# An Optimization and Monte Carlo Planning Approach for High Penetrations of Intermittent Renewables

Elaine K. Hart and Mark Z. Jacobson INFORMS Annual Meeting, Austin, TX November 8, 2010



Atmosphere/Energy Program

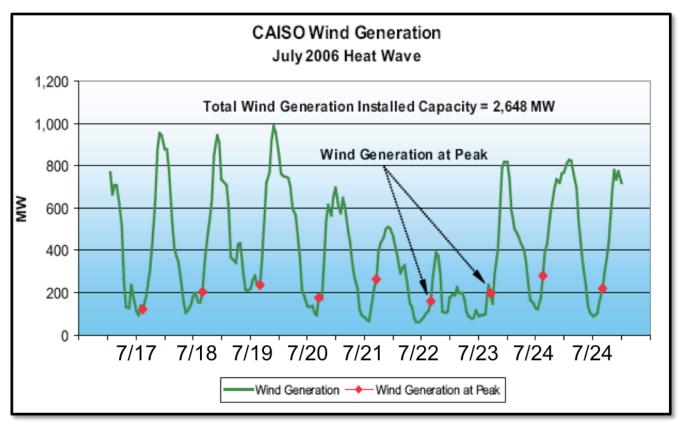
Dept. of Civil and Environmental Engineering

Stanford University



# The Challenge





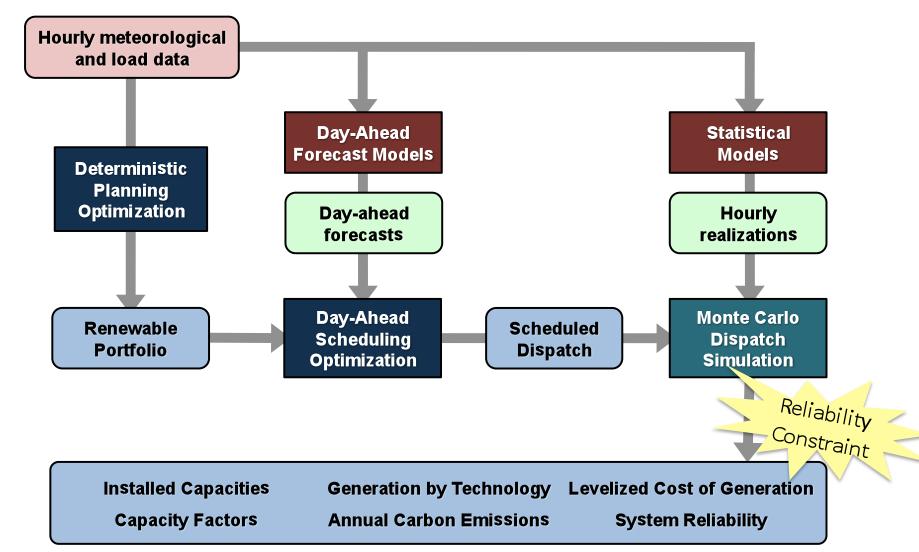
CAISO, 2007: "Integration of Renewable Resources," California ISO, November 2007.

How can the grid accommodate the intermittency of wind and solar to **significantly** reduce carbon emissions?

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# **Low Carbon Portfolio Planning Model**





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## **Problem Formulations**



#### Objective Functions

- Cost (including annualized capital, fixed and variable O&M, fuel, and cost of carbon (in 2050 scenario)
- Approximate Emissions linear function of natural gas generation and spinning capacity

#### Linear Constraints

- System-wide power balance
- Generator governing equations (affine w.r.t. capacity, fuel)
- Thermal plant ramp rates
- Energy (integrated power) constraints

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# **Generator Technology Models**



#### **Intermittent Generators**

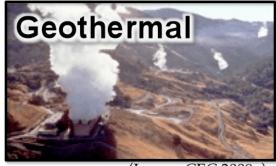


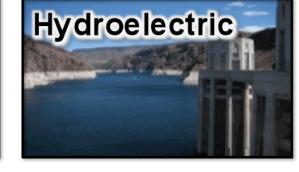




(Image: NREL 2008)

#### **Conventional Generators**







(Image: CEC 2009a)

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# **Generator Technology Models**



#### Intermittent Generators

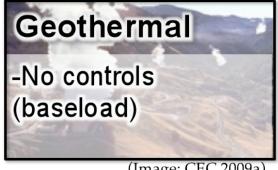
# **Wind Power** -Curtailment



**Photovoltaics** -No controls

(Image: NREL 2008)

#### **Conventional Generators**







# **Natural Gas** -Load balancing -Dispatchable

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# **Realization Models**



- System Load, Irradiance (GHI => DNI, DHI), Wind Speed
- Linear statistical models of the form:

$$f(t) = A(t)\vec{x} + \vec{b}$$
 where  $A(t) = \begin{bmatrix} a_1(t) & a_2(t) & \dots \end{bmatrix}$  is comprised of functions like: 
$$a_i(t) = \hat{f}(t) \qquad \qquad \text{(a forecast)}$$
 
$$a_i(t) = \hat{f}(t-1) - f(t-1) \qquad \qquad \text{(prior forecast error)}$$
 
$$a_i(t) = \gamma(t) \qquad \qquad \text{(diurnal or seasonal bias)}$$
 
$$a_i(t) = 1 \qquad \qquad \text{(constant bias)}$$

Use linear regression to find  $\vec{x}$  and characterize b distribution

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## **Realization Production**



$$f(t) = A(t)\vec{x} + \tilde{b}$$
 and  $\tilde{b} \sim \mathcal{N} \big( 0, \sigma_{model} \big)$  is a random variable

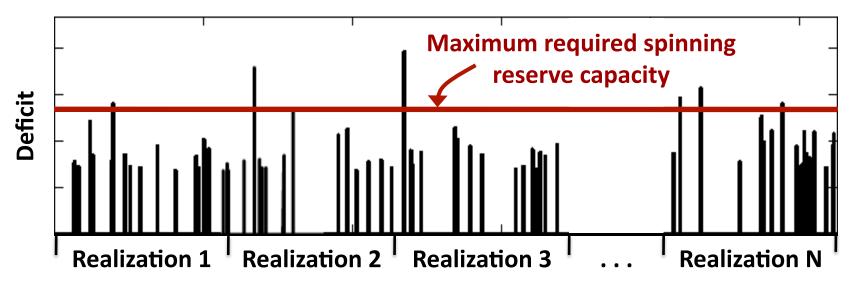
#### To create each realization, at each time step:

- -Apply linear model
- -Sample the model error distribution
  - -Impose site-site correlations where appropriate
- -Apply additional models where necessary

# **Ensuring System Reliability**



- Dispatch optimization includes expensive deficit in case of extreme forecast error.
- Deficit signal is used with LOLE to determine necessary spinning reserve capacity and schedule



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## **Case Studies**



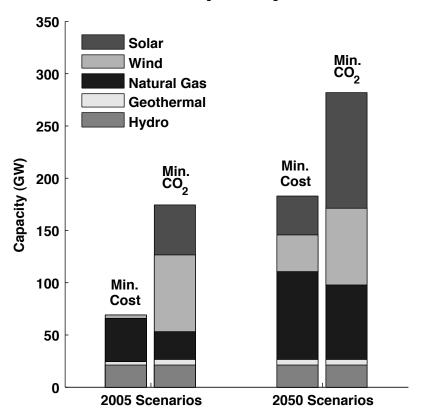
- Load scenarios:
  - 2005-2006 load data, 2050-2051 load projection
- Renewable Portfolios produced by minimizing:
  - Cost, Emissions
- Data:
  - Wind: Western Wind Integration Datasets (NREL, 3TIER)
  - Irradiance: NSRDB (NREL)
  - Load: California ISO OASIS Database
- Solve using CVX (Grant and Boyd, 2010)
   [17,520 time steps with 20 realizations each]

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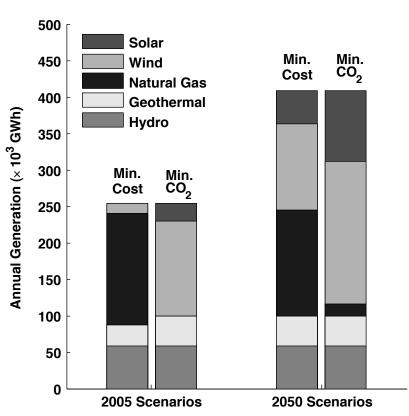
# **Solved Generator Portfolios**



#### **Capacity**



#### Generation



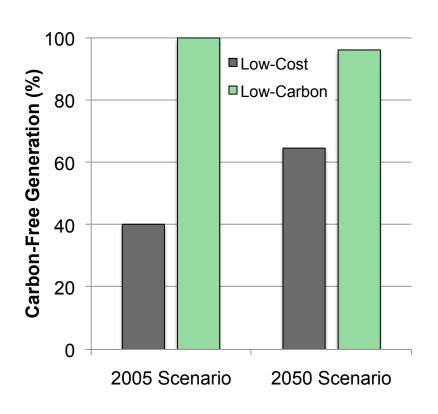
Hart and Jacobson, 2011. [In Review]

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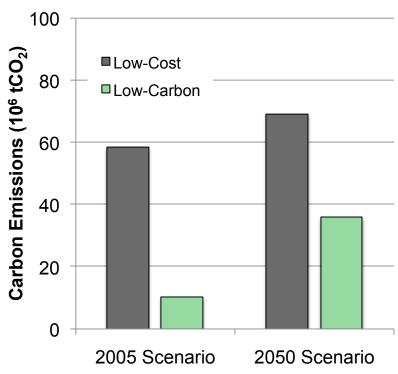
# **Carbon Emissions Characteristics**



#### **Carbon-Free Generation**



#### **Carbon Emissions**

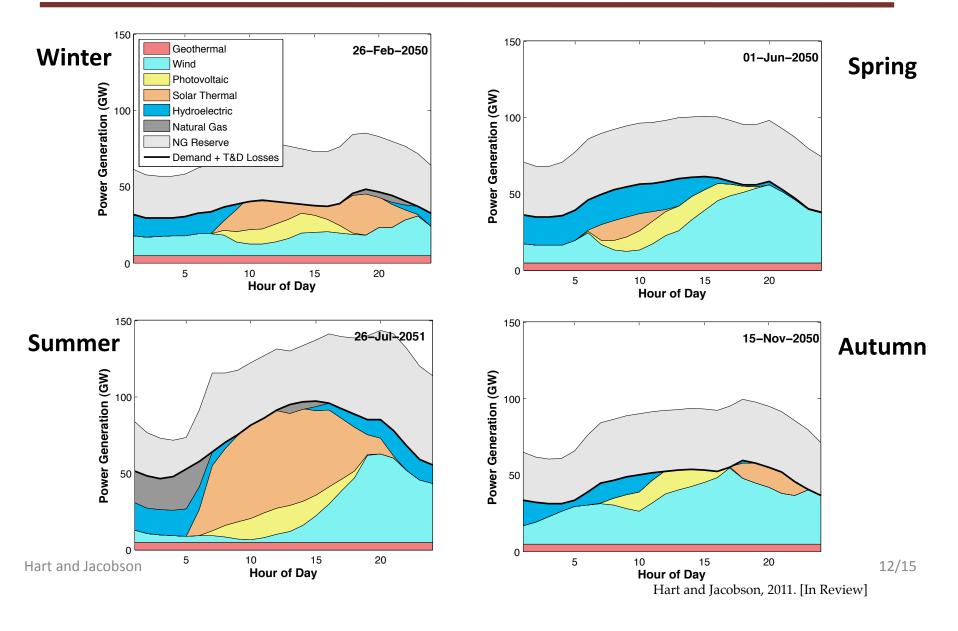


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# Example Realizations (2050 Low-CO<sub>2</sub>)



# Stochastic vs. Deterministic



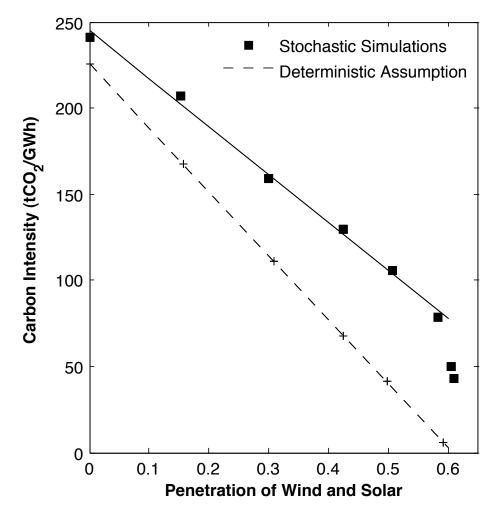
Portfolios produced by scaling 2005 low-carbon capacities uniformly

#### **Stochastic simulations:**

Monte Carlo simulation with forecast error

#### **Deterministic assumption:**

Simulate single realization where forecast = actual data



# **Conclusions**



- We can provide >99% of generation from noncarbon based generators while meeting an LOLE requirement of I day in I0 years
- With conservative assumptions regarding thermal plant operation, can still achieve significant reductions in carbon emissions from base case levels
- Stochastic analyses are needed in system planning
- Low capacity factors will require enhanced capacity markets for thermal plants

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# **Next Steps**



- Include hour-ahead forecasts
- Improve forecast error characterization
  - Include phase errors
- Improve flexibility of hydroelectric generators
- Build participating load and storage models
  - EV's, Batteries, Fuel Cells, CAES

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# **Questions?**



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# For more information (and a copy of this presentation): www.stanford.edu/~ehart/

