Political Science 452: Text as Data

Justin Grimmer

Assistant Professor Department of Political Science Stanford University

April 27th, 2011

Where We've Been, Where We're Going

- Class 1: Finding Text Data
- Class 2: Representing Texts Quantitatively
- Class 3: Dictionary Methods for Classification
- Class 4: Comparing Language Across Groups
- Class 5: Texts in Space
- Class 6: Clustering
- Class 7: Topic models
- Class 8: Supervised methods for classification
- Class 9: Ensemble methods for classification
- Class 10: Scaling Speech

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I'm curious if you have ever used mechanical turk for coding of data (e.g., from text). Any experience with that? Thoughts?

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How is Homework Going? Class? What Can I do to help you?

More About R Code

```
How to write to a file in R
Many method, easiest: sink
> sink('Test.txt')
> print('This is a great tool')
> sink()
```

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Today's Lecture: How to identify those words?

Method 1: Mutual Information

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Bigger mutual information \Rightarrow better discrimination

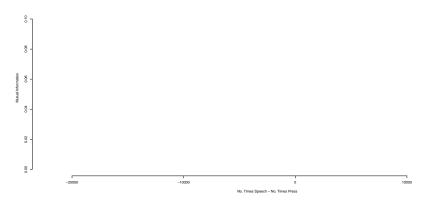
Formula for mutual information (based on ML estimates of probabilities)

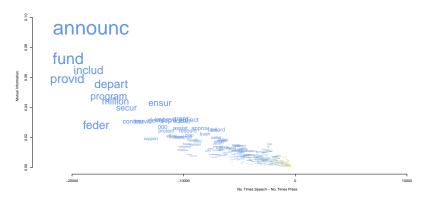
```
n_p = Number Press Releases
  n_s = Number of Speeches
  D = n_p + n_s
  n_j = \sum w_{i,j} (No. docs w_j appears )
 n_{-i} = No. docs w_i does not appear
 n_{i,p} = No. press and w_i
 n_{i,s} = No. speech and w_i
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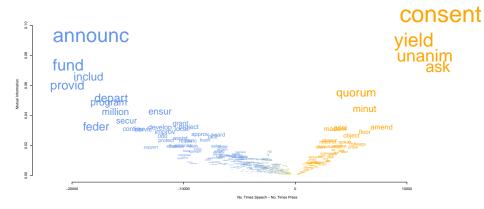
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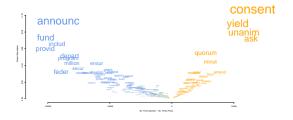
$$MI(w_{j}) = \frac{n_{j,p}}{D} \log_{2} \frac{n_{j,p}D}{n_{j}n_{p}} + \frac{n_{j,s}}{D} \log_{2} \frac{n_{j,s}D}{n_{j}n_{s}} + \frac{n_{-j,p}}{D} \log_{2} \frac{n_{-j,p}D}{n_{-j}n_{p}} + \frac{n_{-j,s}D}{D} \log_{2} \frac{n_{-j,s}D}{n_{-j}n_{s}}.$$

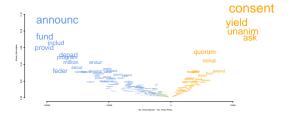
(Page 258, 259 of this document http://stanford.edu/~jgrimmer/RepStyle.pdf for more information)





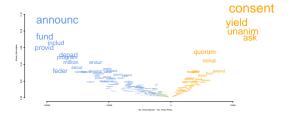




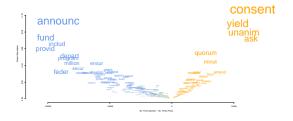


What's Different?

- Press Releases: Credit Claiming



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- Floor Speeches: Procedural Words

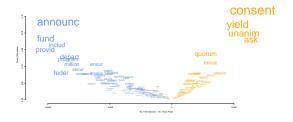


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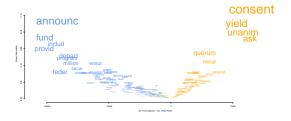
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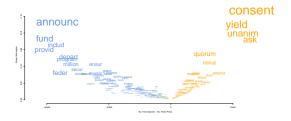
- Validate: Manual Classification



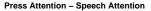
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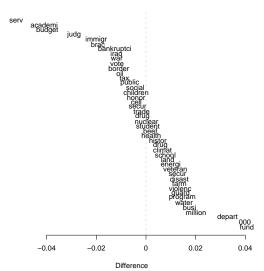


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- Feature selection: one method to mitigate over fitting

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Be skeptical!

Running Example

How Do Democrat and Republican Arguments About the Iraq War Differ?

- Assume: Identified set of documents (press releases) about Iraq War
- Speaker labels: know who (Democrat, Republican) issued press release
- Inferential Goal: framing-considerations Democrats and Republicans use when discussing war

Present simple methods, show similarity.

The example already has stop words and some names removed.

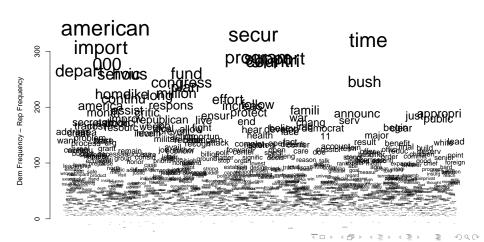
```
(Following steps are from Fightin' Words )
Difference in word frequency:
For each word j compute
```

 n_{jD} = No. times used in Dem Documents

 n_{jR} = No. times used in Rep Documents

Difference = $n_{jD} - n_{jR}$

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Differences in Word Proportions:

For each word j compute

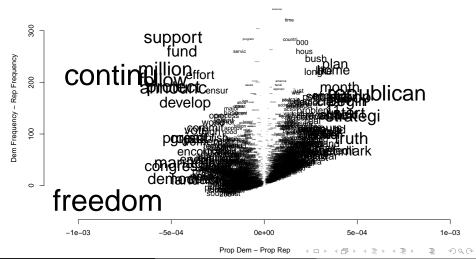
$$p_{jD} = \frac{n_{jD}}{n_D}$$

$$= \text{Proportion of Dem words that are } j$$
 $p_{jR} = \frac{n_{jR}}{n_R}$

$$= \text{Proportion of Rep words that are } j$$

Difference =
$$p_{jD} - p_{jR}$$

Difference = $p_{jD} - p_{jR}$



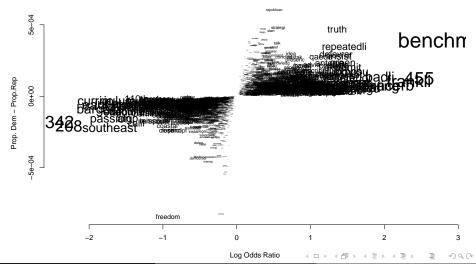
Log Odds Ratio:

For each word j compute:

$$\begin{array}{ccc} \mathsf{Odds}_{jD} & = & \frac{p_{jD}}{1-p_{jD}} \\ \mathsf{Odds}_{jR} & = & \frac{p_{jR}}{1-p_{jR}} \\ \mathsf{Odds} \; \mathsf{Ratio}_{j} & = & \frac{\mathsf{Odds}_{jD}}{\mathsf{Odds}_{jR}} \end{array}$$

 $\log \text{Odds Ratio}_j = \log \text{Odds}_{jD} - \log \text{Odds}_{jR}$

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Problem: What to Do With Dem (GOP) Only Words? If Only Dems Use Words:

$$p_{jR} = \frac{0}{n_R}$$

$$Odds_{jR} = \frac{0}{1}$$

$$\log Odds_{jR} = \log 0 - \log 1$$

What should we do?

Solution: "add" a little, but in a principled way

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Prior

$$\mathbf{p}_R \sim \mathsf{Dirichlet}(\alpha)$$

 $\mathbf{p}_D \sim \mathsf{Dirichlet}(\alpha)$

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 $\mathbf{p}_D \sim \operatorname{Dirichlet}(\alpha)$
 $\alpha = (\alpha_1, \alpha_2, \dots, \alpha_N)$

Solution: "add" a little, but in a principled way We need a model!: Intro to Bayes in 10 minutes Notation:

$$\mathbf{p}_{R} = (p_{1R}, p_{2R}, \dots, p_{NR})$$
 $\mathbf{p}_{D} = (p_{1D}, p_{2D}, \dots, p_{ND})$
 $\mathbf{y}_{D} \sim \text{Multinomial}(n_{D}, \mathbf{p}_{D})$

Prior

$$\mathbf{p}_R \sim \mathsf{Dirichlet}(\alpha)$$
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Before showing why this "adds" a little.

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Before showing why this "adds" a little. Let me teach you how to Dirichlet

Dirichlet Distribution

Distribution over proportions.

$$\pi \sim \operatorname{Dirichlet}(\alpha)$$

$$p(\pi|\alpha) = \frac{\Gamma(\sum_{j} \alpha_{j}}{\prod_{j} \Gamma \alpha_{j}} \prod_{j=1}^{N} \pi_{j}^{\alpha_{j}-1}$$

Facts:

$$E[\pi_j] = \frac{\alpha_j}{\sum_{k=1}^N \alpha_k}$$

$$Variance[\pi_j] = \frac{E[\pi_j](1 - E[\pi_j])}{\sum_{k=1}^N (\alpha_k) + 1}$$

Conjugate to Multinomial: easily apply to the model

Methods for Identifying Separating Words

$$\mathbf{p}_D | \alpha \sim \mathsf{Dirichlet}(\alpha)$$
 $\mathbf{y}_D | \mathbf{p}_D \sim \mathsf{Multinomial}(n_D, \mathbf{p}_D)$

Conjugacy implies

$$\begin{aligned} \mathbf{p}_{D}|\mathbf{y}_{D}, \boldsymbol{\alpha} &\sim & \mathsf{Dirichlet}(\boldsymbol{\alpha}') \\ \alpha_{j}^{'} &= & y_{jD} + \alpha_{j} \\ E[p_{j,D}] &= & \frac{y_{jD} + \alpha_{j}^{'}}{n_{D} + \sum_{k=1}^{N} \alpha_{k}^{'}} \end{aligned}$$

Smoothing (borrowing information): easy to understand in Bayesian framework, take Simon's class

Methods for Identifying Separating Words

Now, we can compute all log-odds.

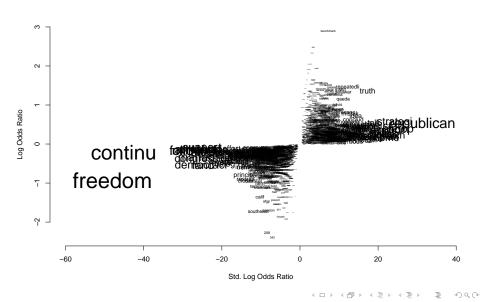
But same problem: rare words dominate Solution: include estimate of variance

$$\text{Var}(\log \text{Odds Ratio}_j) \approx \frac{1}{y_{jD} + \alpha_j} + \frac{1}{y_{jR} + \alpha_j}$$

$$\text{Std. Log Odds}_j = \frac{\log \text{Odds Ratio}_j}{\sqrt{\text{Var}(\log \text{Odds Ratio}_j)}}$$

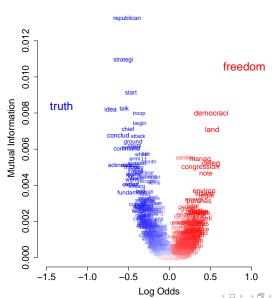
Analogues from Contingency Tables Key Idea:

Systematic or Random Difference



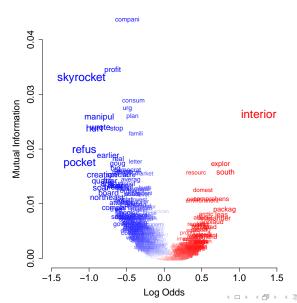
Mutual Information, Standardized Log Odds

Iraq War, Partisan Words



Mutual Information, Standardized Log Odds

Gas Prices, Partisan Words



Text as Data

There are many other similar methods

- Difference in standardized proportions
- χ^2 statistics
- Pointwise Mutual Information
- ..

Characteristics:

- Definition of separation
- Word by word test of separation
- Providing rank ordering of words
- Best Method: depends on context, intuition provided

Moving Forward

- Considered word by word methods solely
- During supervised classification, we will consider joint separability
 - Conditional on other words, how much more information does this word provide

Next Week:

- Geometry of texts
- Foundation for clustering
- topic modeling
- supervised classification