



An Information-Theoretic Explanation of Adjective Ordering Preferences

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Background

Adjectives are subject to ordering preferences:

“the big blue plate” > “the blue big plate”

“the beautiful old house” > “the old beautiful house”

“the delicious boiling curry” > “the boiling delicious curry”

Generalizations include ‘Specificity’, ‘Inherentness’, ‘Concept-Formability’, ‘Subjectivity’

Scontras et al. (2017): The more **subjective** an adjective, the **farther** away from the noun it occurs

Can this be explained in terms of **general principles** of **language use** and **processing**?

Corpus Analysis: Subjectivity and MI

Previous hypotheses ‘specificity’, ‘inherentness’. We formalize using **Pointwise Mutual Information**:

$$PMI(Adj, Noun) = \log P(Adj|Noun) - \log P(Adj)$$

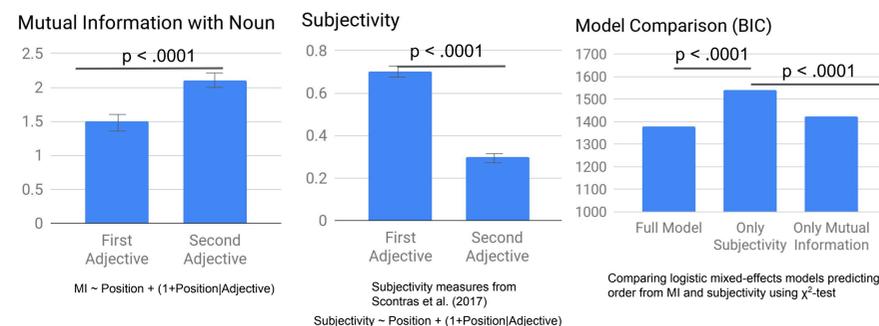
This is a common measure of **collocation** and a plausible quantitative measure of **specificity**.

Prediction: Adjectives with **higher** mutual information with the noun come **closer** to the noun.

We test this on BookCorpus and Gigaword.

Results: Prediction is confirmed

Subjectivity and Mutual Information **independently** impact ordering.



The Use of Adjectives

Goal: Provide a model of adjective use that **explains** effects of **subjectivity** and mutual **information**.

Adjectives can:

1. **pick out** a referent (**Restrictive**)
2. **describe** and **comment on** a referent (**Non-Restrictive**)

We focus on **non-restrictive** use.

RSA Model of Adjective Use

In a typical **world state**:

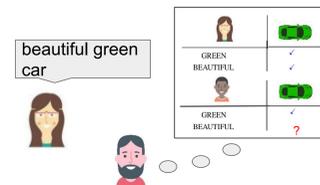
METAL	✓	✓	✓	METAL	✓	✓	✓
GREEN	✓	✓	✓	GREEN	✓	✓	✓
LARGE	✓	✓	✓	LARGE	✓	✓	✓
BEAUTIFUL	✓	✓	✓	BEAUTIFUL	✓	✓	✓

- Speakers mostly **agree** on **objective** judgments (METAL, GREEN)
- More **disagreement** for more **subjective** judgments (LARGE, BEAUTIFUL)

Formally, adjectives have different **inter-speaker correlations** under **prior distribution** over **possible worlds**.

Speaker utters sequence **Adjective₁-Adjective₂-Noun**

Listener performs **Bayesian Inference** about judgments of speaker and other people.



$$P_{\text{listener}}(w|u) \propto P_{\text{prior}}(w|u) \delta_{\text{utterance } u \text{ is true of the speaker in the world } w}$$

Speaker chooses utterance by trading off **informativity** and **cost** of utterance:

$$P_{\text{speaker}}(u) \propto \exp(\alpha \cdot (U(u) - \beta \cdot C(u)))$$

Informativity of utterance ‘u’:

$$U(u) := -\text{KL}(P_{\text{speaker}} || P_{\text{listener}}(\cdot|u))$$

$$= \sum_w P_{\text{speaker}}(w) \log \frac{P_{\text{listener}}(w|u)}{P_{\text{speaker}}(w)}$$

Cost of producing ‘u’:

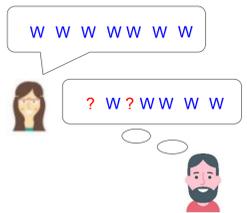
$$C(A_1 A_2 N) = -\log P(A_1 A_2 N)$$

Memory Loss Breaks Symmetry

Formal model by Futrell and Levy, 2017:

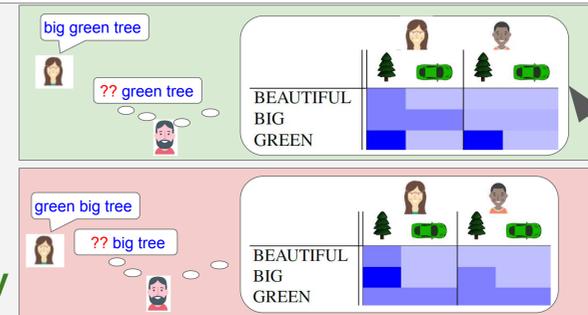
Assumption 1: Previous words in the input may be **lost from memory** stochastically

Assumption 2: Probability of loss **increases** as one goes **further back**.



Consequence: First adjective **less likely** to be **integrated with noun** by the listener.

Placing **subjective** adjective **first** has **higher informativity**



Listener learns more about third person → higher informativity

Placing **high-MI** adjective **second** has **lower cost**

$$C(A_1, A_2, N) - C(A_2, A_1, N) = \lambda \cdot (PMI(A_1, N) - PMI(A_2, N))$$

Cost Difference between Orderings = Loss Rate · Difference in Mutual Information

Testing against Corpus Data

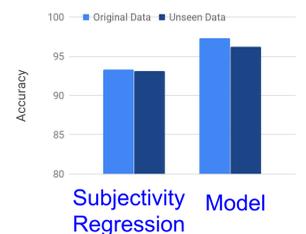
Predict adjective order in corpus data

Model Parameters:

- Inter-speaker correlation = 1 - subjectivity
- Other parameters inferred using Bayesian Data Analysis

Evaluation Datasets

1. Set from corpus analysis (~ 4,700 examples)
2. Unseen data set (10,000 examples)



Conclusion

- **Subjectivity** and **MI** impact adjective ordering.
- Both effects can be explained by integrating **Bayesian reasoning** with **memory limitations**.
- Adjective ordering can be explained by general principles of **human communication** and **language processing**.

References: Scontras, G., Degen, J., & Goodman, N. D. (2017). Subjectivity Predicts Adjective Ordering Preferences. *Open Mind*, 1(1), 53–66. Sproat, R., & Shih, C. (1991). The cross-linguistic distribution of adjective ordering restrictions. In C. Georgopoulos & R. Ishihara (Eds.), *Interdisciplinary approaches to language*. (pp. 565–593). Dordrecht, Netherlands: Kluwer Academic. Futrell, Richard, and Roger Levy (2017). Noisy-context surprisal as a human sentence processing cost model. *Proceedings of EAACL*.