbf{c}_{d} = \frac{1}{30} \sum_{\substack{t: \text{monthday}(t) = d, \\ 1981 \le \text{year}(t) \le 2010}} \mathbf{y}_{t}$$

the long-term average over 1981-2010 for the month-day d

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Highest average skill over the contest period = winner

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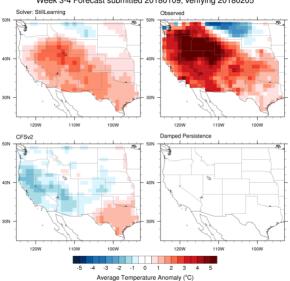
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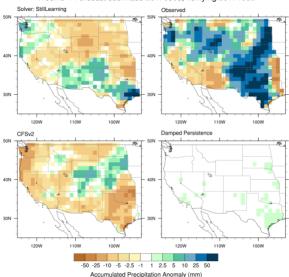
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Benchmarks: debiased CFSv2 and "damped persistence"



Week 3-4 Forecast submitted 20180109, verifying 20180205



Week 3-4 Forecast submitted 20170905, verifying 20171002

Forecast Rodeo		Conclusion

Our dataset

#### ► No data provided!

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	Dataset		
Data matrix			

lat 47 47 47 48 :	lon 260 261 262 236	date 1979-02-09 1979-02-09 1979-02-09 1979-02-09	rhum_shift30 86.539415 89.957313 92.553695 93.731037 :	pres_shift30 96061.320731 96419.183454 97493.990932 97277.973493	· · · · · · · · · · ·	target -18.464830 -18.329887 -18.289105 2.575200 :	
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 $J_{10^{6} \times 30}$ 

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  - MultiLLR (local linear regression with multitask model selection): uses lagged predictors based on all weather variables, chosen using multitask model selection tailored to the cosine similarity objective
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- Ensemble of the two models performs better than either model individually

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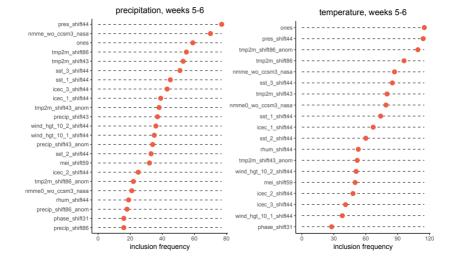
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- Backward stepwise has to be customized
  - At each step, remove variable that decreases predictive performance the least
  - Predictive performance is the *leave-one-year-out cross-validated cosine similarity* on the target date's day of year, averaged across all historical years
  - To properly leave one year out around t, need to hold out from 4 weeks before t to 48 weeks after t

	Models	

### Inclusion frequencies of candidate variables



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AutoKNN: Multitask *k*-nearest-neighbor autoregression

▶ For each target date t, find the 20 most similar historical dates by looking at cosine similarity between anomaly trajectory in the 60 days leading up to t and leading up to each historical date

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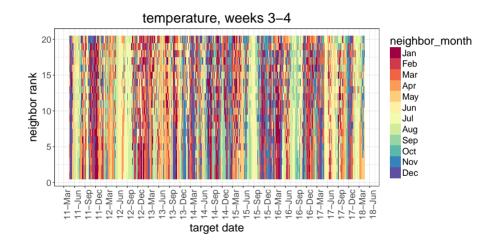
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- Perform weighted local linear regression using knn1 through knn20 and fixed lagged measurements of temperature or precipitation to predict future anomaly

Introduction	Forecast Rodeo	Dataset	Models	Results	Conclusion
Learned near	est neighbors				
	Precipitation		Tempe	rature	
	and constants a server in target Jul Server Aug So	and the second s		torum minutes	

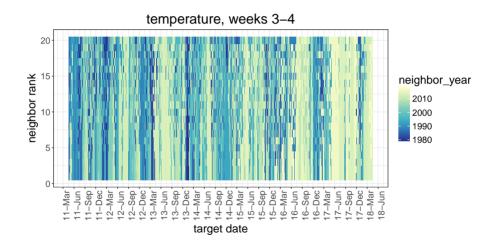
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## Learned nearest neighbors



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# Ensemble of the two models

• We ensemble by averaging the  $\ell_2$ -normalized forecasted anomalies:

$$\hat{\boldsymbol{a}}_{\mathrm{ensemble}} = \frac{1}{2} \frac{\hat{\boldsymbol{a}}_{\mathrm{LLR}}}{\|\hat{\boldsymbol{a}}_{\mathrm{LLR}}\|_2} + \frac{1}{2} \frac{\hat{\boldsymbol{a}}_{\mathrm{KNN}}}{\|\hat{\boldsymbol{a}}_{\mathrm{KNN}}\|_2}$$

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#### Proposition

Consider an observed anomaly vector **a** and *m* distinct forecast anomaly vectors  $(\hat{\mathbf{a}}_i)_{i=1}^m$ . For any vector of weights  $\mathbf{p} \in \mathbb{R}^m$  with  $\sum_{i=1}^m p_i = 1$  and  $p_i \ge 0$ , let

$$ar{\mathbf{a}}_{(\mathbf{p})} = \sum_{i=1}^m p_i rac{\hat{\mathbf{a}}_i}{\|\hat{\mathbf{a}}_i\|}$$

be the weighted average of the  $\ell_2$ -normalized forecast anomalies. Then,

$$\left|\sum_{i=1}^{m} p_i \cos(\hat{\mathbf{a}}_i, \mathbf{a})\right| \leq |\cos(\bar{\mathbf{a}}_{(p)}, \mathbf{a})|.$$

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- In the contest period (2017-2018), our models beat both of the contest baselines (and the top competitor) by a lot
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- Ensembling the two models helps significantly

Dataset

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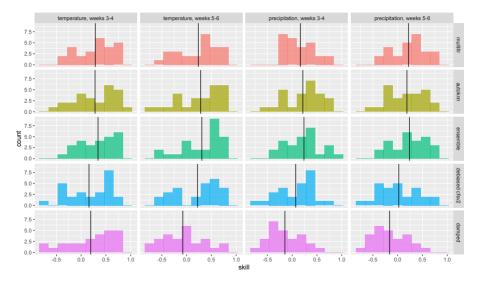
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# Contest period, 2017-2018

task	LLR	KNN	ensemble	cfsv2	damped	top competitor
temp, weeks 3-4	0.2856	0.2807	0.3414	0.1589	0.1952	0.2855
temp, weeks 5-6	0.2371	0.2817	0.3077	0.2192	-0.0762	0.2357
precip, weeks 3-4	0.1675	0.2156	0.2388	0.0713	-0.1463	0.2144
precip, weeks 5-6	0.2219	0.1870	0.2412	0.0227	-0.1613	0.2162

		Results	Conclusion

# Contest period, 2017-2018



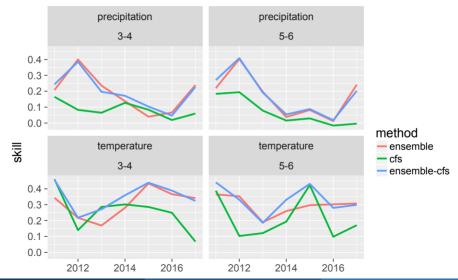
Results

# Historical evaluation period, 2011-2017

task	LLR	KNN	ensemble	cfsv2	ens-cfsv2
temp, weeks 3-4	0.2230	0.3111	0.3073	0.2557	0.3508
	0.2204		0.2962	0.2142	0.3279
precip, weeks 3-4	0.1573	0.1513	0.1893	0.0860	0.1964
precip, weeks 5-6			0.1703	0.0691	0.1755

		Results	

# Historical evaluation period, 2011-2017



Paulo Orenstein

			Conclusion
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- ► Ensembling statistical and physics-based forecasts produce further improvements

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  - More sophisticated modeling approaches can almost certainly do even better. Try your own!