

# AA103 Homework 8

Cantwell Spring 2020-21

Due May 25, 2021

## Suggested Reading

AA283 Course reader Chapters 2 and 3.

### Problem 1

It is late August and a female Bar-tailed Godwit with a mass of  $0.6\text{kg}$  takes off from the west coast of Alaska beginning her fall migration south. Estimate her mass when she arrives eight days later after a nonstop flight of  $11,680\text{km}$  to the Piako river on the North Island of New Zealand. Assume the overall efficiency is  $\eta_{\text{overall}} = 0.45$  and the change in weight is mainly loss of fat. You will need to do some internet research to supply whatever additional information you need to make the estimate.

### Problem 2

A ramjet operates at a free-stream Mach number,  $M_0 = 3$ . The area ratio across the engine is  $A_1/A_8 = 1.75$ . Supersonic flow is established at the entrance of the inlet and a normal shock is stabilized in the diverg-

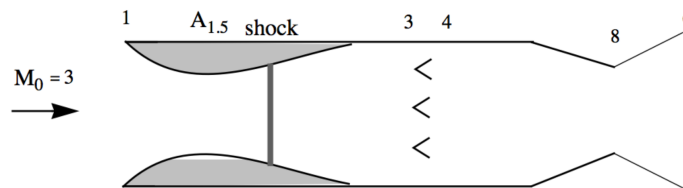


Figure 1: Ramjet with fully expanded nozzle.

ing part of the inlet. The stagnation temperature exiting the burner is  $T_{t4} = 1512\text{K}$ . The nozzle is fully expanded,  $P_e = P_0$ . The fuel enthalpy is  $h_f = 4.28 \times 10^7\text{J/kg}$ . The ambient temperature and pressure are  $T_0 = 216\text{K}$  and  $P_0 = 2 \times 10^4\text{N/m}^2$ .

- 1) Determine the fuel/air mass flow ratio,  $f$ .
- 2) Determine the stagnation pressure ratio,  $P_{t8}/P_{t0}$ .
- 3) Determine the nozzle exit Mach number,  $M_e$ .
- 4) Determine the dimensionless thrust,  $T/(P_0 A_0)$ .

### Problem 3

Shown below is a unique concept for a hypersonic scramjet. It operates on principles similar to a hybrid rocket except that the oxidizer is air entering the motor at  $M_0 = 5$ . The ambient temperature and pressure are  $227\text{K}$  and  $0.01\text{bar}$  corresponding to flight at about  $100,000$  feet. The air is decelerated through a loss-free inlet to  $M_3 = 2$ . The stagnation temperature of the incoming air is so high that auto-ignition occurs at the leading edge of the solid fuel grain and a diffusion flame is established over the length of the fuel surface producing hot gases for thrust. In a sense the solid fuel acts like a distributed spray injector of fuel into the supersonic stream. The solid fuel protects the motor case from the high combustion temperatures meaning the ramjet can operate at the stoichiometric fuel/air ratio,  $\dot{m}_f/\dot{m}_a = 0.07$  at station 4. The gas

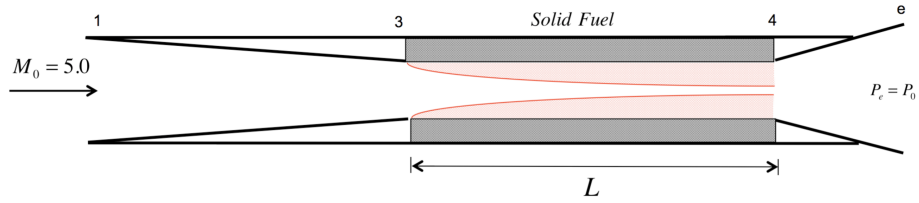


Figure 2: Solid fuel scramjet.

then expands to ambient pressure in a diverging nozzle. The exit velocity is  $U_e = 2337\text{m/sec}$ . Assume that the regression rate of the fuel is given by the simplified form  $\dot{r} = a(G_{air})^{1/2}$  where  $G_{air} = \dot{m}_{air}/\pi r^2$  is the mass flux of air along the port and  $r(t)$  is the instantaneous radius of the port. The regression rate constant is  $a = 1.54 \times 10^{-4}\text{m}^2/\text{kg}^{1/2}\text{sec}^{1/2}$ . The air mass flow rate is  $\dot{m}_{air} = 1000\text{kg/sec}$ . The fuel density is  $\rho = 800\text{kg/m}^3$ .

- 1) Show that the fuel mass flow rate is independent of the radius of the port.
- 2) Determine the port length  $L$  needed to generate the required fuel mass flow rate.
- 3) Determine the capture area,  $A_0$ .
- 4) Determine the thrust coefficient,  $C_{thrust} = T/(\gamma M_0^2 P_0 A_0/2)$ .