

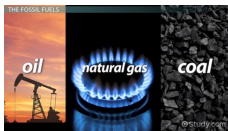
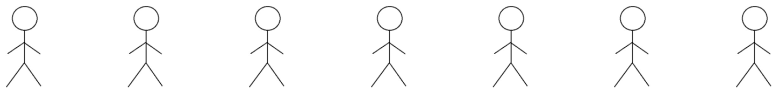
Markets for Public Decision-making

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October 6, 2021

joint work with Nikhil Garg and Ben Plaut

Public decision-making



Utility Model

- ▶ User i has binary preferences over the issues, and a weight $w_{i\ell} > 0$ for issue ℓ . The decision z_ℓ on issue ℓ lies in $[0, 1]$.
- ▶ Utility of user i is given by $u_i(z) = \sum_\ell w_{i\ell} x_i^{(\ell)}$ where $x_i^{(\ell)} = z_\ell$ if user i prefers side 0 on issue ℓ and $1 - z_\ell$ otherwise.

“One person one vote”

- ▶ Give each person a single vote on each issue and select the outcomes which receive the most votes
- ▶ Fair in some sense
- ▶ Lacks expressiveness
- ▶ Can lead to very suboptimal outcomes

MAJORITY VOTING ON EVERY ISSUE

	SIDE 1	SIDE 2
ISSUE 1	A B	C
ISSUE 2	A C	B
ISSUE 3	B C	A

UTILITY

4 when in minority
1 when in majority

VOTE

Side 1 has majority

DECISION

100% Side 1

WELFARE

Everyone is 50% worse
Tyranny of Majority

Markets



Markets

- ▶ Each player has a budget they wish to spend, and has no value for leftover money
- ▶ Goods are divisible
- ▶ “Fisher market” (Irving Fisher)
- ▶ “private goods”

Market equilibrium

- ▶ Each good has a price
- ▶ Each player buys her favorite affordable bundle
- ▶ An equilibrium always exists! [Arrow and Debreu, 1954]
 - ▶ Demand meets supply
 - ▶ The equilibrium maximizes Nash welfare [Eisenberg and Gale, 1959]:

$$\sum_i \log u_i$$

where u_i is the utility for player i

- ▶ Maximizing Nash welfare is often used as an approach to obtain "fair" allocations

Our goal

Design a mechanism for public decision-making based on private goods markets.

- ▶ More expressive than “one person one vote”
- ▶ Markets in general have nice properties
- ▶ Prices can be computed in an iterative and natural way
- ▶

Citizens purchasing political influence?

capitalism democracy



Our goal

Design a mechanism for public decision-making based on private goods markets.

- ▶ More expressive than “one person one vote”
- ▶ Markets in general have nice properties
- ▶ Prices can be computed in an iterative and natural way
- ▶ Each person gets equal endowment of “voting Dollars”

~~Citizens purchasing political influence?~~

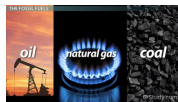
capitalism democracy



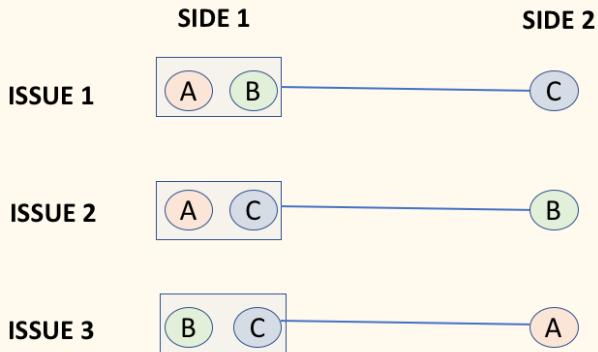
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A first attempt

- ▶ Assume issues are divisible/randomized
- ▶ Each issue has a price (this is the only thing that will change in our other model)
- ▶ Each player uses her budget to “buy probability” (ignoring supply)



SIMPLE PUBLIC MARKET



UTILITY

1.1 when in minority
1 when in majority

PRICE

Identical (symmetry)

EQUILIBRIUM

100% Side 2

WELFARE

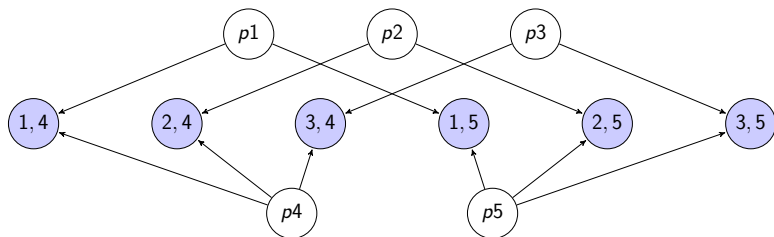
Everyone is 45% worse
Extends to factor N

Context on the simple market

- ▶ Similar to the “free rider” problem
- ▶ Observed in the classical literature before (e.g., [Danziger 1976])
- ▶ The same counter-example extends to several variants, e.g., Quadratic Voting [Lalley, Weyl 2014] and Trading Post [Shapley, Shubik 1977, Branzei et al 2016]
- ▶ Arbitrary per-player prices can implement the Nash-welfare solution (in fact any Pareto-optimal solution) via Lindahl equilibria [Foley 1979]
 - ▶ Lindahl prices are complex, and we would like a simple Fisher-like market, or a simple generative explanation
 - ▶ A simple market might lead to an implementable protocol

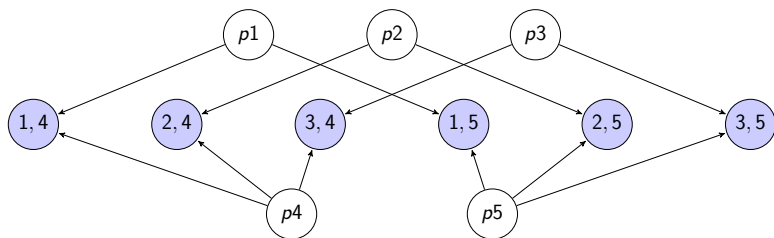
Reduction via Pairwise Expansion

- ▶ For any public decision-making instance, we create a private goods instance as follows
- ▶ Same set of players
- ▶ For each every issue, we create a good for each pair of players who disagree on that issue



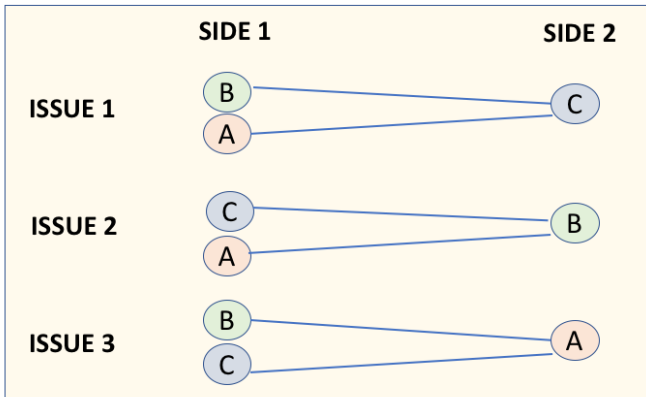
- ▶ “pairwise issue expansion”

Reduction via Pairwise Expansion



- ▶ Let u_i be the utility of player i in the private market
- ▶ One issue: x_{ij} is what player i buys of good j . Define
$$u_i = \min_{\text{her pairwise goods } j} x_{ij} \quad (\text{Leontief})$$
- ▶ Many issues: $u_i = \sum_{\text{issues } \ell} w_{i\ell} \left(\min_{\substack{\text{her pairwise goods } j \\ \text{on issue } \ell}} x_{ij}^{(\ell)} \right)$
- ▶ **Key insight:** For each issue, each player i is in direct competition with everyone she disagrees with, and with no one she agrees with

PAIRWISE EXPANDED MARKET



UTILITY

1.1 when in minority
1 when in majority

PRICE

Identical (symmetry)

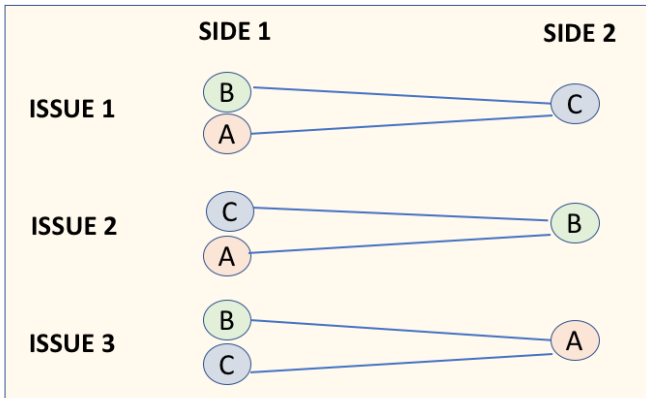
EQUILIBRIUM

100% Side 1

WELFARE

Maximizes
Nash Welfare

PAIRWISE EXPANDED MARKET



UTILITY

4 when in minority
1 when in majority

PRICE

Identical (symmetry)

EQUILIBRIUM

100% Side 2

WELFARE

Maximizes
Nash Welfare

Our main result

Theorem

Equilibria in the constructed private goods market correspond to valid solutions in the original public decisions instance.

- ▶ This will give us the nice private goods market equilibrium properties!
- ▶ Maximum Nash welfare

The mechanism:

- ▶ Players never see the constructed private goods market
- ▶ Compute equilibrium prices
- ▶ Reduction turns these into per-player prices in the public decisions instance
- ▶ These per-player prices give an equilibrium in the public decisions instance that maximizes Nash welfare.

Conclusion

- ▶ Markets have been well-studied for private goods, lots of nice properties
- ▶ Can use these concepts to design mechanisms for "fair" public decision-making in an epistemic sense
- ▶ Can lift private goods results to public decisions setting

Future work:

- ▶ More practical mechanisms (iterative? deterministic?)
- ▶ Scalability
- ▶ The cognitive load of complex mechanisms can itself can be a deterrent and lead to "unfairness". Simpler approaches?
- ▶ Need for more affirmative normative guidance