### Modeling Human Reading with Neural Attention

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EMNLP 2016

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- $\blacktriangleright$   $\approx$  40% of words are **skipped**

# **Computational Models I**

- 1. models of saccade generation in cognitive psychology
  - EZ-Reader [Reichle et al., 1998, 2003, 2009]
  - SWIFT [Engbert et al., 2002, 2005]
  - Bayesian inference [Bicknell and Levy, 2010]
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These models...

- involve theoretical assumptions about human eye-movements, or
- require selection of relevant eye-movement features, and
- estimate parameters from eye-tracking corpora

# Computational Models II: Surprisal

$$\operatorname{Surprisal}(w_i | \boldsymbol{w}_{1...i-1}) = -\log P(w_i | \boldsymbol{w}_{1...i-1})$$
(1)

- measures predictability of word in context
- computed by language model

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- measures predictability of word in context
- computed by language model
- correlates with word-by-word reading times [Hale, 2001, McDonald and Shillcock, 2003a,b, Levy, 2008, Demberg and Keller, 2008, Frank and Bod, 2011, Smith and Levy, 2013]
- but cannot explain...
  - reverse saccades
  - re-fixations
  - spillover
  - skipping
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# **Tradeoff Hypthesis**

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Build unsupervised models jointly accounting for **reading times** and **skipping** 

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#### Hypothesis

Human reading optimizes a tradeoff between

- Precision of language understanding: Encode the input so that it can be reconstructed accurately
- Economy of attention:
  Fixate as few words as possible

# **Tradeoff Hypothesis**

#### Approach: NEAT (NEural Attention Tradeoff)

- 1. develop generic architecture integrating
  - neural language modeling
  - attention mechanism
- 2. train end-to-end to optimize tradeoff between precision and economy
- 3. evaluate on human eyetracking corpus

# Architecture I: Recurrent Autoencoder



## Architecture II: Real-Time Predictions



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- Humans constantly make predictions about the upcoming input
- Reader outpus probability distribution P<sub>R</sub> over the lexicon at each time step
- Describes which words are likely to come next

# Architecture III: Skipping



Attention module shows word to R or skips it

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- Attention module shows word to R or skips it
- ► A computes a probability + draws a sample  $\omega \in \{\text{READ}, \text{SKIP}\}$
- R receives special 'SKIPPED' vector when skipping

# Implementing the Tradeoff Hypothesis

#### **Training Objective**

Solve prediction and reconstruction with minimal attention:

$$\arg_{\theta} \min \{ \mathsf{E}_{\boldsymbol{w}, \boldsymbol{\omega}} [L(\boldsymbol{\omega} | \boldsymbol{w}, \theta) + \alpha \cdot \|\boldsymbol{\omega}\|_{\ell_1}] \}$$
  
Loss on Prediction + Reconstruction # of fixated words

# Implementing the Tradeoff Hypothesis

#### **Training Objective**

Solve prediction and reconstruction with minimal attention:



- **w** is word sequence drawn from corpus
- ω sampled from attention module A
- α > 0: encourages NEAT to attend to as few words as possible

# Implementation and Training

#### Implementation

- one-layer LSTM network with 1,000 memory cells
- attention network: one-layer feedforward network
- optimized by SGD + REINFORCE policy gradient method [Williams, 1992]
- trained on corpus of newstext [Hermann et al., 2015]
  - 195,462 articles from Daily Mail
  - $\blacktriangleright$  pprox 200 million tokens
- Input data split into sequences of 50 tokens

### NEAT as a Model of Reading

- Attention module models fixations and skips
- NEAT surprisal models reading times of fixated words



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The only ingredients are

- architecture
- objective
- unlabeled corpus

No eye-tracking data, lexicon, grammar, ... needed.

## **Evaluation Setup**

- English section of the Dundee corpus [Kennedy and Pynte, 2005]
  - > 20 texts from The Independent
  - annotated with eye-movement data from ten English native speakers who were asked to answer questions after each text.
- split into development (1–3) and test set (4–20)
- Size: 78,300 tokens (dev); 281,911 tokens (test)
- exclude from the evaluation words at the beginning or end of lines, outliers, cases of track loss, out-of-vocabulary words
- Fixation rate: 62.1% (dev), 61.3% (test)

# Intrinsic Evaluation: Prediction and Reconstruction

	Pe	Eix Bata	
	Prediction	Reconstruction	FIX. Hale
NEAT	180	4.5	60.4%
$\omega$ $\sim$ Bin(0.62)	333	56	62.1%
Word Length	230	40	62.1%
Word Freq.	219	39	62.1%
Full Surprisal	211	34	62.1%
Human	218	39	61.3%
$\omega \equiv 1$	107	1.6	100%

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$$\mathsf{FirstPassDuration} = \beta_0 + \sum_{i \in \mathsf{Predictors}} \beta_i x_i + \sum_{j \in \mathsf{RandomEffects}} \gamma_j y_j + \varepsilon$$

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(Intercept)	247.4	7.1	34.7*	
Word Length	12.9	0.2	60.6*	
Previous Word Freq.	-5.3	0.3	-18.3*	
Prev. Word Fixated	-24.7	0.8	-30.6*	Destruction
Obj. Landing Pos.	-8.1	0.2	-41.3*	Baseline
Word Pos. in Sent.	-0.1	0.03	-3.0*	Predictors
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► NEAT surprisal captures more than word length, frequency, ...

even though it only has access to 60.4% of the words

# **Evaluating Reading Times: Deviance**

- Assume we have models M<sub>1</sub>, M<sub>2</sub> for the same data
- ▶ They assign likelihoods  $P_1 = P(\text{Data}|M_1), P_2 = P(\text{Data}|M_2)$
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Here:

 $M_1$ : Model containing only baseline predictors  $M_2$ : Model including surprisal

Full surprisal	$\omega \equiv 1$	980
NEAT surprisal	$\boldsymbol{\omega}\equiv P_{\mathcal{A}}(\boldsymbol{w})$	867
Random surprisal	$\mathbf{\omega} \equiv \textit{Binom}(0.604)$	832

# **Evaluating Fixations I: Heatmaps**

HUMAN



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	Acc	$F1_{\mathrm{fix}}$	F1 <sub>skip</sub>
NEAT	63.7	70.4	53.0
Lower and Upp	er Bou	nds	
Random Baseline	52.6	62.1	37.9
Intersubject Agreement	69.5	76.6	53.6
Feature-Based	d Mode	els	
Nilsson and Nivre [2009]	69.5	75.2	62.6
Matthies and Søgaard [2013]	69.9	72.3	66.1
Word Frequency	67.9	74.0	58.3
Word Length	68.4	77.1	49.0

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- supervised models at upper limit
- bulk of data explained by word length/frequency predictors

### Fixations of Successive Words

 Humans more likely to fixate a word when the previous word was skipped

$$P(\omega_i = \mathsf{READ} | \omega_{i-1} = \mathsf{READ}) < P(\omega_i = \mathsf{READ})$$

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Ratio:

Setting	$\frac{P(\omega_i = READ   \omega_{i-1} = READ)}{P(\omega_i = READ)}$
NEAT	0.81
Human	0.85
Word Frequency	0.91
Random	1.0

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Mixed models show effect beyond word frequency

# Fixation Rates by POS Categories



# Conclusion

- unsupervised model of reading predicting reading times and skipping
- ► based on tradeoff between precision of understanding ⇔ economy of attention
- trained end-to-end without linguistic knowledge, eyetracking data, or feature extraction
- Experiments on the Dundee corpus
  - provides accurate predictions for human skipping behavior
  - predicts reading times, while only accessing 60.4% of the words
  - known qualitative properties of skipping emerge, without specifying relevant features in advance

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# **Correlations with Known Predictors**

	Human	NEAT
Restricted Surprisal	0.465	0.762
Full Surprisal	0.512	0.720
Log Word Freq.	-0.608	-0.760
Word Length	0.663	0.521