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# **The Interplay of Neutrino Nucleus Cross Sections and Nuclear Effects**

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Fermilab

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# The Exquisite Goal

and the **Hazards** that Block our Way

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## Main (4-Nail) Hazard: Knowledge of $\nu$ -Nucleus Interactions

What do we observe in our detectors constructed of heavy nuclei?

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$Y_{c\text{-like}}(E_m)$ : Yield in our detectors is dependent on

$\phi(E' \geq E_m)$  Neutrino Flux

⊗

$\sigma_{c,d,e..}(E' \geq E_m)$  Neutrino Cross Section

⊗

$Nuc_{c,d,e.. \rightarrow c}(E' \geq E_m)$  Neutrino Nuclear Effects

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⊗

$Nuc_{c,d,e. \rightarrow c}(E' \geq E_m)$  Neutrino Nuclear Effects

# Neutrino Nucleus Scattering

What do we observe in our detectors?

- 
- ◆ The events we observe in our detectors are convolutions of:

$$Y_{\mathbf{c-like}}(\mathbf{E}_m) \propto \phi_\nu(E' \geq E_m) \otimes \sigma_{\mathbf{c,d,e..}}(E' \geq E_m) \otimes \text{Nuc}_{\mathbf{c,d,e..} \rightarrow \mathbf{c}}(E' \geq E_m)$$

- ◆  $Y_{\mathbf{c-like}}(\mathbf{E}_m)$  is the event energy and channel / topology of the event observed in the detector. It is called **c-like** at  $\mathbf{E}_m$  since it is detected as channel c with energy  $E_m$  but may not have been so at interaction.
- ◆ The energy  $E_m$  is the sum of energies coming out of the nucleus that are measurable in the detector.
- ◆ That is the topology and energy measured in the detector is **not necessarily what was produced at the initial interaction. The neutrino physics analyses depend on the initial interaction.**

# Neutrino Nucleus Scattering

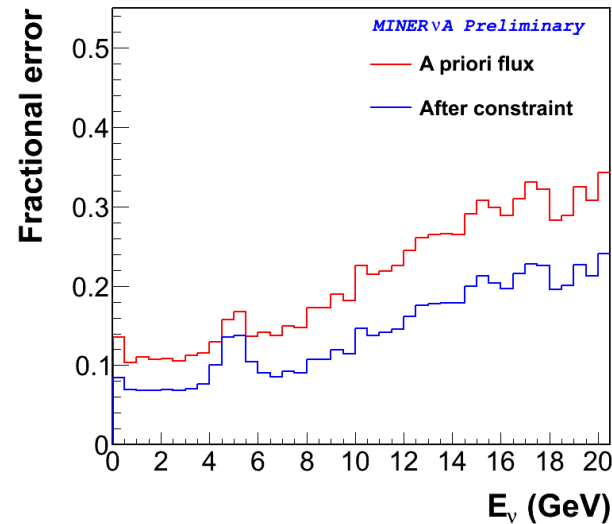
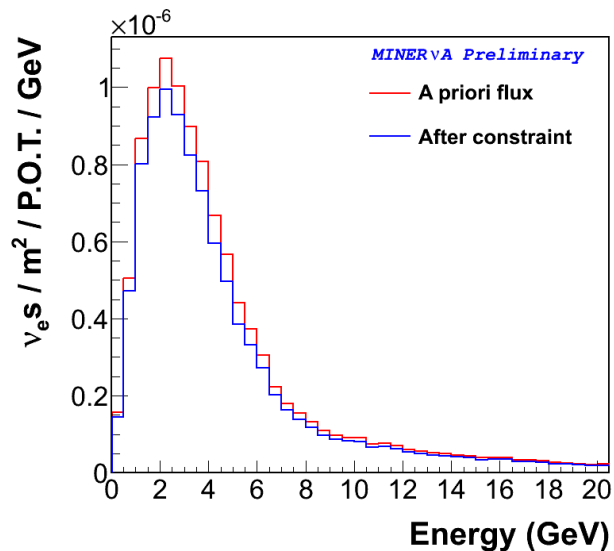
## Neutrino Flux Term: $\phi_\nu(E' \geq E_m)$

In-situ Flux Measurement:  $\nu - e$  scattering

$$\frac{d\sigma(\nu_\mu e^- \rightarrow \nu_\mu e^-)}{dy} = \frac{G_F^2 m_e E_\nu}{2\pi} \left[ \left( \frac{1}{2} - \sin^2 \theta_W \right)^2 + \sin^4 \theta_W (1-y)^2 \right]$$

$G_F$  and  $\theta_W$ : well-known electroweak parameters

- Using  $\nu - e$  results, we can apply an additional constraint to the flux
- Here, the a priori is the HP corrected flux.



- Reduction of 5-10% in the flux prediction and  $> 15\%$  in predicted uncertainty as well.

# Neutrino Nucleus Scattering

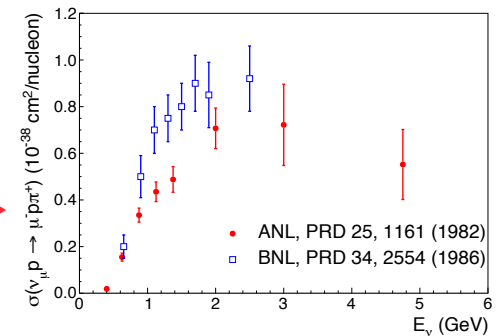
## Cross Section Term: $\sigma_{c,d,e..}(E' \geq E_d)$

- ◆ The events we observe in our detectors are convolutions of:

$$Y_{c\text{-like}}(E_d) \propto \phi_\nu(E' \geq E_d) \otimes \sigma_{c,d,e..}(E' \geq E_d) \otimes \text{Nuc}_{c,d,e..\rightarrow c}(E' \geq E_d)$$

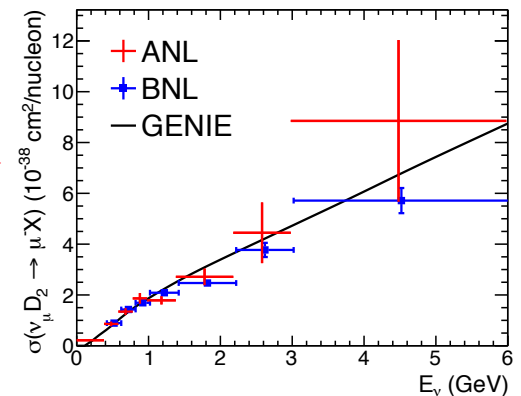
- ◆  $\sigma_{c,d,e..}(E')$  is the measured or the Monte Carlo (model) energy dependent neutrino cross section off a **nucleon within a nucleus**.

- ◆ **Limited statistics ANL and BNL bubble chamber data off  $D_2$  from the 80's is what we have ie.  $1 \pi$  production.**



- ◆ **Recent combined analyses of ANL and BNL data using ratios of  $\sigma_{QE}$  to  $\sigma_{Tot}$  have claimed to resolve flux issues and we now could have a much improved combined fit.**

Wilkinson et al. – arXiv:1411.4482



- ◆ **However a recent study by Sato suggests that nuclear effects in deuterium have to be carefully considered.**

# Neutrino Nucleus Scattering

## Nuclear Effects Term: $\text{Nuc}_{c,d,e.. \rightarrow c}(E' \geq E_d)$

- ◆ The events we observe in our detectors are convolutions of:

$$Y_{c\text{-like}}(E_d) \propto \phi_\nu(E' \geq E_d) \otimes \sigma_{c,d,e..}(E' \geq E_d) \otimes \text{Nuc}_{c,d,e.. \rightarrow c}(E' \geq E_d)$$

- ◆  $\text{Nuc}_{c,d,e.. \rightarrow c}(E' \geq E)$  – Nuclear Effects

- ▼ **The Supreme Mixer / The Grand Deceiver** – a migration matrix that mixes produced channel and energy to detected channel and energy.

- ▼ There are many nuclear effects that have to be considered that take the interaction of a neutrino with energy  $E'$  with the bound nucleon(s) and producing initial channel  $d,e...$  that will then appear in our detector as energy  $E$  and channel  $c$ .

- ▼ The physics we want to study depends on the initial interaction – not what we observe coming out of the nucleus. **How do we move detected quantities backwards through the nucleus?**



# A Step-by-Step Two-Detector LBL Oscillation Analysis

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- 1) Measure neutrino energy and event topology in the near detector.
- 2) Use the **nuclear model** to take the detected energy and topology back to the initial interaction energy and topology.
- 3) Project this initial interaction distribution, perturbed via an oscillation hypothesis, to the far detector.
- 4) Use the **nuclear model** to take the incoming energy and topology to a detected energy and topology.
- 5) Compare with actual measurements in the far detector.

**Critical dependence on the nuclear model even with a near detector!**

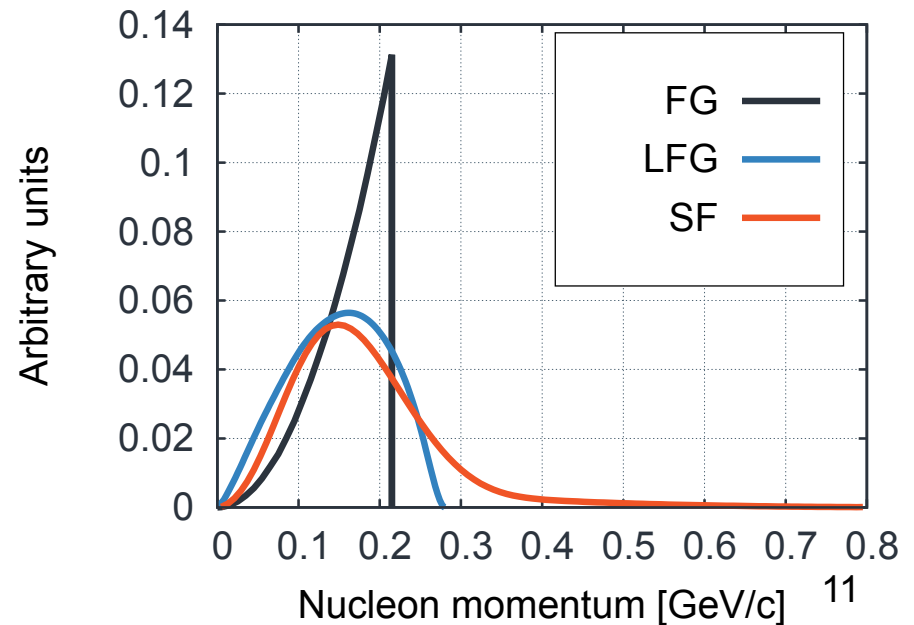
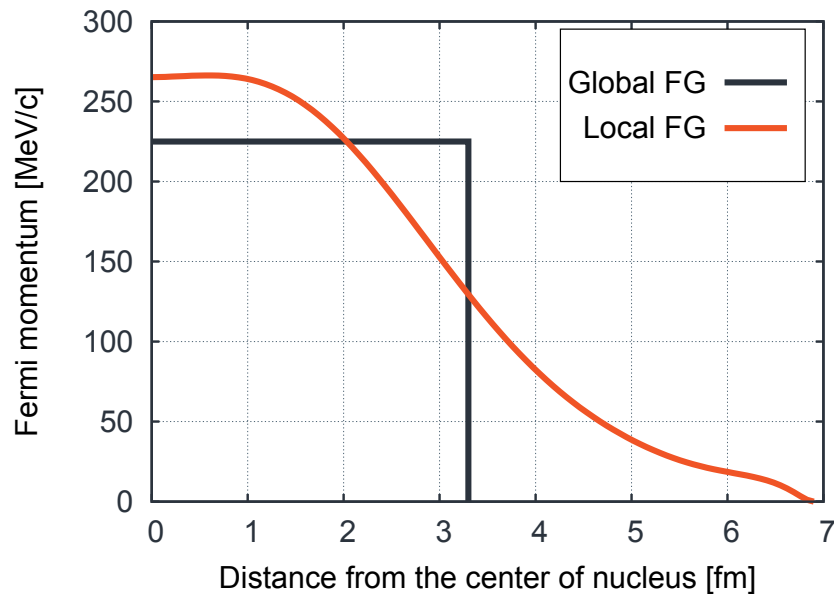
**How do we constrain/improve the nuclear model?**

# What are these Nuclear Effects $\text{Nuc}_{c,d,e.. \rightarrow c} (E' \geq E)$ in Neutrino Nucleus Interactions?

- ◆ Target nucleon in motion – classical Fermi gas model or spectral functions (Benhar et al.) or more sophisticated models.
- ◆ Certain reactions prohibited - Pauli suppression.
- ◆ Nucleon-nucleon correlations such as MEC and SRC and even RPA implying multi-nucleon initial states.
- ◆ Cross sections, form factors and structure functions are modified within the nuclear environment and parton distribution functions within a nucleus are different than in an isolated nucleon.
- ◆ Produced topologies are modified by final-state interactions modifying topologies and possibly reducing detected energy.
  - ▼ Convolution of  $\sigma(n\pi)$  (x) formation zone model (x)  $\pi$ -charge-exchange/absorption.

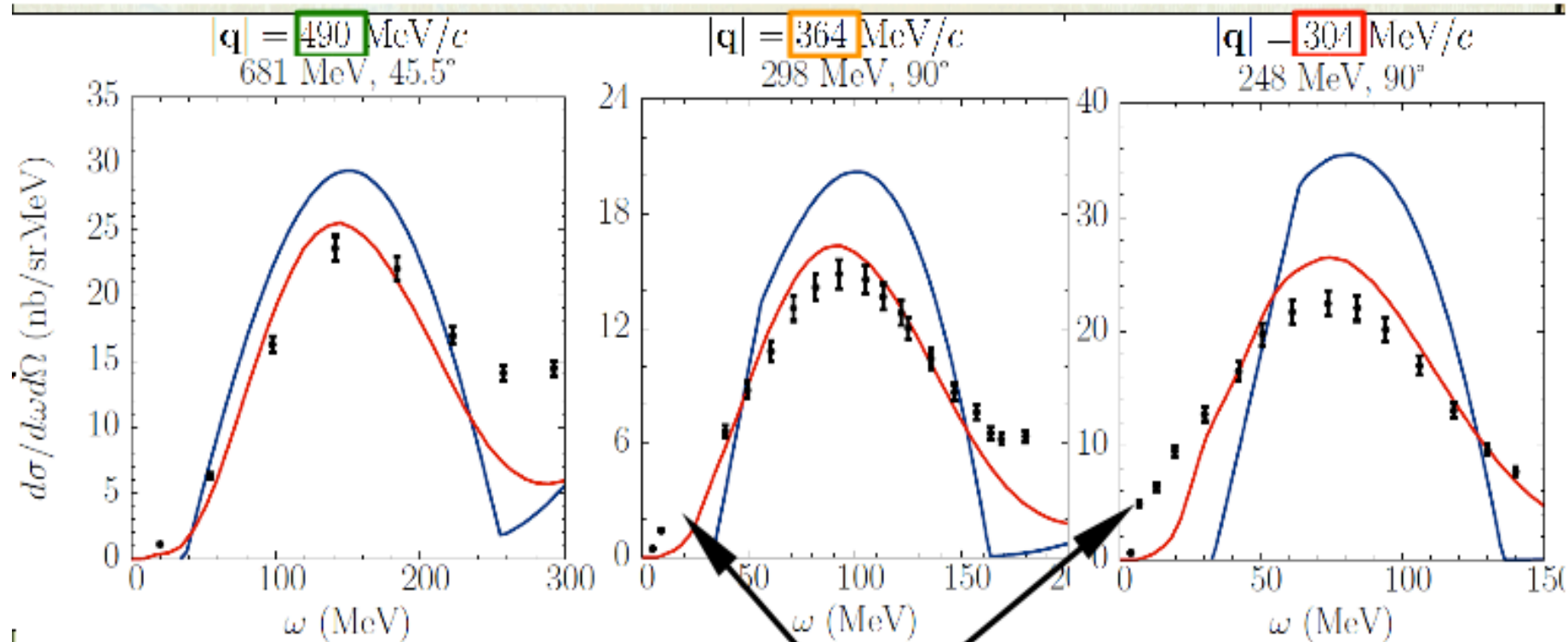
# Before the $\nu$ even interacts, what is the initial state of nucleons within the nucleus?

- ◆ **Fermi Gas:** Nucleons move freely within the nuclear volume in a constant binding potential.
- ◆ **Spectral Function:** The probability of removing of a nucleon with momentum  $p \vec{}$  and leaving residual nucleus with excitation energy  $E$ . Allows off mass shell nucleons.



# Target Nucleon in Motion – Fermi Gas (still in many models) vs Spectral Function. A step up in sophistication

Superior particularly as Q Decreases



**Spectral function**

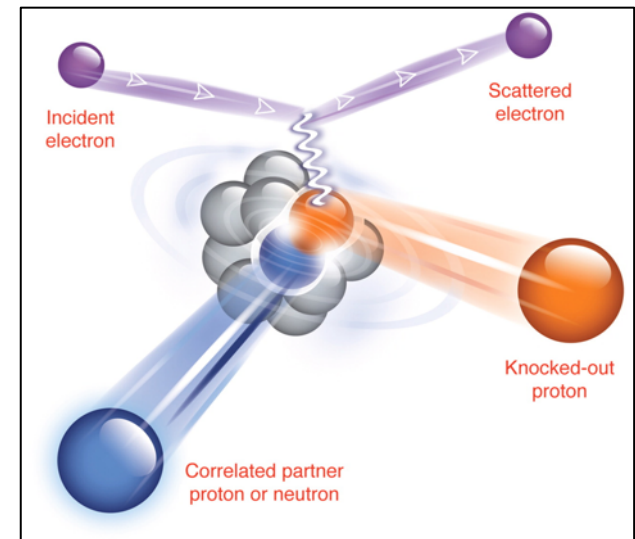
**Fermi gas**

When  $|q| \leq 400$  MeV two- and few-nucleon contributions appear

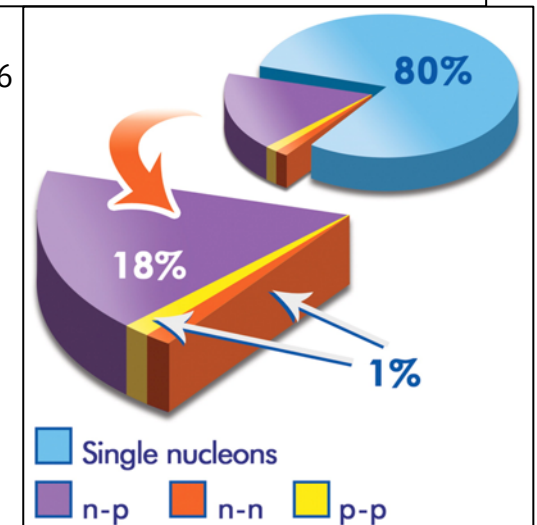
Artur Ankowski  
NuInt09

# Independent Nucleons? Nucleon-Nucleon Correlations

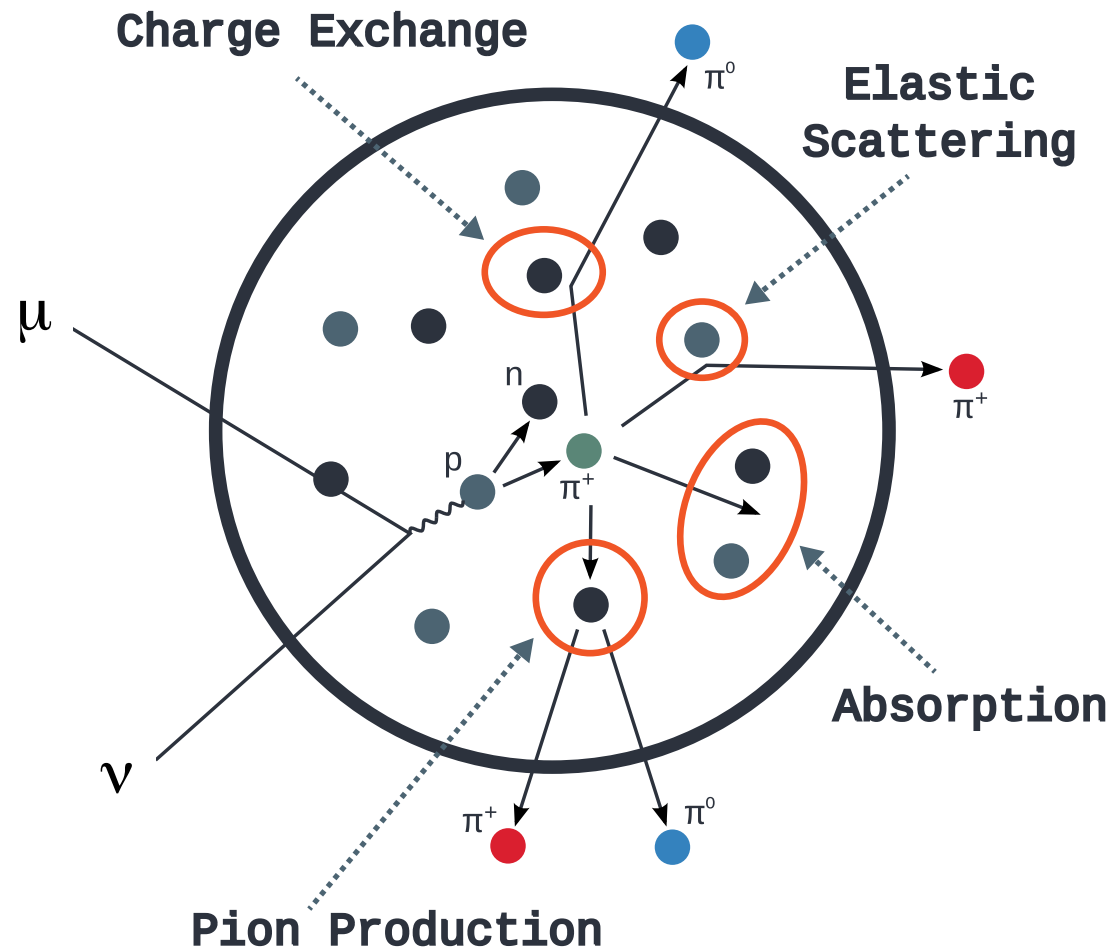
- ◆ Electron scattering
  - ▼ Measurements on  $^{12}\text{C}$  indicate 20% correlated nucleons with mostly **np** pairs in the initial state.
- ◆ Neutrino scattering
  - ▼ Implies initial produced state in neutrino scattering of **nn in antineutrino** and **pp in neutrino** CC scattering.
  - ▼ For other forms of correlation, final state depends on model.
  - ▼ **Of course, what we eventually detect can be modified by Final State Interactions when interpreting neutrino scattering data.**



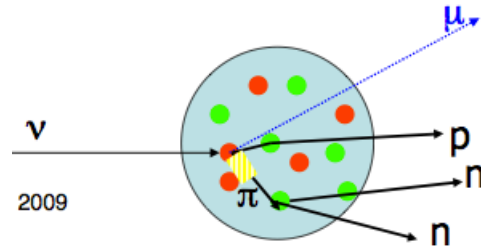
R. Subedi et al.,  
Science 320, 1476  
(2008)



# Final State Interactions (FSI)



# Final State Interactions (FSI)



- ◆ Components of the initial hadron shower interact within the nucleus changing the apparent final state configuration and even the detected energy. Currently using mainly **cascade models for FSI**.
- ◆ For example, an initial pion can charge exchange or be absorbed on a pair of nucleons.
- ◆ Final state observed is  $\mu + p$  that makes this a fine candidate for QE production. We've probably also lost measurable energy.

Example numbers	Final $\mu p$	Final $\mu p \pi$
Initial $\mu p$	90%	10%
Initial $\mu p \pi$	25%	75%

# Neutrino Nucleus Scattering

## Putting it all together: The Nuclear Model

- ◆ The events we observe in our detectors are convolutions of:

$$Y_{c\text{-like}}(E_d) \propto \phi_\nu(E' \geq E_d) \otimes \overset{\text{effective } \sigma_{c\text{-like}}^A(E)}{\sigma_{c,d,e..}(E' \geq E_d)} \otimes \text{Nuc}_{c,d,e.. \rightarrow c}(E' \geq E_d)$$

- ◆ The community models these last two terms in **event generators**:
  - ▼ Provide information on how signal and background events should **appear** in our detectors if the model is correct.
  - ▼ Provide means for estimating systematic errors on measurements.
  - ▼ One of the most important components in the analysis of neutrino experiments.
- ◆ Current Generators used by experimental community – each with their own models of the nuclear environment!
  - ▼ **GENIE** – ArgoNeut, MicroBooNE, MINOS, MINERvA, NOvA, T2K, DUNE
  - ▼ **NEUT** – SuperKamiokande, K2K, SciBooNE, T2K
  - ▼ **NuWRO** – K2K, MINERvA as check of other generators
- ◆ **GiBUU** – Nuclear Transport Model used to check other generators<sup>16</sup>

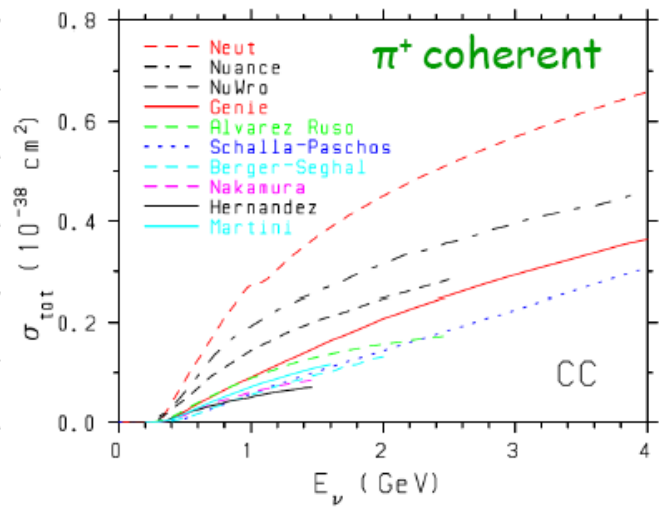
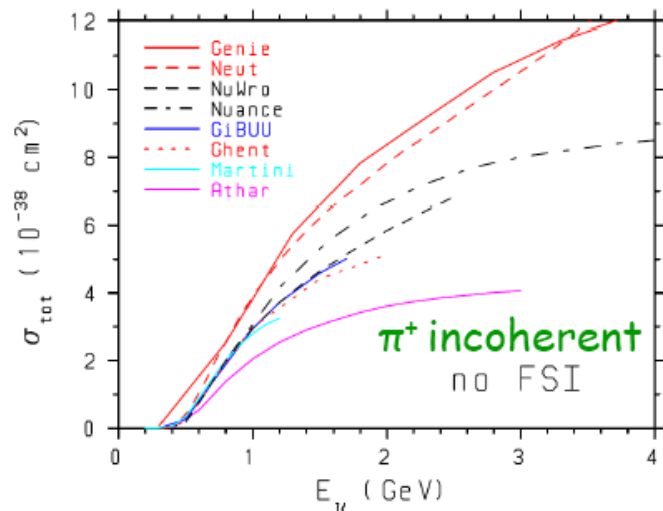
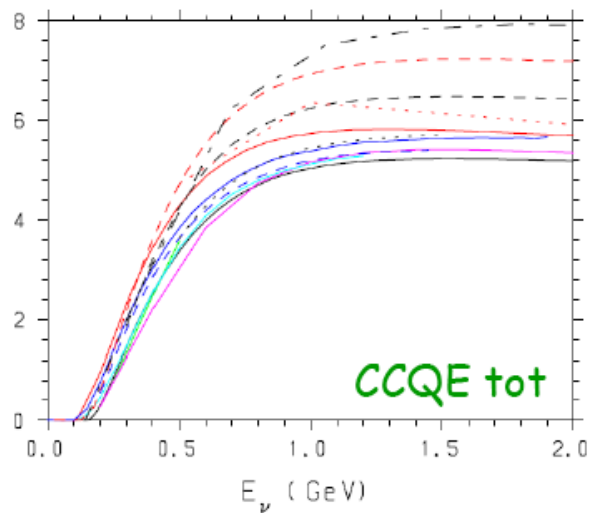
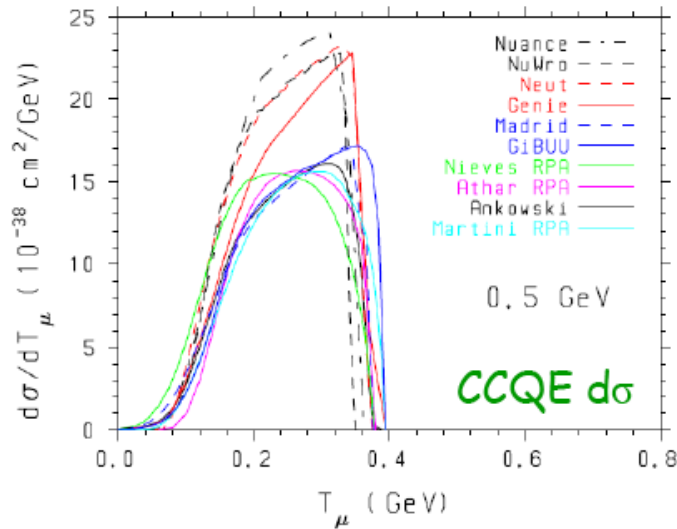


# How Good are these Nuclear Models?

Addressing this question in this talk?

Range of Existing Model (MC) Predictions off C

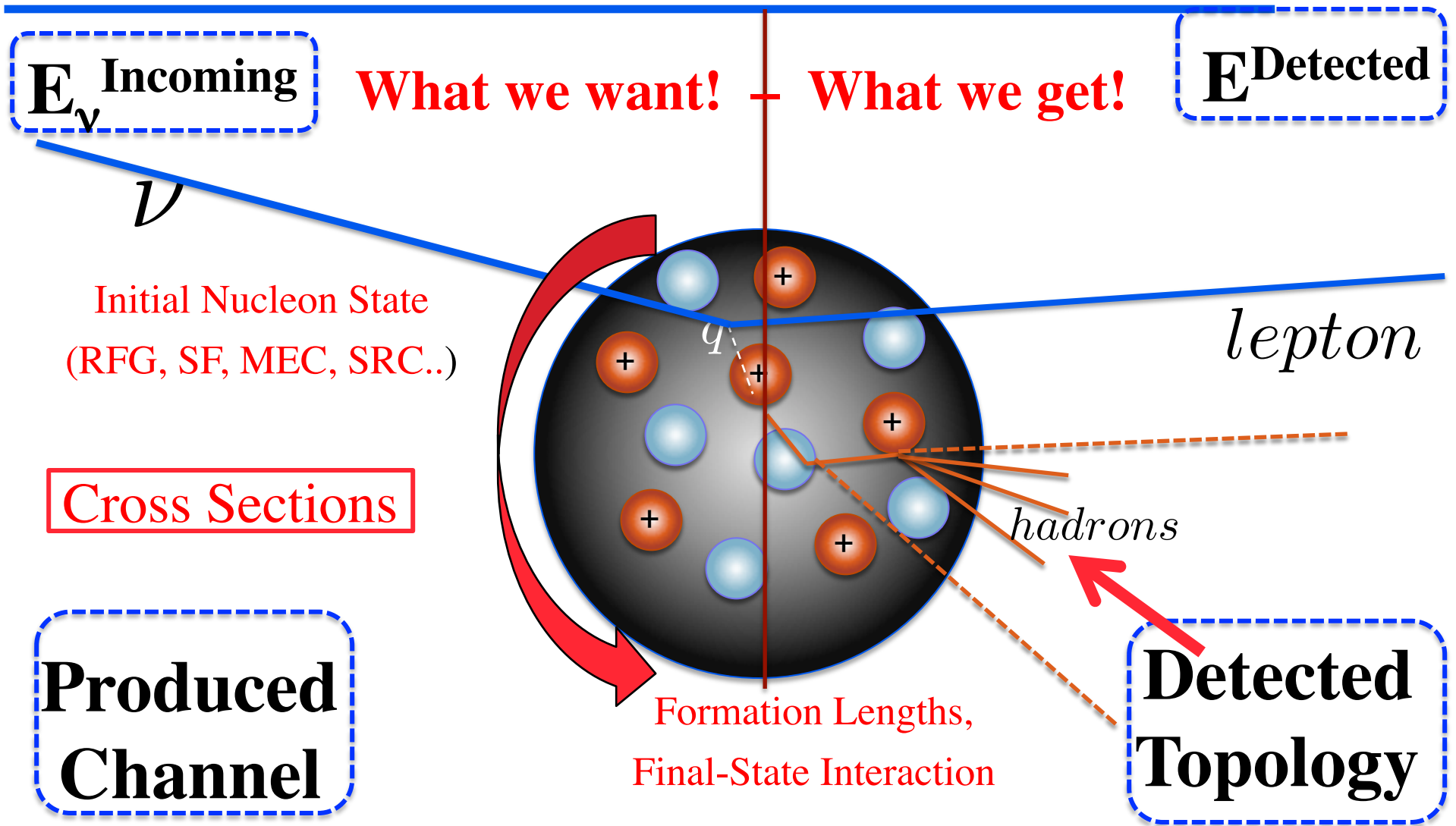
NuInt09  
Steve Dytman



# Where we are depends on which nuclear model / generator we use!



# Nuclear Physics of GeV $\nu$ -nucleus Interactions



# Understanding Effects of the Nucleus

## Leptonic vs Hadronic Clues

### ◆ **Lepton:**

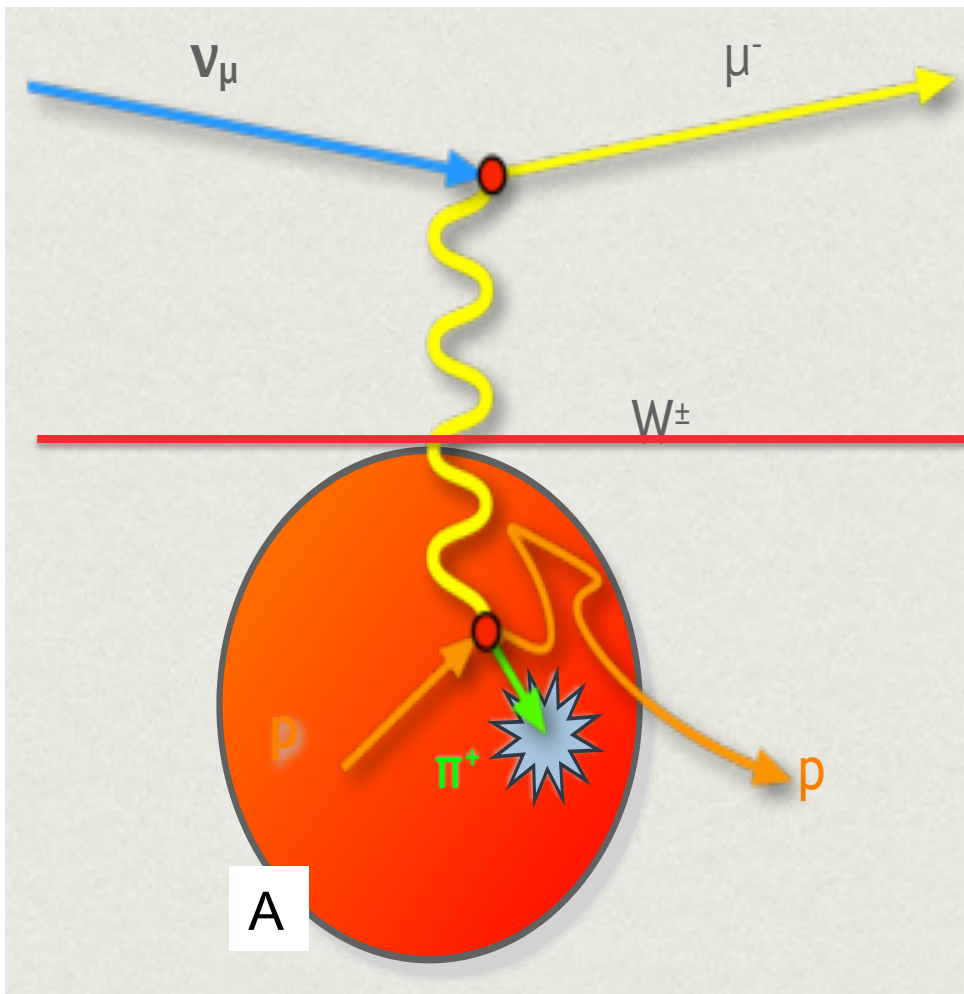
- ◆ Provide information on initial interaction on nucleon within the nucleus.

### ◆ **Initial Nucleon State**

- ▼ **Relativistic Fermi Gas Model**
- ▼ **Local Fermi Gas Model**
- ▼ **Spectral Functions**
- ▼ **Correlated Nucleons (RPA, MEC, SRC..)**

### ◆ **Hadrons:**

- ◆ Provide information on Final State Interactions within the nucleus.
  - ▼ **Note that correlated nucleons (RPA, MEC, SRC..) also undergo final state interactions.**



# Important Contributors to Results in this Presentation

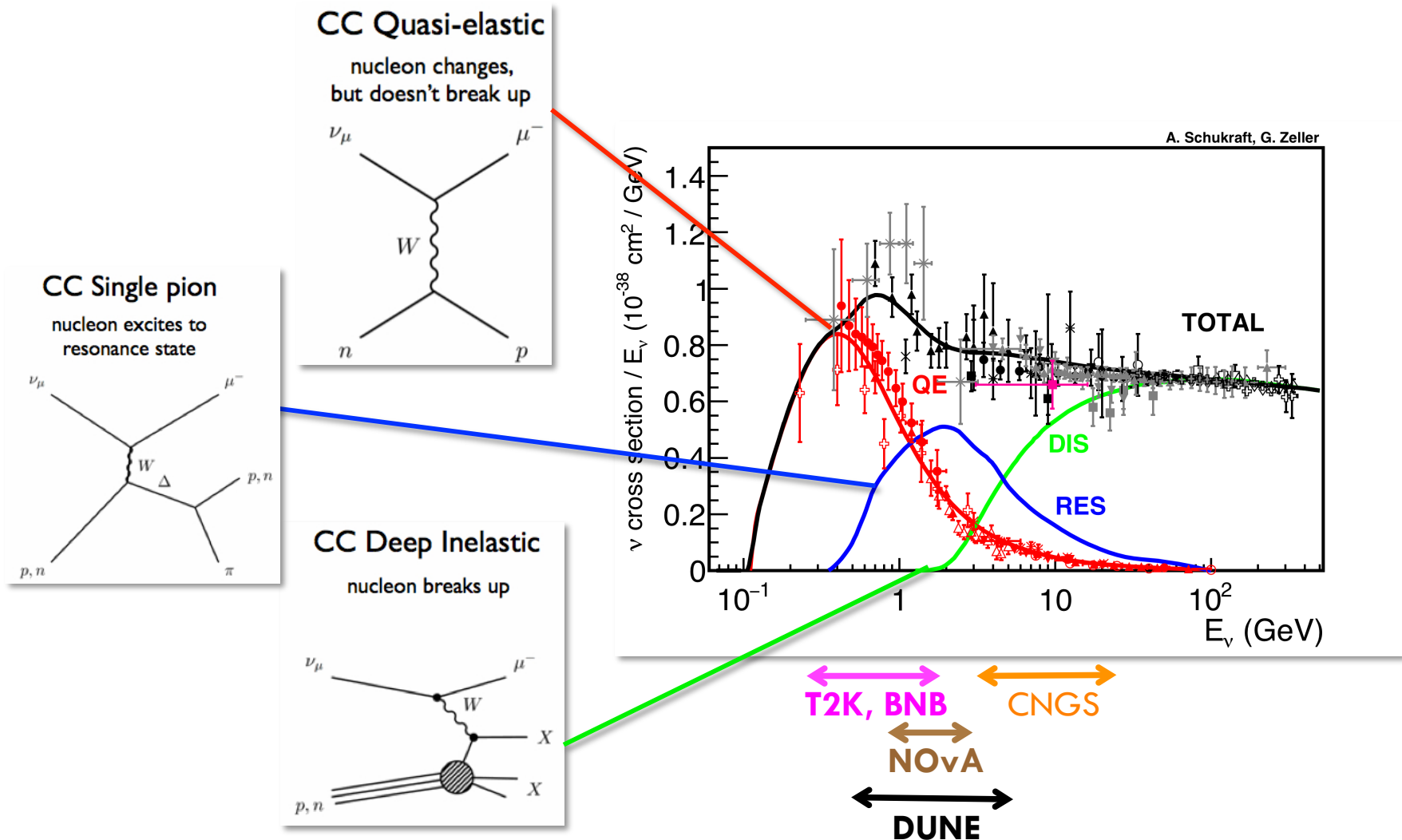
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- ◆ There are many excellent neutrino nucleus interaction measurement from MiniBooNE, ArgoNeut and T2K that I will only mention in passing.
- ◆ To get the message across, since no specific MINERvA talk, I will concentrate on results from MINERvA that are mainly due to the analyses of:
  - ▼ Arturo Fiorentini – Rio de Janeiro (now York postDoc)
  - ▼ Aaron Higuera – Guanajuato (now Huston postDoc)
  - ▼ Brandon Eberly, Pittsburgh (now SLAC postDoc)
  - ▼ Brian Tice, Rutgers (to ANL postDoc now Bloomberg capitalist)
  - ▼ Tammy Walton, Hampton (now Fermilab postDoc)
  - ▼ Trung Le, Rutgers postDoc
  - ▼ Carrie McGivern, Pittsburgh postDoc
- ◆ Borrowed freely from presentations of Steve Dytman and Sam Zeller

# Dominant Interaction Modes

We essentially know the vector part of these interactions via CVC and e-A scattering.

**The challenge is the axial-vector contribution!**



# Quasi-elastic (QE) Neutrino Scattering

Here from a free nucleon

first derived by C.H. Llewellyn-Smith

$$\frac{d\sigma}{dQ^2} = \frac{M^2 G_F^2 \cos^2 \theta_c}{8\pi E_\nu^2} \left[ A(Q^2) + B(Q^2) \frac{(s-u)}{M^2} + C(Q^2) \frac{(s-u)^2}{M^4} \right]$$

The vector form factors ( $F_V^1$  and  $F_V^2$ ) can be related to the nucleon electromagnetic form factors, which are described by electron scattering data.

A first order approximation (Goldberger-Treiman relation) relates the pseudoscalar form factor ( $F_P$ ) to the axial form factor.

The axial form factor ( $F_A$ ) is approximated by the dipole form.

nuclear  $\beta$ -decay experiments

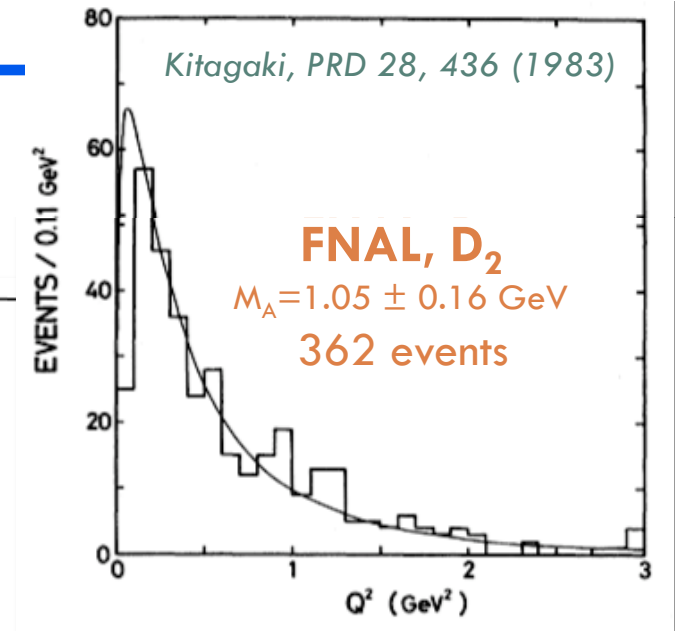
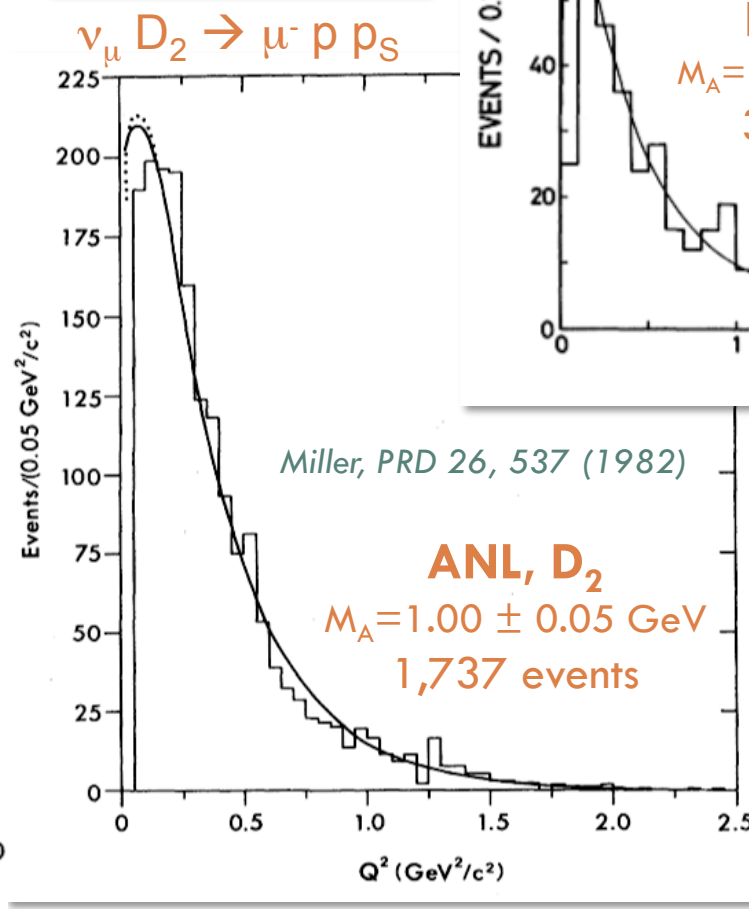
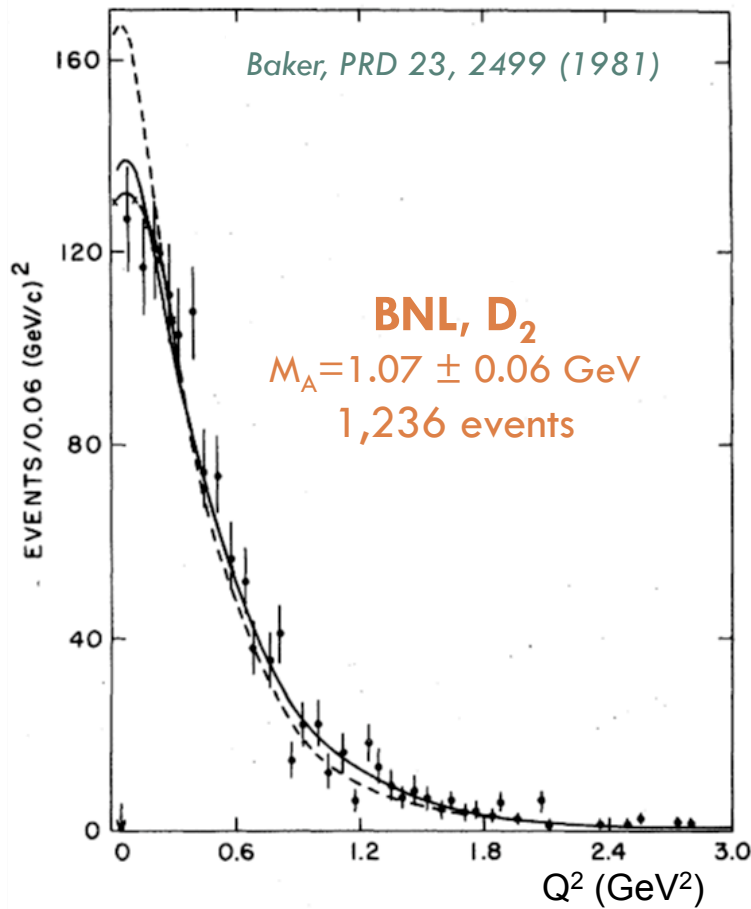
$$F_A(Q^2) = \frac{F_A(Q^2=0)}{\left(1 + \frac{Q^2}{M_A^2}\right)^2}$$

Axial Mass

Extracted from neutrino quasi-elastic cross-section measurements.

# First QE **Nucleon** Results Published in early '80s

Good Agreement on the value of  $M_A$



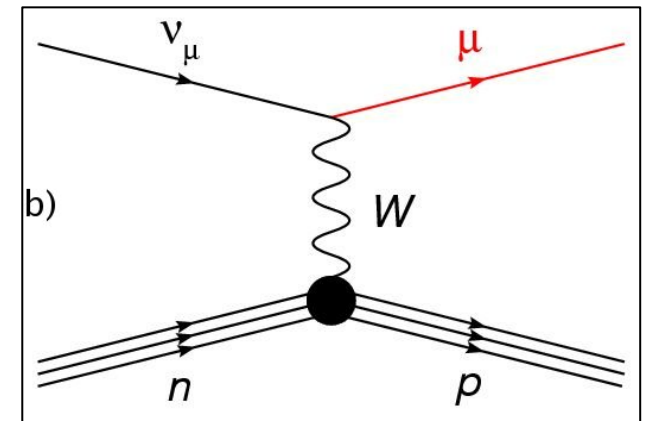


Where the real effects of nucleus-induced problems begin!

## Quasi-elastic (QE) Neutrino **Nucleus** Scattering

Important for oscillation experiments

- ◆ A technique used by oscillation experiments, (particularly when blind to the hadronic final state), for analyzing quasi-elastic scattering, is to assume the **nucleon is at rest!**
- ◆ One can then determine  $E_\nu$  and  $Q^2$  from lepton side kinematics only (“2-body interaction”)



neutrino energy

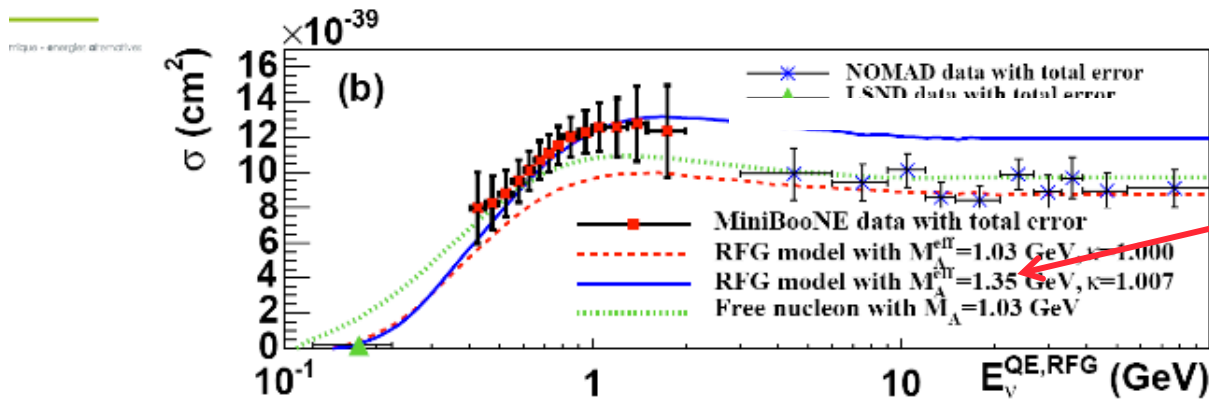
$$E_\nu^{QE} = \frac{2(M_n - E_B) E_\ell - \left[ (M_n - E_B)^2 + m_\ell^2 - M_p^2 \right]}{2[M_n - E_B - E_\ell + p_\ell \cos(\theta_\ell)]}$$

$$Q_{QE}^2 = -m_\ell^2 + 2E_\nu^{QE} \left( E_\ell - \sqrt{E_\ell^2 - m_\ell^2} \cos(\theta_\ell) \right)$$

4-momentum transferred

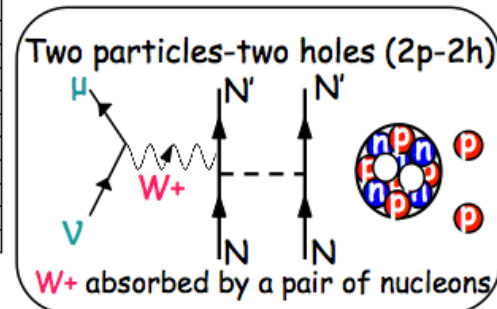
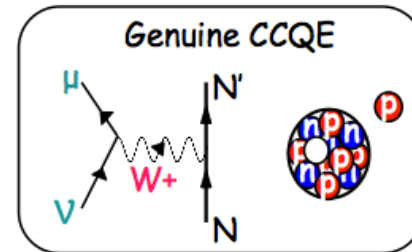
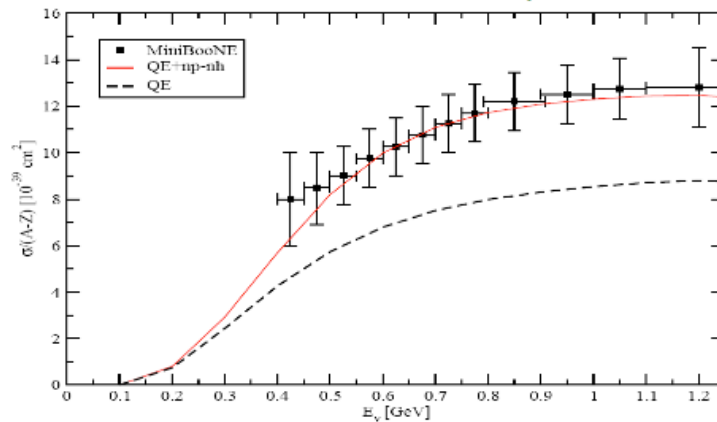
$M_n$  = neutron mass  
 $M_p$  = proton mass  
 $E_B$  = separation energy  
 $m_\ell$  = lepton mass  
 $E_\ell, \theta_\ell$  = lepton energy and angle

# The MiniBooNE QE Analysis: Introduction of nucleon-nucleon correlations Meson Exchange Currents – 2p2h Effects



$M_A = 1.35$  GeV

Inclusion of the multinucleon emission channel (np-nh)



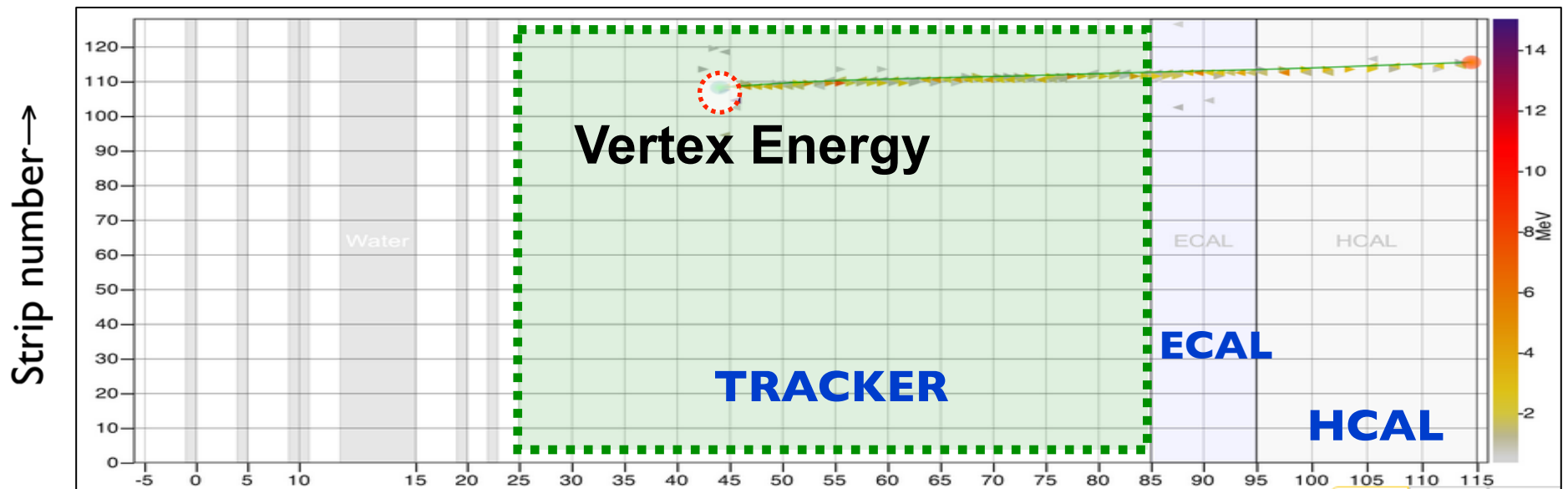
# MINERvA: Single Muon (lepton side) QE-like Analysis

Also sees evidence for nucleon-nucleon correlation effects

$\bar{\nu}_\mu$  Beam  $\longrightarrow$

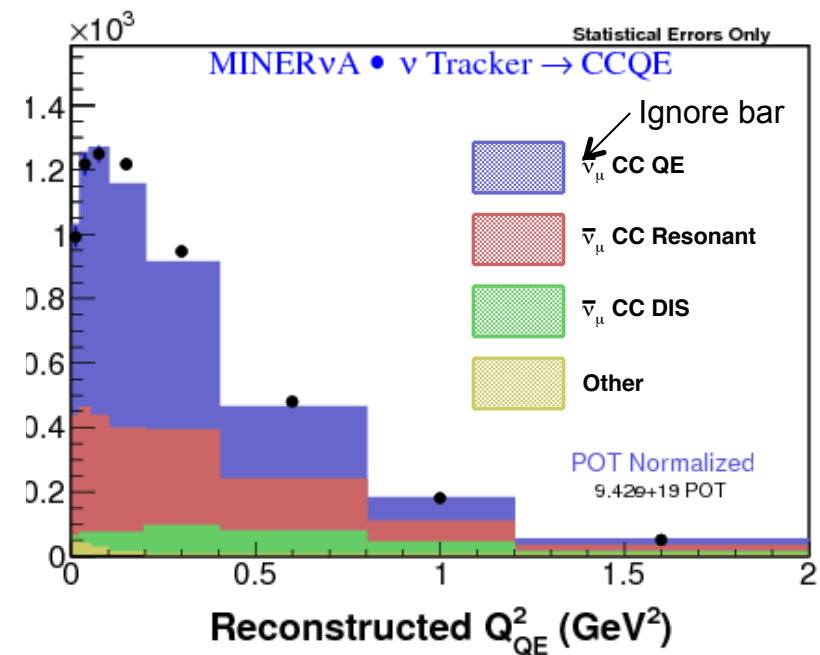
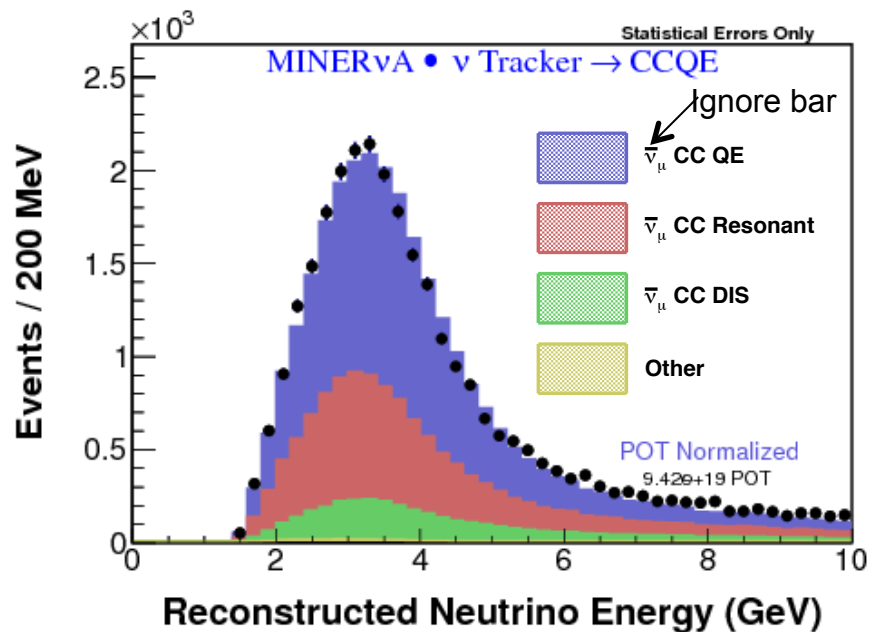
Fiducial volume:  
5.57 tons scintillator (CH)

MeV



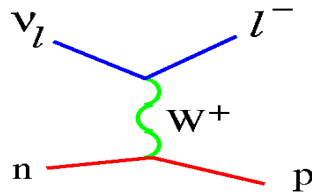
# MINERvA: Single Muon QE-like Analysis

- ◆ According to this nuclear model (GENIE) analysis, the resulting QE-like sample is 49% QE with large QE-like contributions from resonant, transition and even DIS events appearing, through nuclear effects, as QE in the detector



# These Nuclear Effects Change the $E_{QE}$ and $Q_{QE}^2$ Reconstruction for “QE” Events

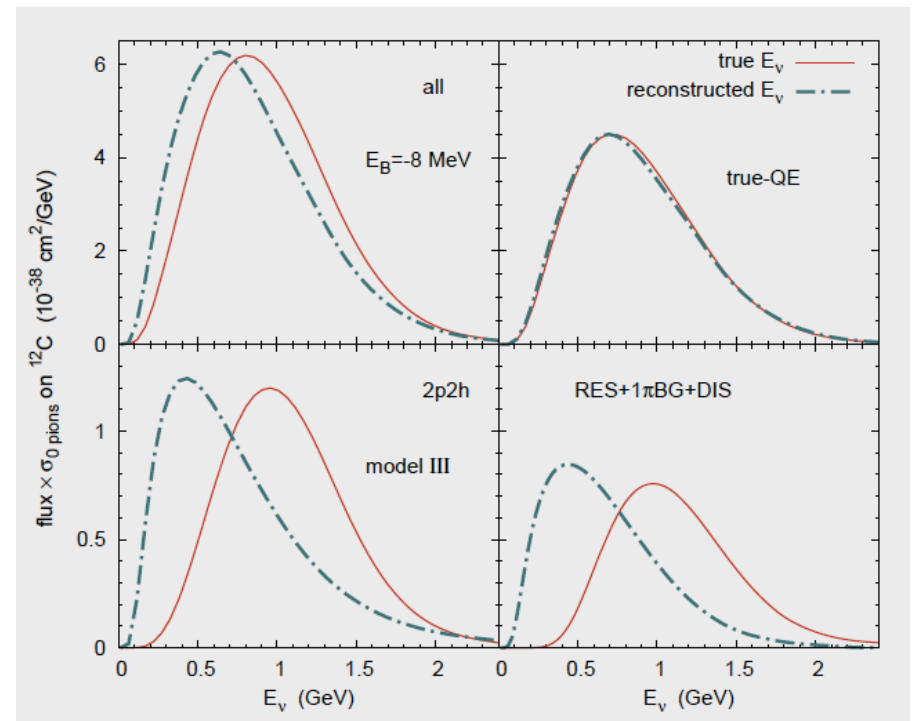
- Using the outgoing lepton to determine  $E_{QE}$  and  $Q_{QE}^2$ :



$$E_{QE} = \frac{2M_N E_\mu - m_\mu^2}{2(M_N - E_\mu + p_\mu \cos \theta_\mu)}$$

Reconstructed energy shifted to lower energies for all processes other than true QE.

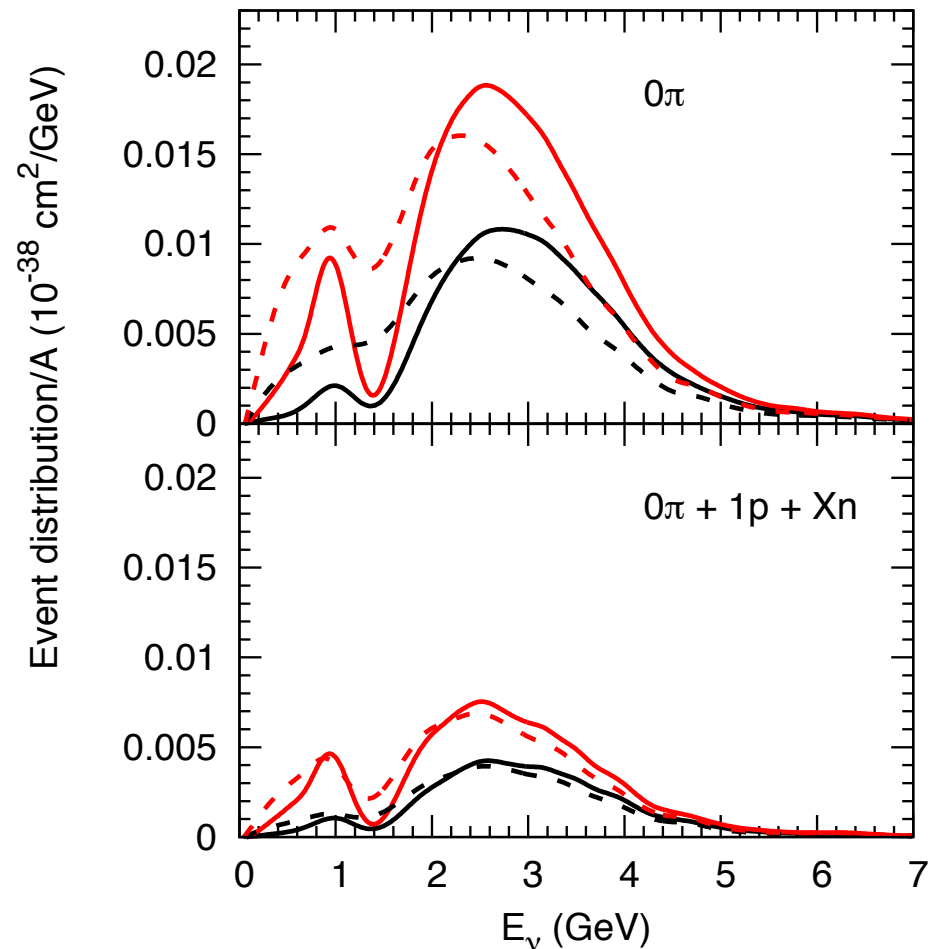
Number of events experiencing these shifts depends on the nuclear model being used!



U. Mosel GiBUU

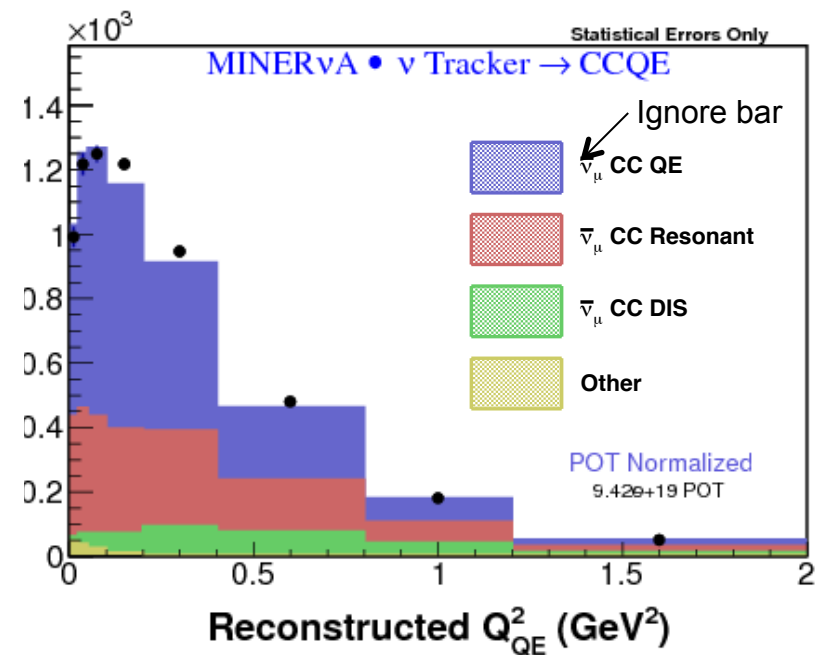
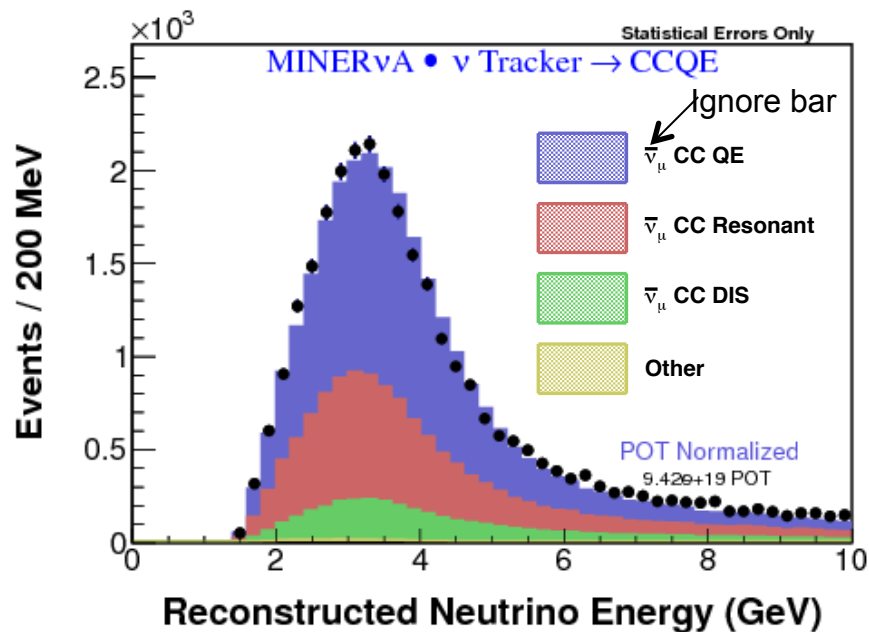
# Significant Implications for Oscillation Experiments using only the Lepton Information

- ◆ **We need an excellent model of this convolution to be able to extract physics quantities from the far detector measurements to needed precision.**
- ◆ At right, for  $\nu_e$  appearance, using a pre-DUNE  $E_\nu$  spectrum looking for CP violations with  $\delta_{CP} = +\pi/2$  (red) and  $-\pi/2$  (black) at initial interaction (solid) and detected after nuclear effects (dashed).
- ◆ **Other generators using alternative models get different results.**

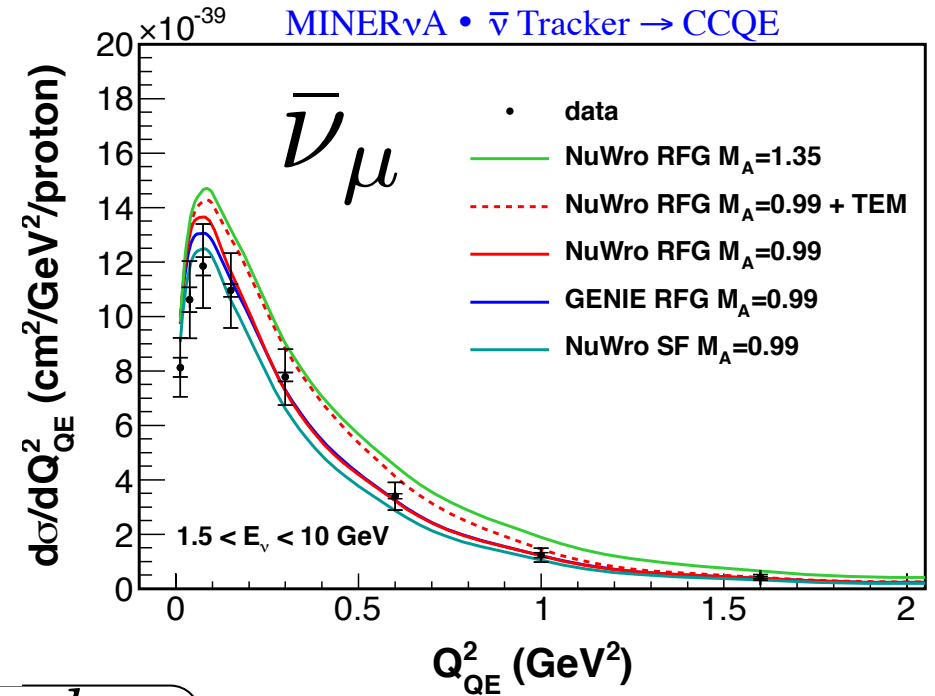
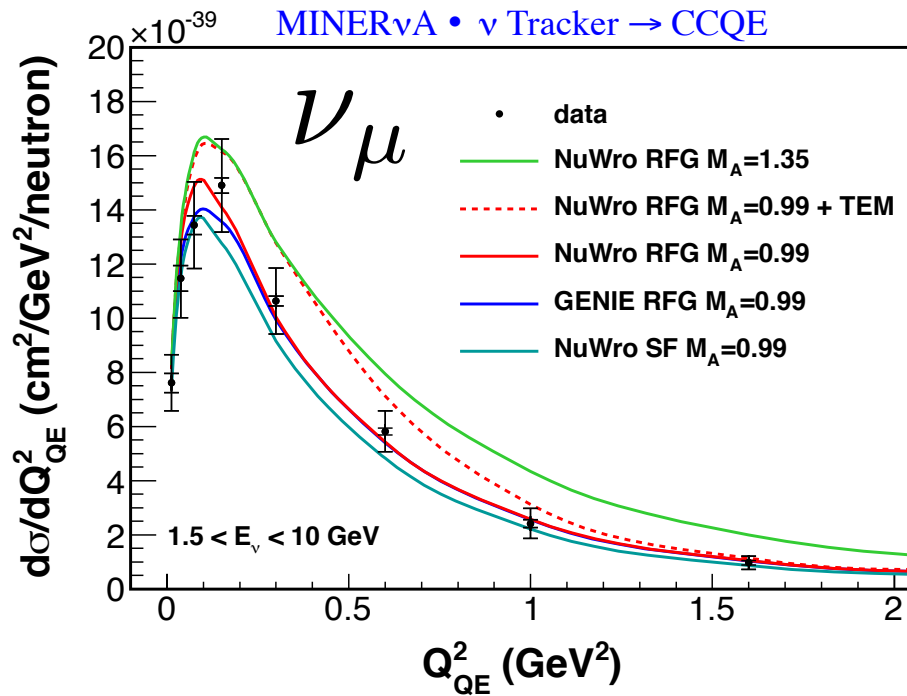


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# MINERvA: Single Muon QE-like Analysis



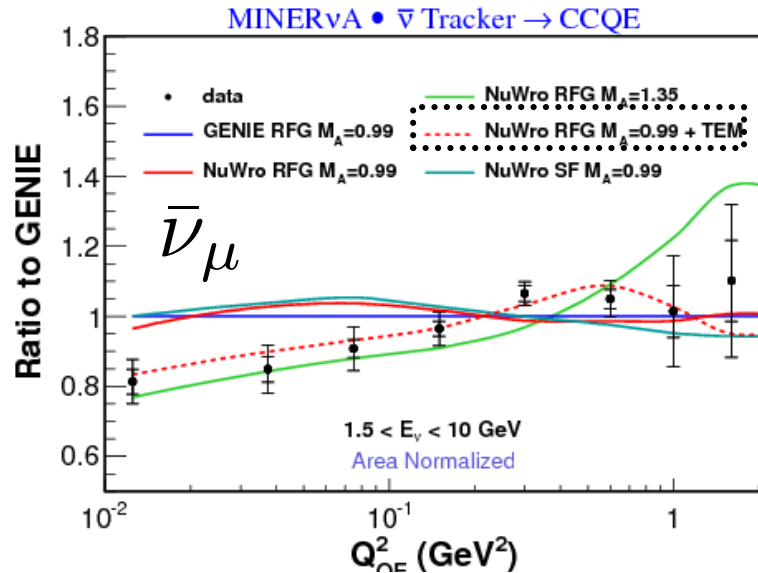
$$\frac{d\sigma}{dQ_{QE}^2}$$



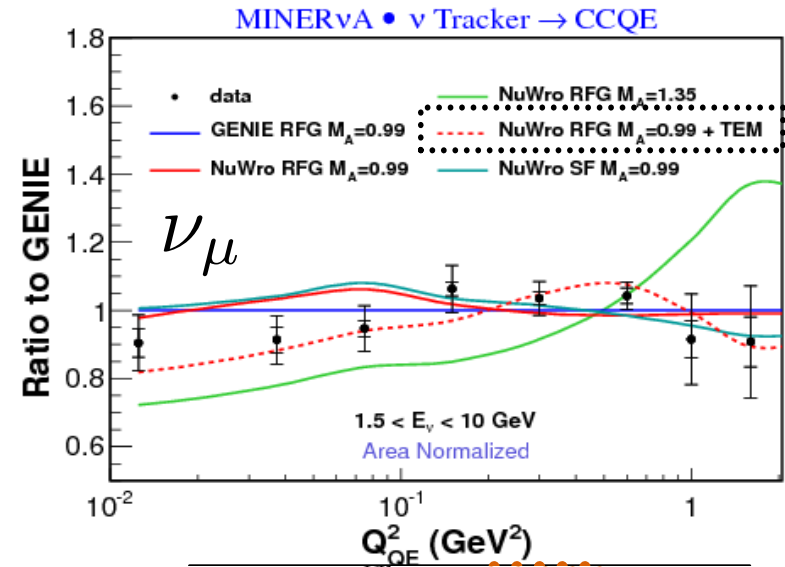
# MINERvA: Single Muon QE-like Analysis

Emphasis on the Shape

- Using leptonic information only, the results favor the RFG with  $M_A = 0.99$  + a Transverse Enhancement Model for NN correlations (vector current only contributions!!)



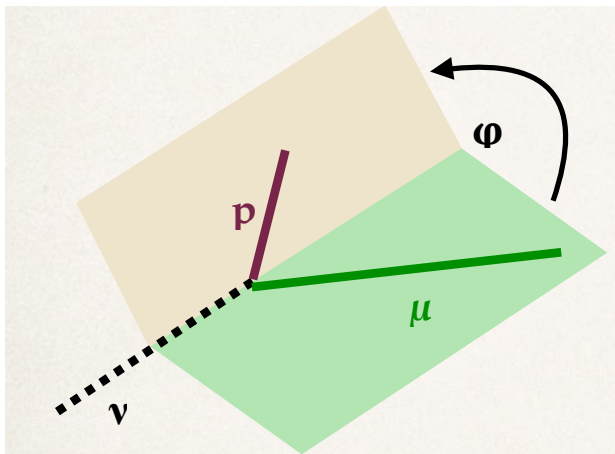
NuWro Model	RFG	RFG + TEM	RFG	SF
$M_A$ (GeV)	0.99	0.99	1.35	0.99
Rate $\chi^2$ /d.o.f.	2.64	1.06	2.90	2.14
Shape $\chi^2$ /d.o.f.	2.90	0.66	1.73	2.99



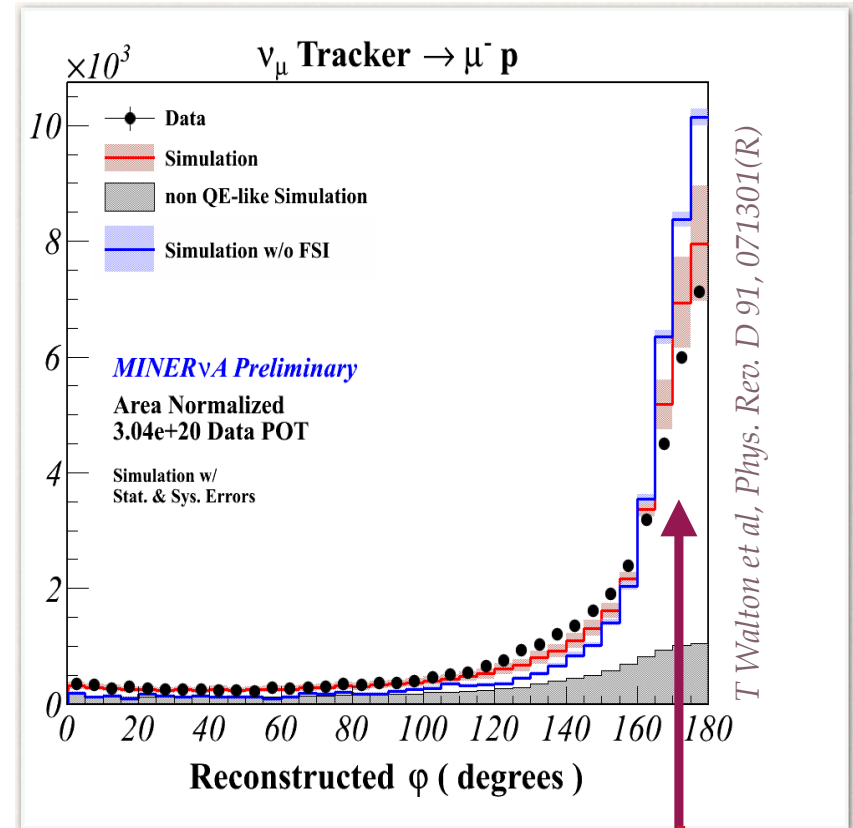
NuWro Model	RFG	RFG + TEM	RFG	SF
$M_A$ (GeV/c <sup>2</sup> )	0.99	0.99	1.35	0.99
Rate $\chi^2$ /d.o.f.	3.5	2.4	3.7	2.8
Shape $\chi^2$ /d.o.f.	4.1	1.7	2.1	3.8

# Quasi Elastic from the Hadron Side

- ◆ Study the angle between the  $\nu$ - $\mu$  and  $\nu$ -p planes



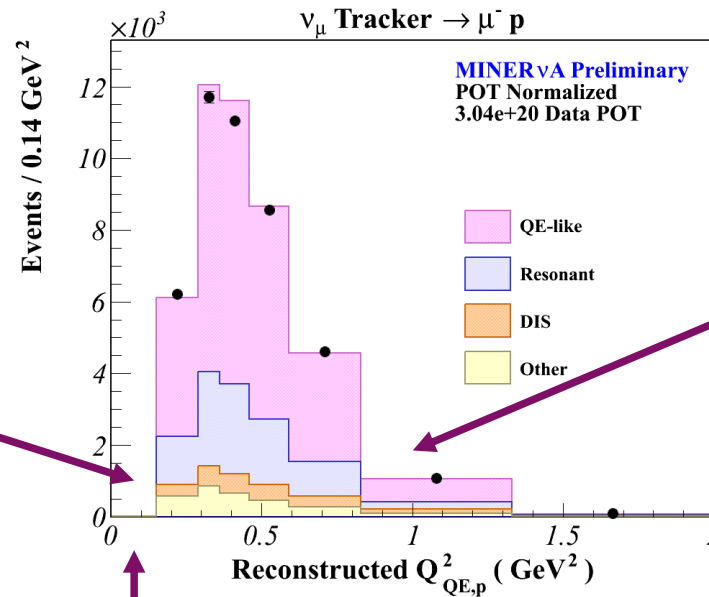
- ◆ For QE scattering from a stationary neutron  $\varphi$  should be  $180^\circ$
- ◆ Fermi motion, FSI and QE-like resonant events cause the spread in the distribution.



Data event distribution tends to lower co-planarity angle due to un-modeled FSI, or nuclear correlation effects?

# What initial interactions comes out of the nucleus a QE-like event – according to GENIE!

Data Candidates = 40,102



Resonant Production with a pion in the final state dominant background.

Requiring the hadron to resemble a ranging out proton → drop in the efficiency.

Tracking threshold prevents the reconstruction of events in the first bin.

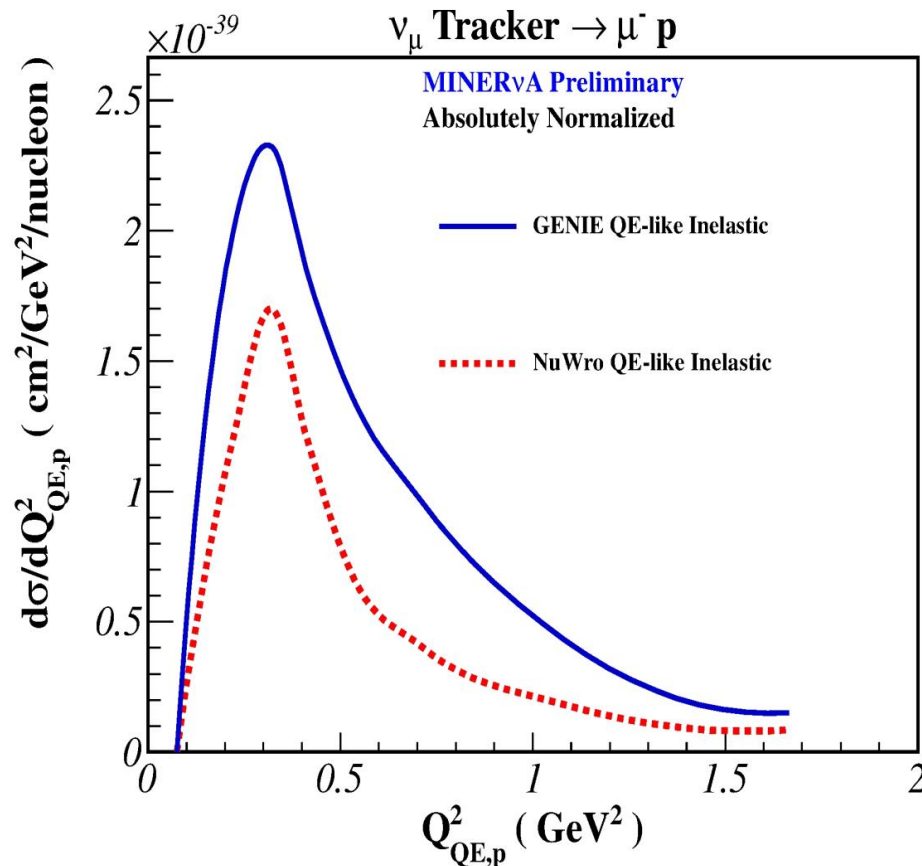
The QE-like signal is predicted to consists of:

**QE = 72.3 %**

**Res = 23.9%**

**DIS = 3.8%**

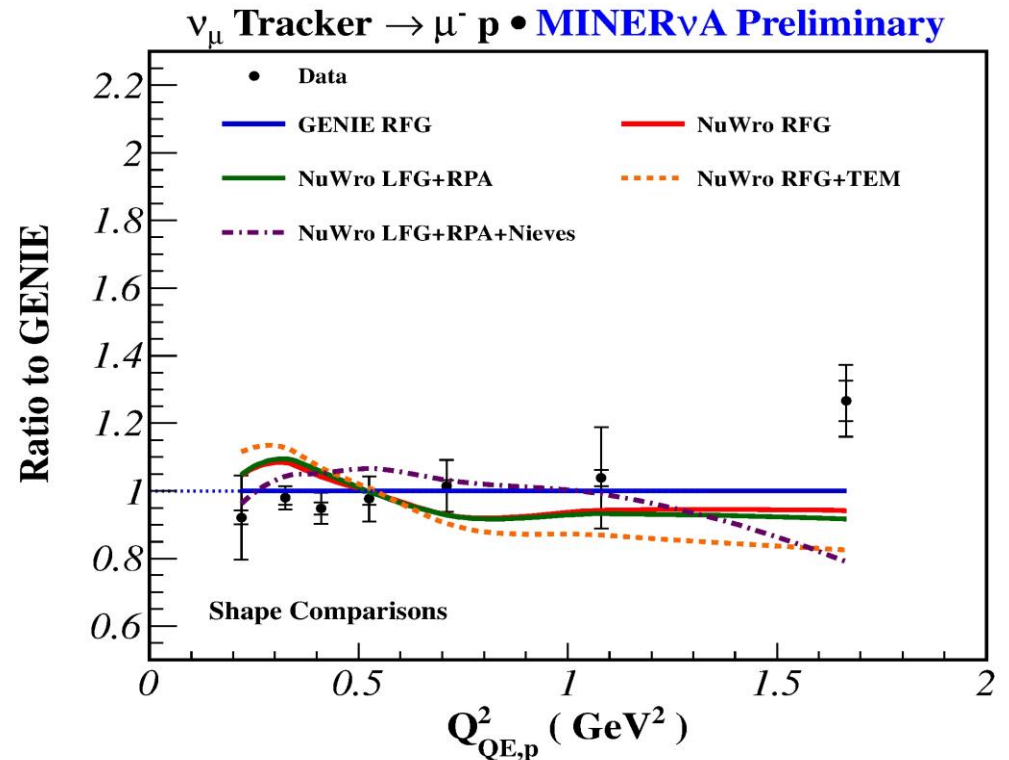
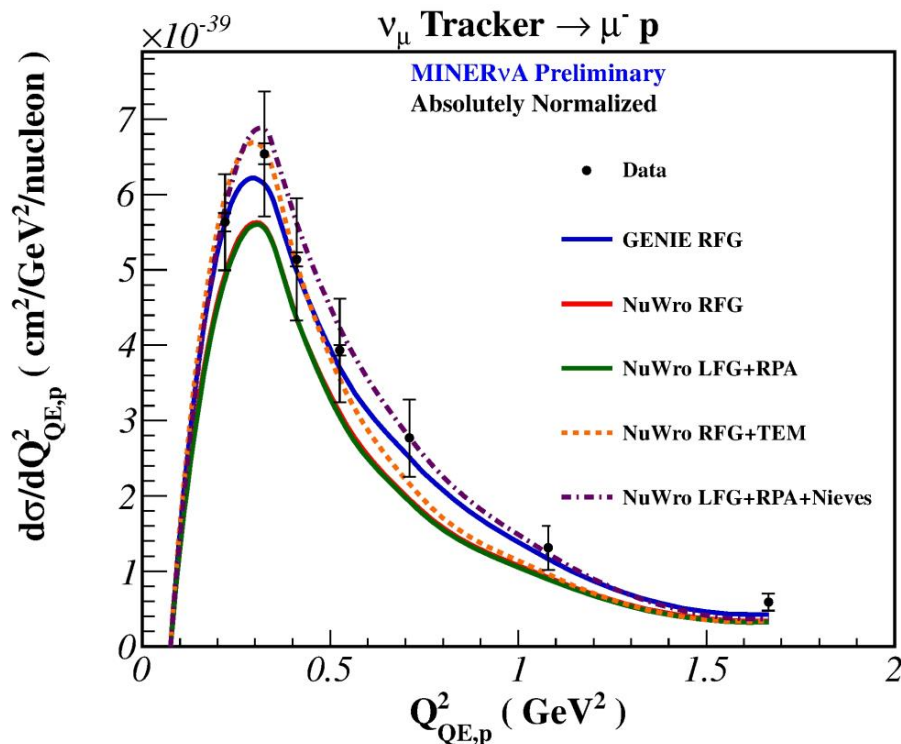
# QE-like background



- ◆ The major background to true QE events comes from inelastic produced events detected as QE-like.
- ◆ Observe the difference in this inelastic contribution from the NuWro vs GENIE generators!
- ◆ Difference in both magnitude and shape coming from modeling of the production cross sections and final state interactions!
- ◆ **Reduce GENIE resonance production by 30%!**
- ◆ **Big differences expected between  $\nu$  and  $\bar{\nu}$  !!**

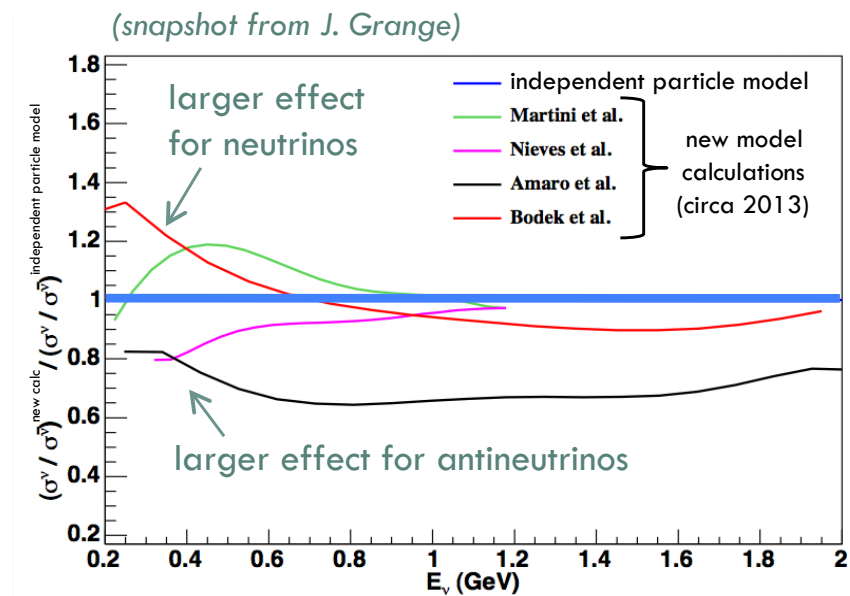
# Quasi Elastic from the Hadron Vertex

$$Q_{QE,p}^2 = (M')^2 - M_p^2 + 2M'(T_p + M_p - M')$$



- ◆ Quasi-elastic analysis from the hadron vertex (proton) favors the straightforward GENIE RFG model.
- ◆ **This in contrast to the RFG + transverse enhanced model for the analysis from the single muon anlysis - inconsistent.**

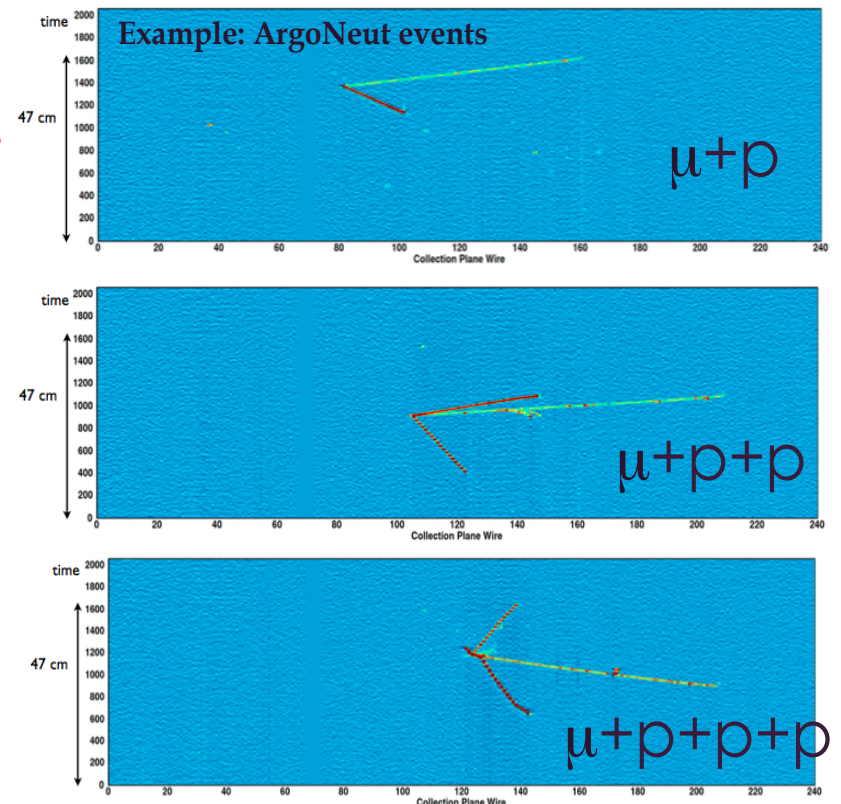
# $\nu$ to $\bar{\nu}$ QE Ratio: Essential for $\cancel{CP}$ studies



- ◆ Major differences in the initial ratio of  $\nu$  to  $\bar{\nu}$  mainly due to different treatments of the axial-vector contribution.
- ◆ On top of this comes the many differences of nuclear effects that determine the detected final state topology and energy.
- ◆ Consider the large contamination of  $\nu$  in the  $\bar{\nu}$  beam and the need for charge of lepton.
- ◆ A challenge for oscillation experiments measuring  $\cancel{CP}$

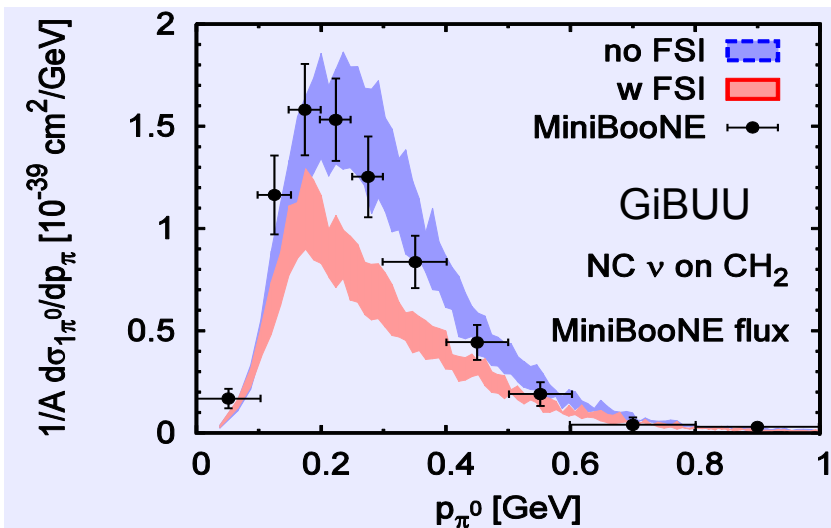
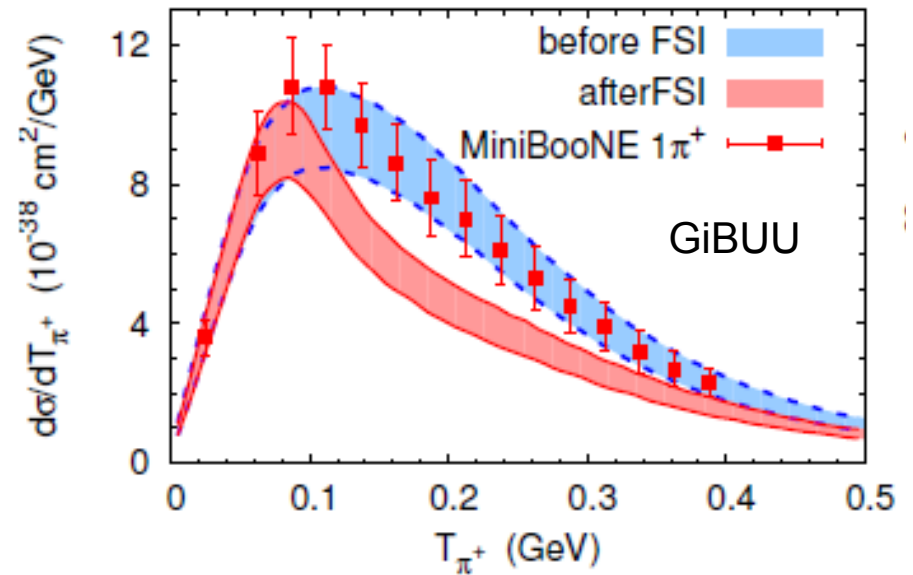
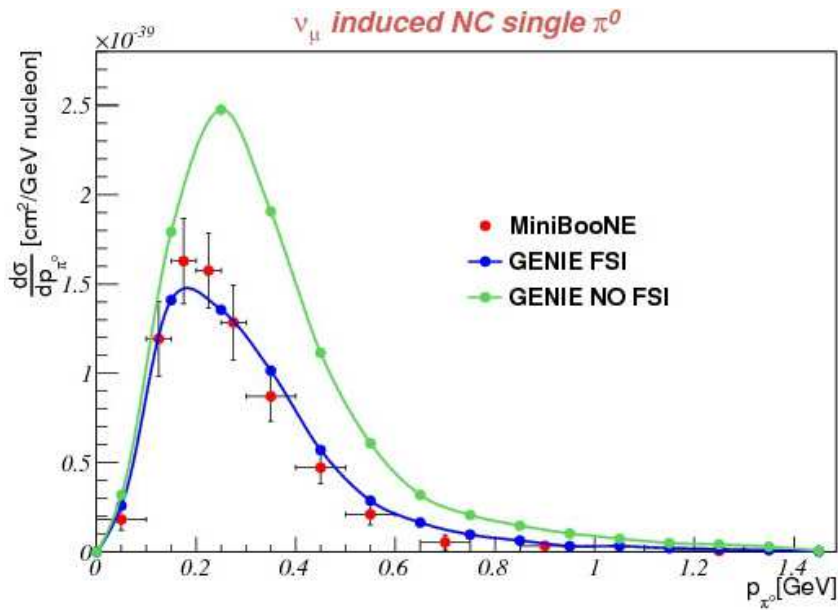
# Conclusions: QE-like Scattering off a Nucleus

- ◆ Best model fitting single  $\mu$  QE-like events includes parameterization of N-N correlation effect from e-A scattering (**Vector Current Only**)
- ◆ Best model fitting single  $\mu$  QE-like events is NOT best for  $\mu + p$  !  
Problem with FSI model?
- ◆ **NO SINGLE MODEL FITS MINIBOONE, MINERVA SINGLE  $\mu$  AND  $\mu + p$  DATA.**
- ◆ **Large** variation in predicted ratio of  $\nu$  to  $\bar{\nu}$  cross section ratio.
- ◆ Evidence for nucleon-nucleon correlations from both MiniBooNE and MINERVA
- ◆ Waiting for LAr TPC results!



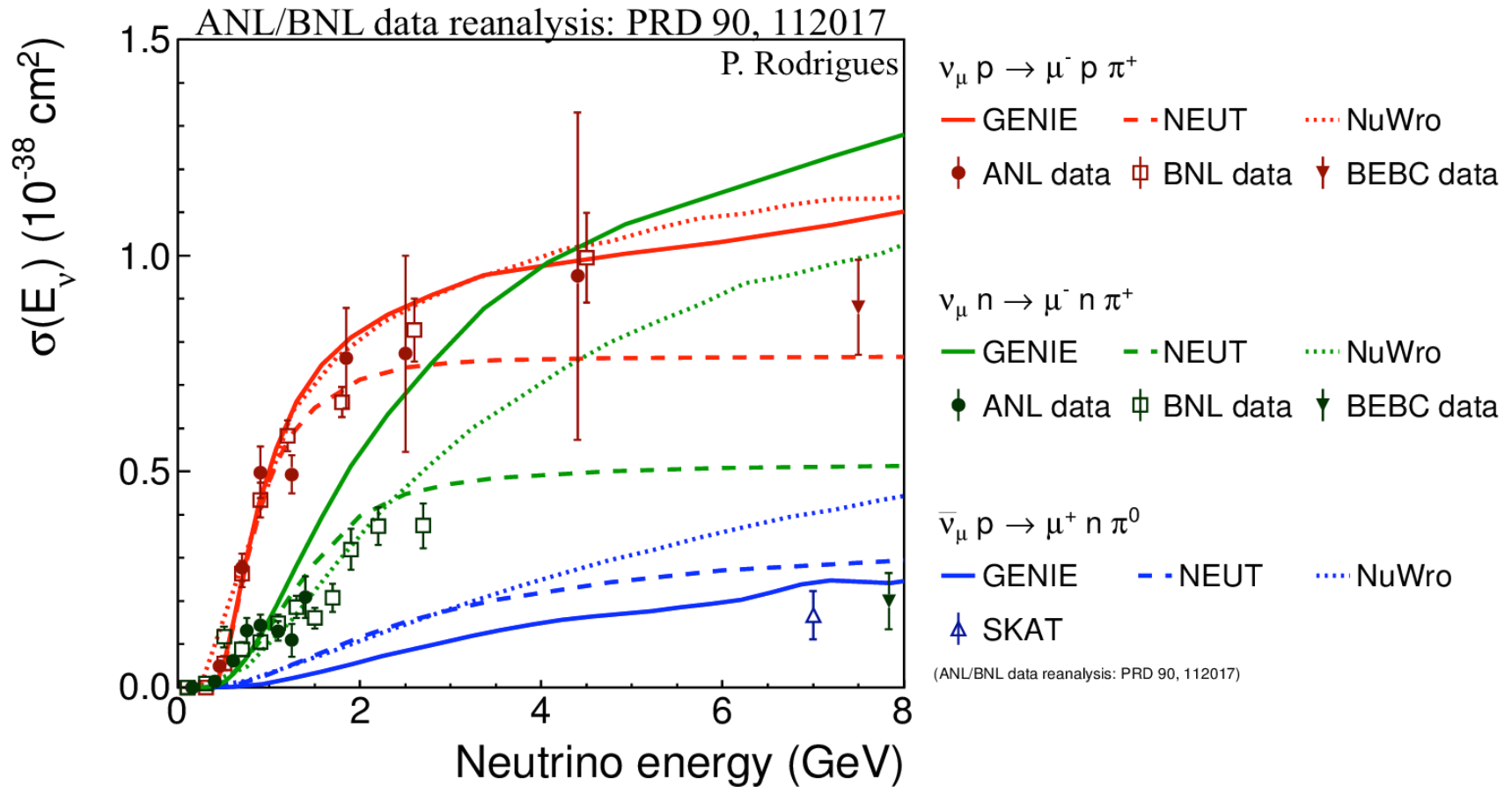
# A step up in W to pion production

## Comparison of $\pi^0$ and $\pi^\pm$ Models with Data





# What About $\nu$ **Nucleon** $\rightarrow \pi$ Cross Sections?



- ◆ However a recent study by Sato suggests that nuclear effects in deuterium have to be carefully considered.

# Move up in Hadronic Mass

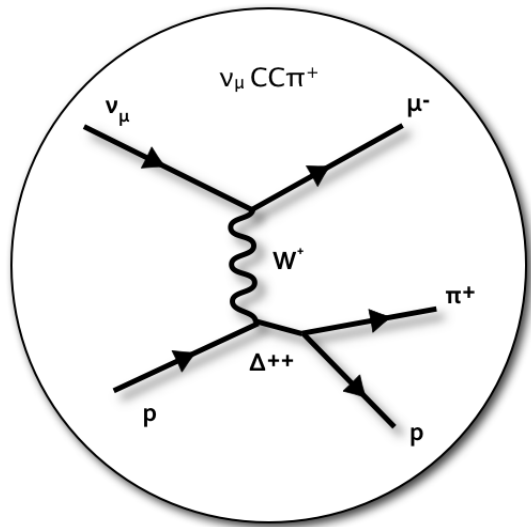
## .MINERvA: Charged and Neutral Pion Analyses

### Neutrino

Single charged pion production

$$\nu_{\mu} + CH \rightarrow \mu^{-} (1\pi^{\pm}) X$$

$X$  can contain any number of  $\pi^0$ s,  
no charged pions

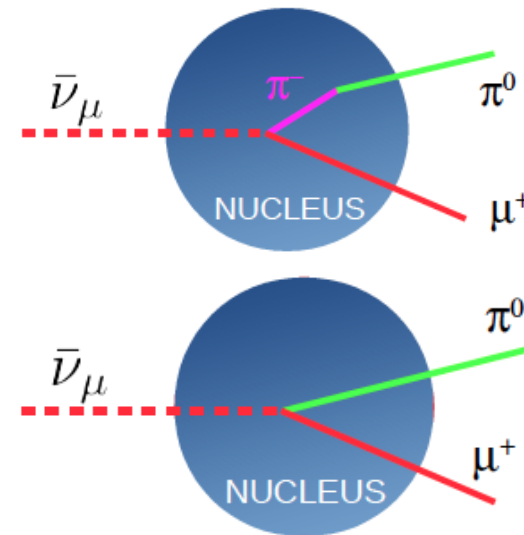


### Antineutrino

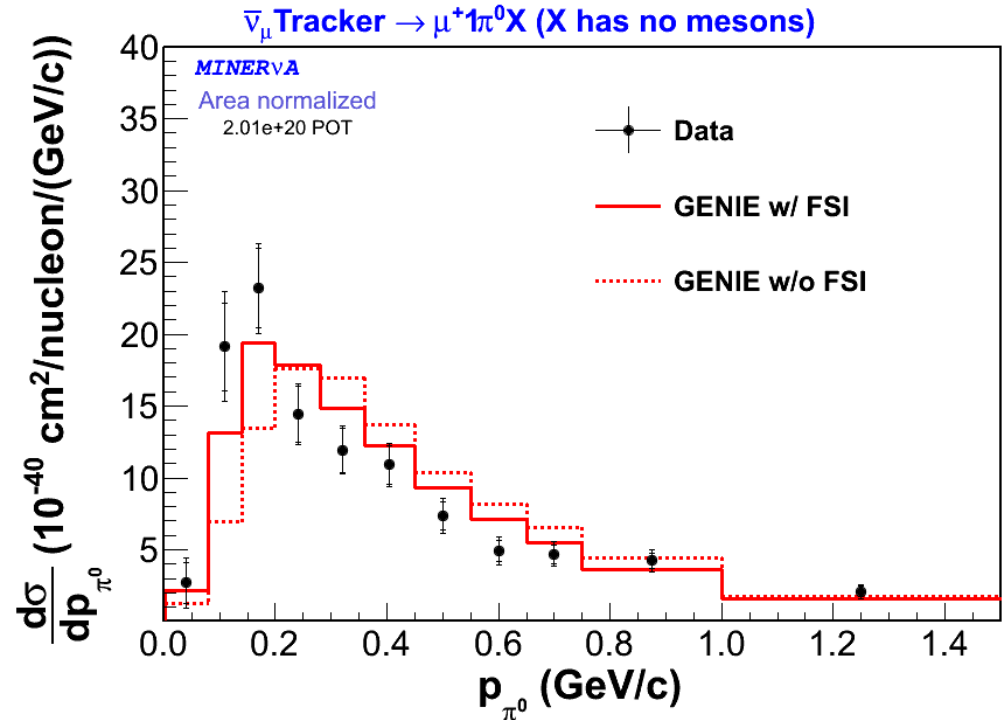
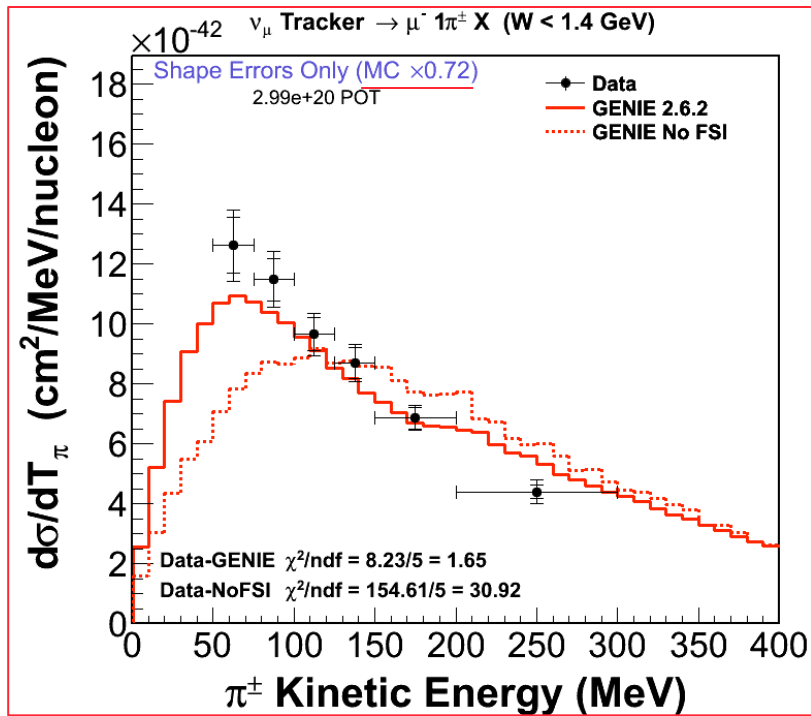
Single neutral pion production

$$\bar{\nu}_{\mu} + CH \rightarrow \mu^{+} (1\pi^0) X$$

$X$  contains no mesons



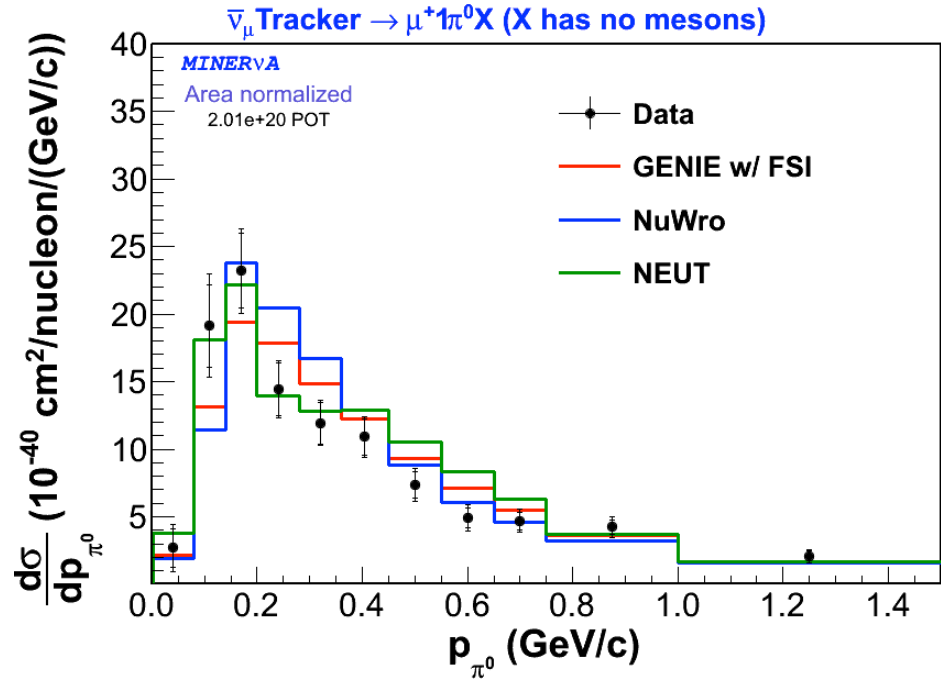
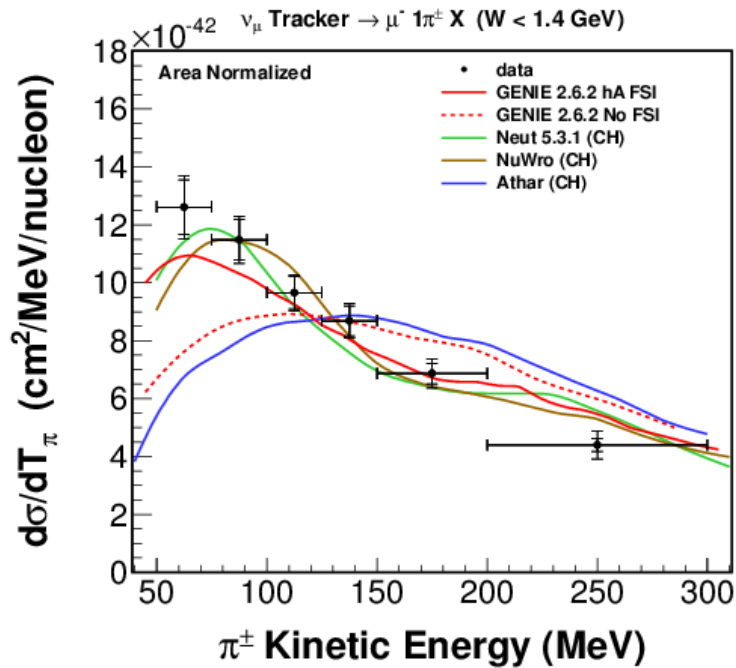
# FSI Conclusions for Pion Energy (Shape Comparisons)



- ◆ Data prefer GENIE with FSI

# FSI Conclusions for Pion Energy

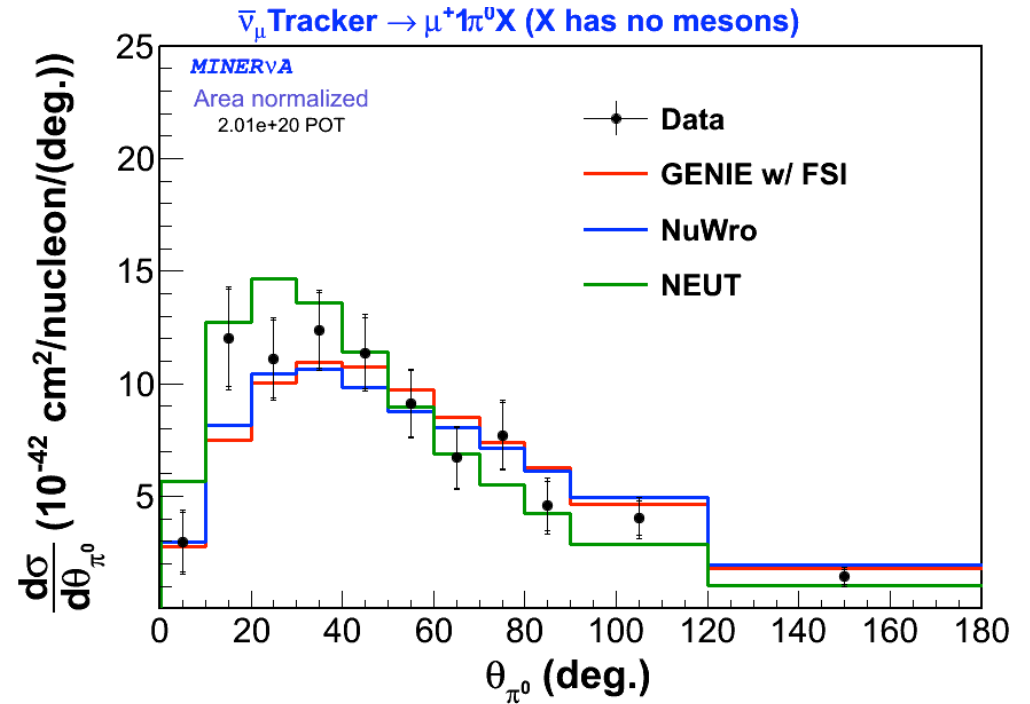
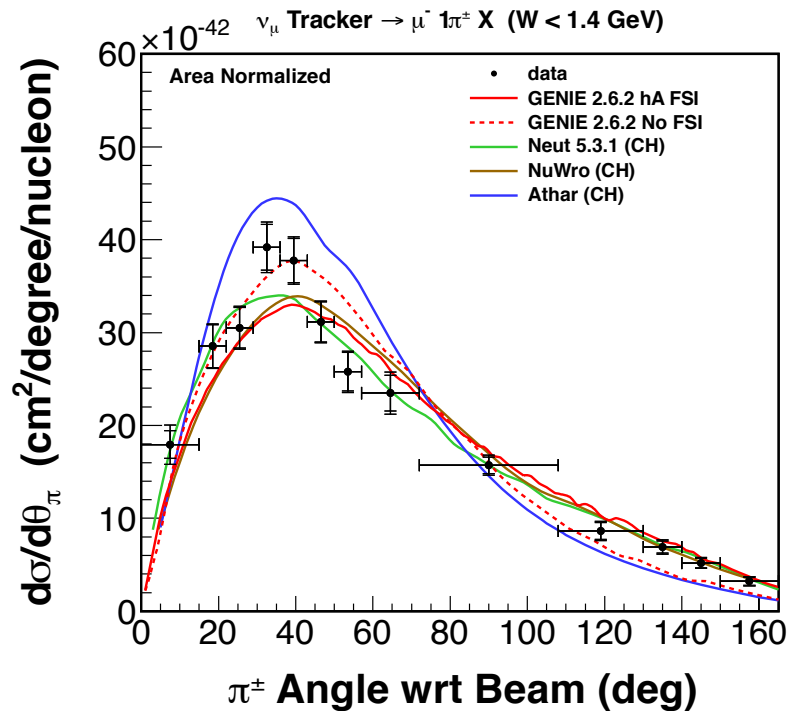
## (Multi model - Shape Comparisons)



- ◆ GENIE (with FSI), NEUT, and NuWro predict the data shape well
- ◆ Data is unable to distinguish different FSI models

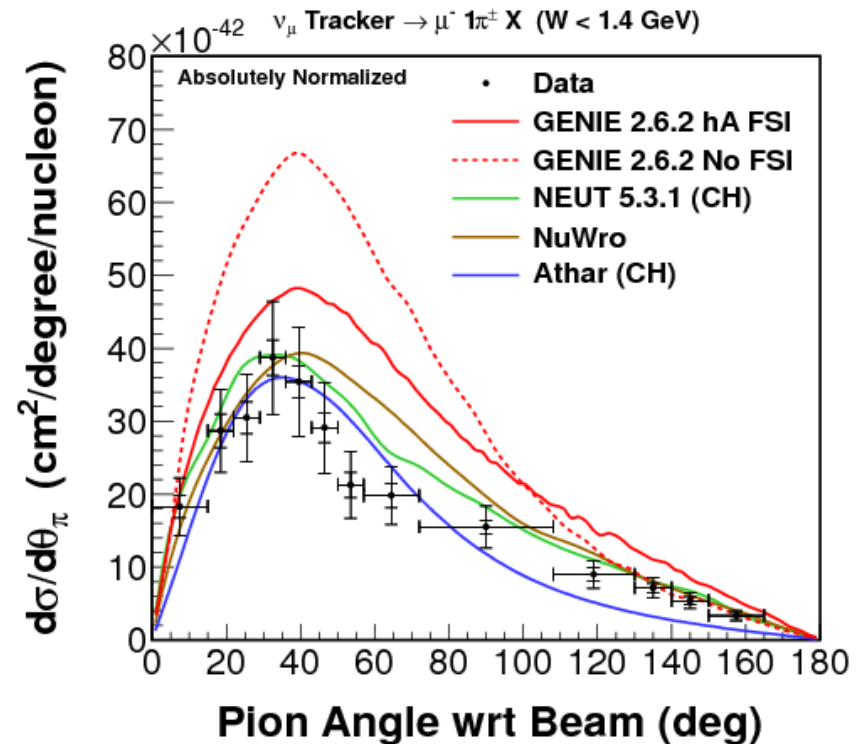
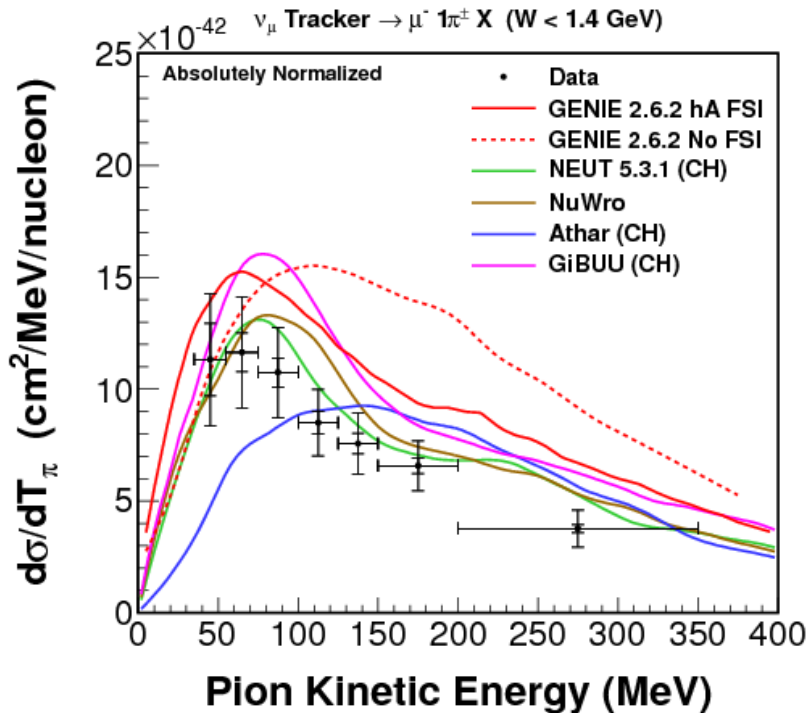
# FSI Conclusions for Pion Angle

## (Multi model - Shape Comparisons)



- ◆ GENIE (with FSI), NEUT, and NuWro predict the data shape well
- ◆ Again, data is unable to distinguish different FSI models

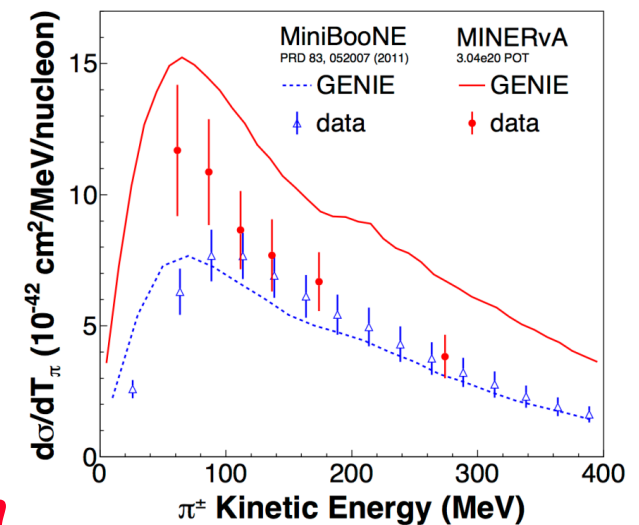
# More details: charged pion ( $W < 1.4$ GeV) absolute cross section – model comparisons



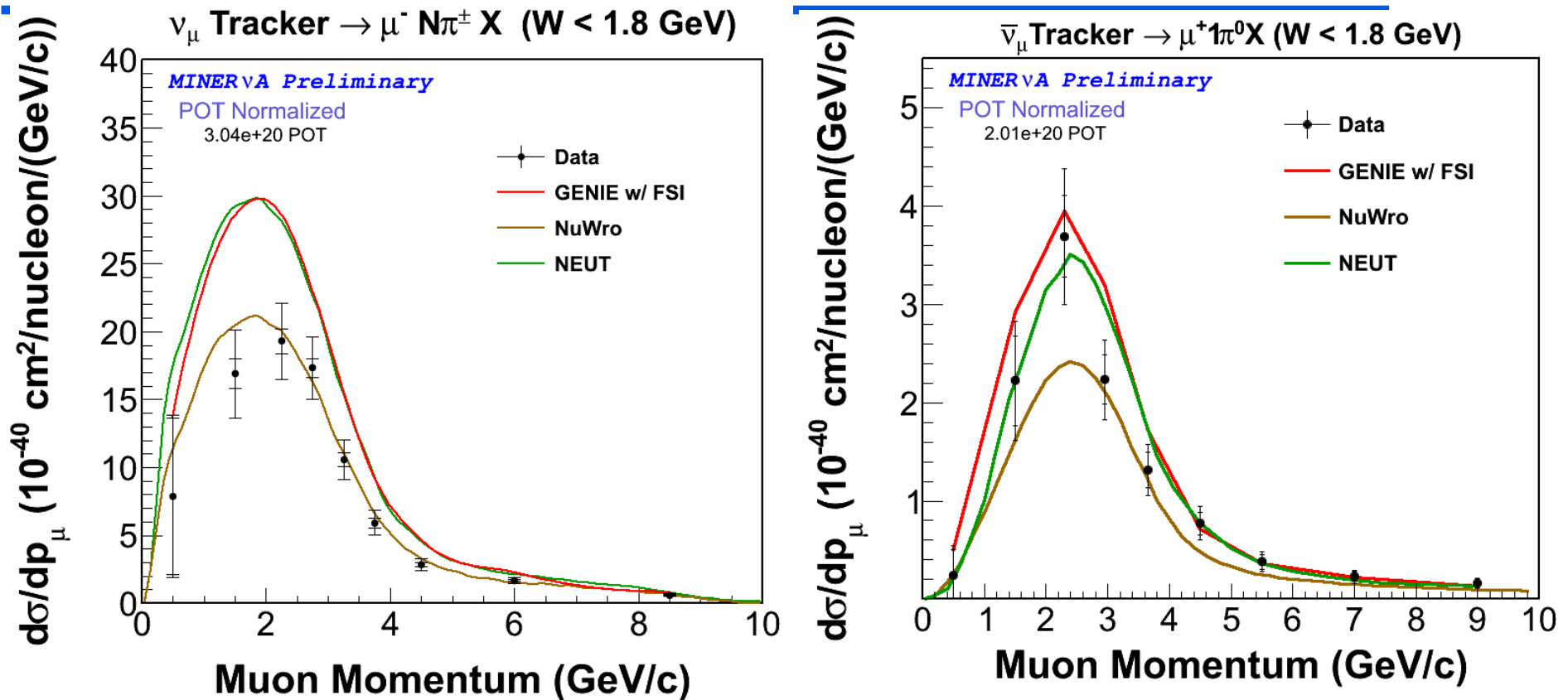
- NEUT and NuWro normalization agree the best with data.
- GiBUU, GENIE normalizations disfavored by a couple  $\sigma$
- GENIE (with FSI), NEUT, and NuWro predict the data shape well
- Except for Athar, data is unable to distinguish different FSI models

# Summary for $W < 1.4$ GeV Analysis

- ◆ MiniBooNE -  $E_\nu \sim 1$  GeV
  - ▼ Best theory models (GiBUU, Valencia) strongly disagree in shape
  - ▼ Event generators have shape right, but problems in detail
- ◆ MINERvA -  $\langle E_\nu \rangle = 4$  GeV
  - ▼ Dominantly  $\Delta$  resonance formation, decay in nucleus, very similar to MiniBooNE)
  - ▼ Event generators have shape but not magnitude
  - ▼ Event generators show the absolute need for
  - ▼ GiBUU has shape right, but wrong magnitude
- ◆ **No models describes all data sets well!**
  - ▼ Theory based calculations have better physics (nuclear corrections), but don't describe data better than simpler event generator codes.



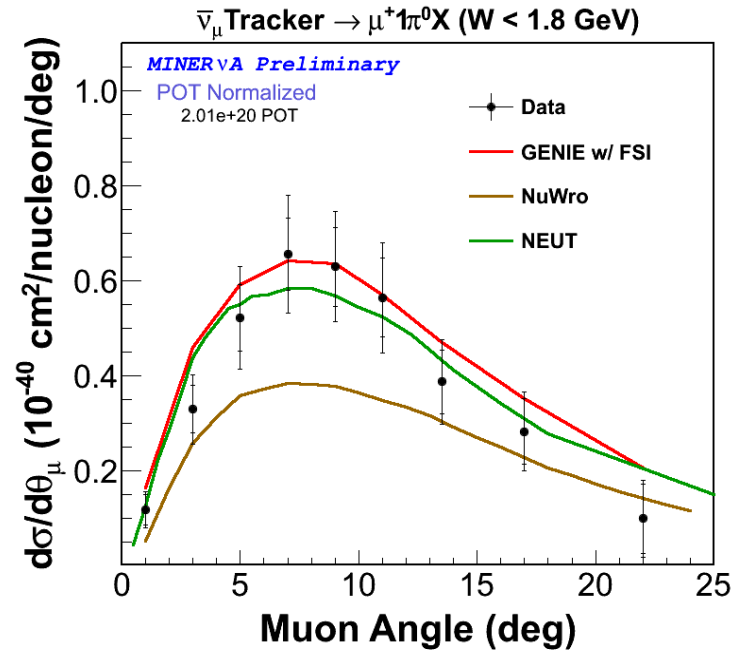
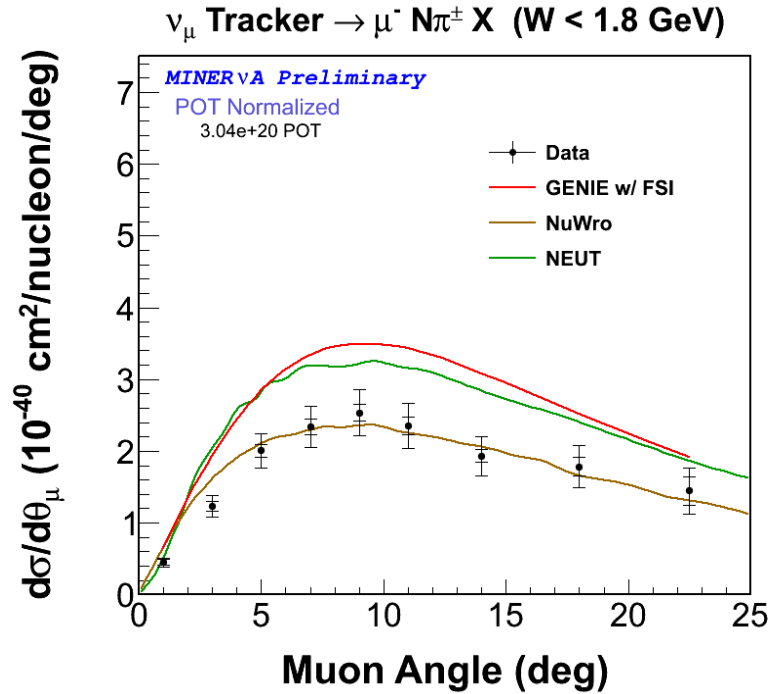
Up into the multi- $\pi$  zone ( $W < 1.8$  GeV) from the lepton side:  
 Cross section model comparisons for  $\mu$  momentum



- ◆ In charged pion both GENIE and NEUT overestimate the cross section
- ◆ GENIE and NEUT predictions are similar and are higher than NuWro in both analyses

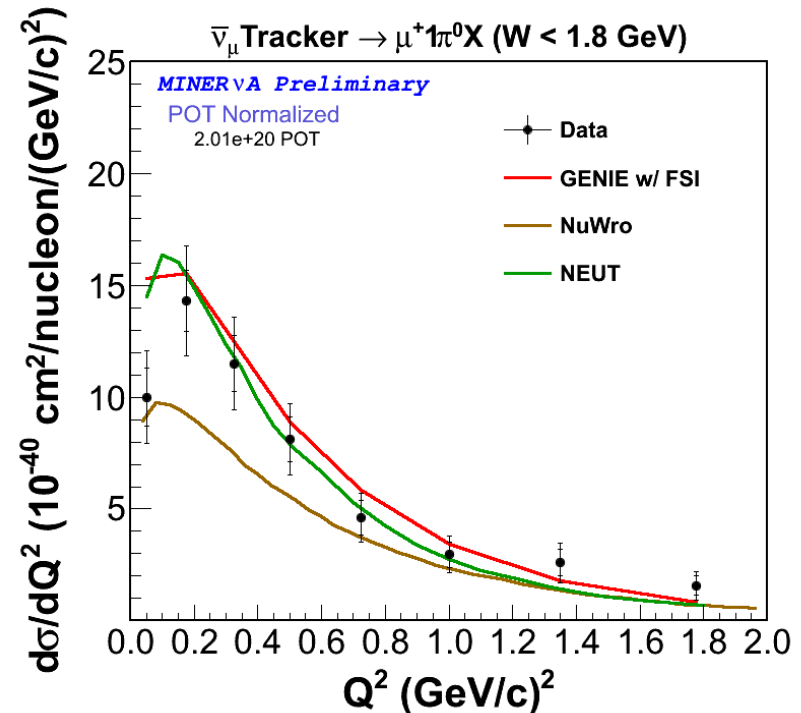
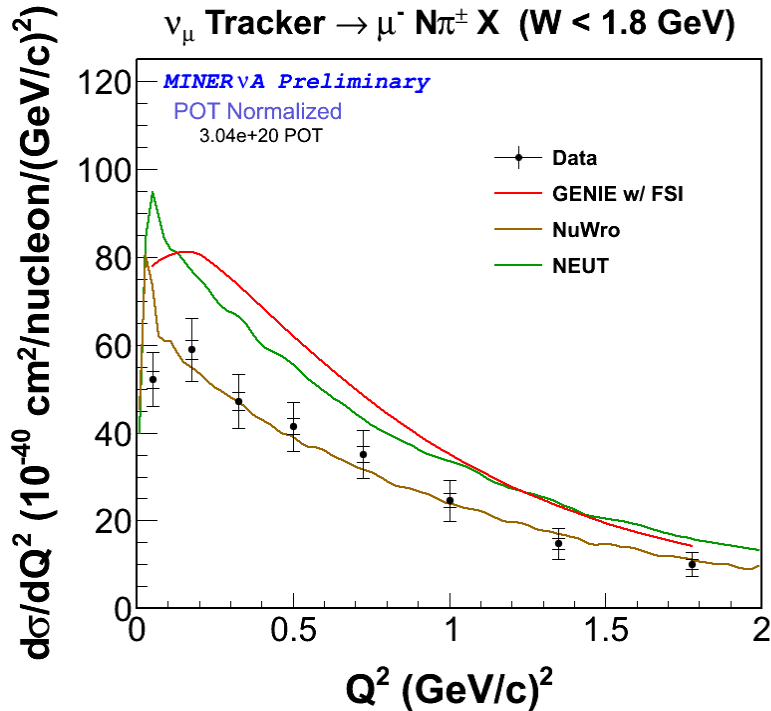


# Up into the multi- $\pi$ zone ( $W < 1.8$ GeV) from the lepton side: Cross section model comparisons for $\mu$ angle



- ◆ The same normalization and shape behavior as with the  $\mu$  momentum

# Up into the multi- $\pi$ zone ( $W < 1.8$ GeV) from the lepton side: Cross section model comparisons for $Q^2$



- ◆ In charged pion both GENIE and NEUT over estimate the cross section (as in the muon variables)
- ◆ In the shape analysis, GENIE agrees well with data except in lowest  $Q^2$  bin of the neutral pions.
- ◆ In lowest  $Q^2$  bin of the charged pions, coherent production in NuWro & NEUT

## Conclusions the multi- $\pi$ zone ( $W < 1.8$ GeV)

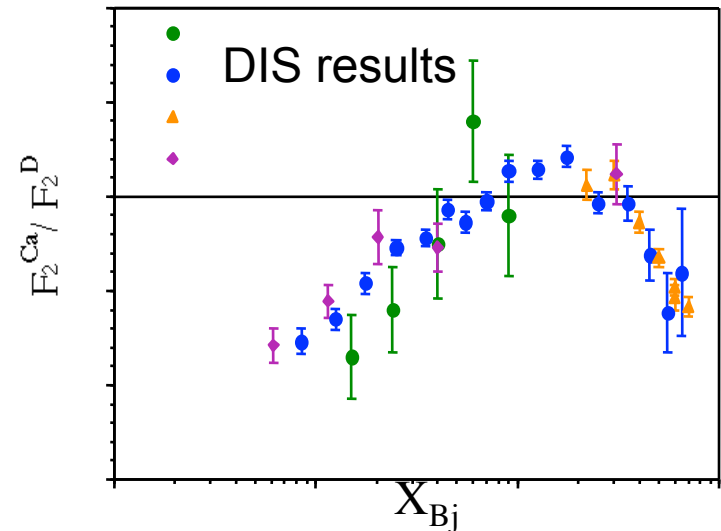
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- ◆ Distributions of the muon observables ( $p_\mu, \theta_\mu, E_\nu, Q^2$ ) are sensitive to nuclear structure.
- ◆ They are complementary to pion variables ( $T_\pi, \theta_\pi$ ), which are sensitive to FSI.
- ◆ The  $Q^2$  spectrum provides the most detail and no single model describes both the  $\pi^+$  and  $\pi^0$  distributions.
- ◆ **Once again we see experimental evidence pointing toward the need of improved nuclear models!**

# Inclusive Nuclear Target Cross section Ratios

Minimal contribution from DIS

- ◆ MINERvA nuclear targets of C (166 Kg), Fe (653 kg) and Pb (750 Kg)
- ◆ We are used to seeing ratios like at right.
- ◆ This has been measured for **DIS events**

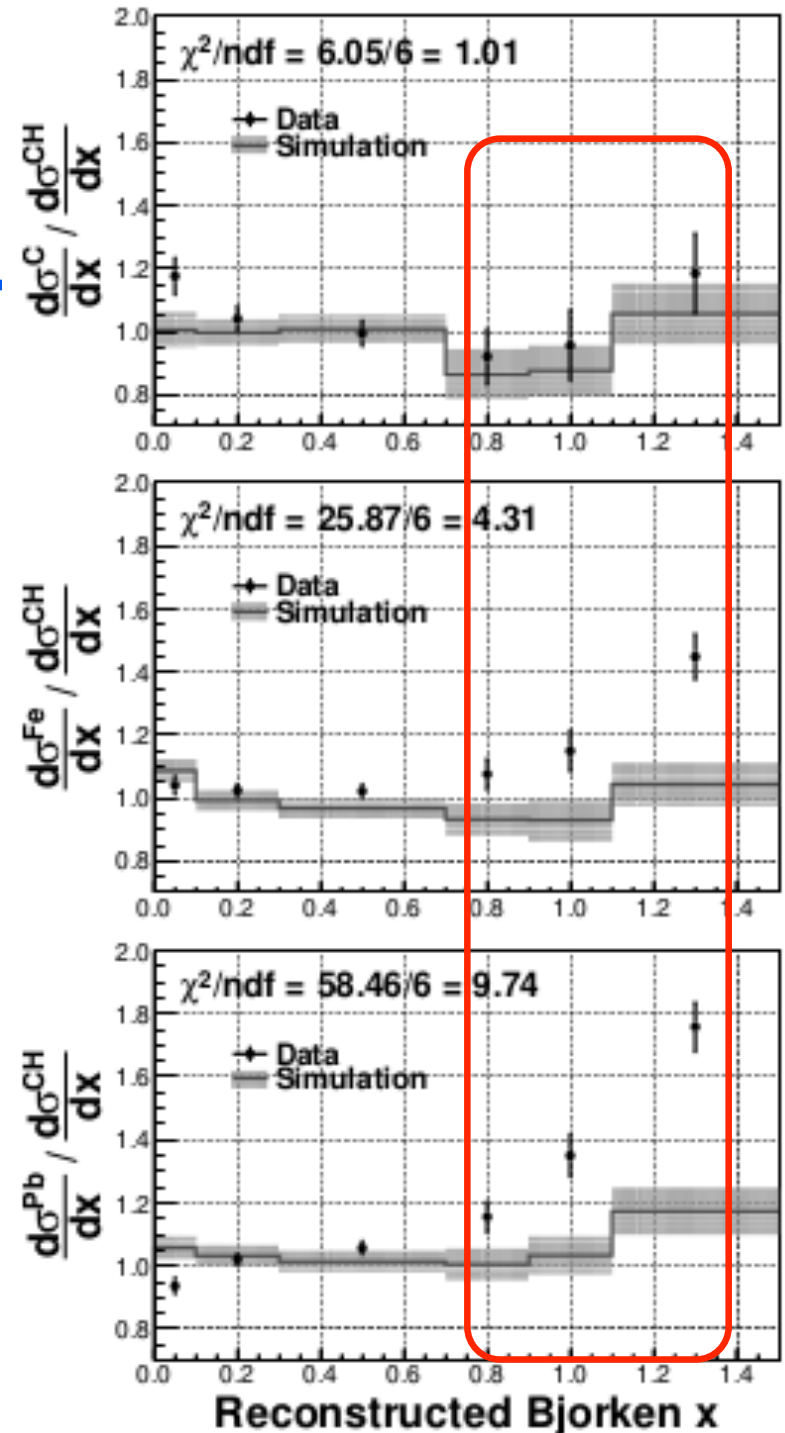


Reconstructed $x$ MINERvA	QE (%)	Res (%)	DIS = lowQ DIS (%)	Con (%)	Mean Generated $Q^2$ (GeV <sup>2</sup> )	
0.0–0.1	11.3	42.5	5.9	19.2	15.7	0.23
0.1–0.3	13.6	36.4	16.7	9.1	23.0	0.70
0.3–0.7	32.7	32.8	11.8	1.4	21.1	1.00
0.7–0.9	55.1	25.4	4.3	0.5	14.6	0.95
0.9–1.1	62.7	21.6	2.8	0.5	12.3	0.90
1.1–1.5	69.6	18.1	1.9	0.4	9.9	0.82
> 1.5	79.1	12.8	0.6	0.3	7.1	0.86

# High x summary INCLUSIVE RATIOS

- ◆ At  $x = [0.7, 1.1]$ , we observe an **excess** that grows with the size of the nucleus
- ◆ This effect is not modeled in the GENIE simulation.

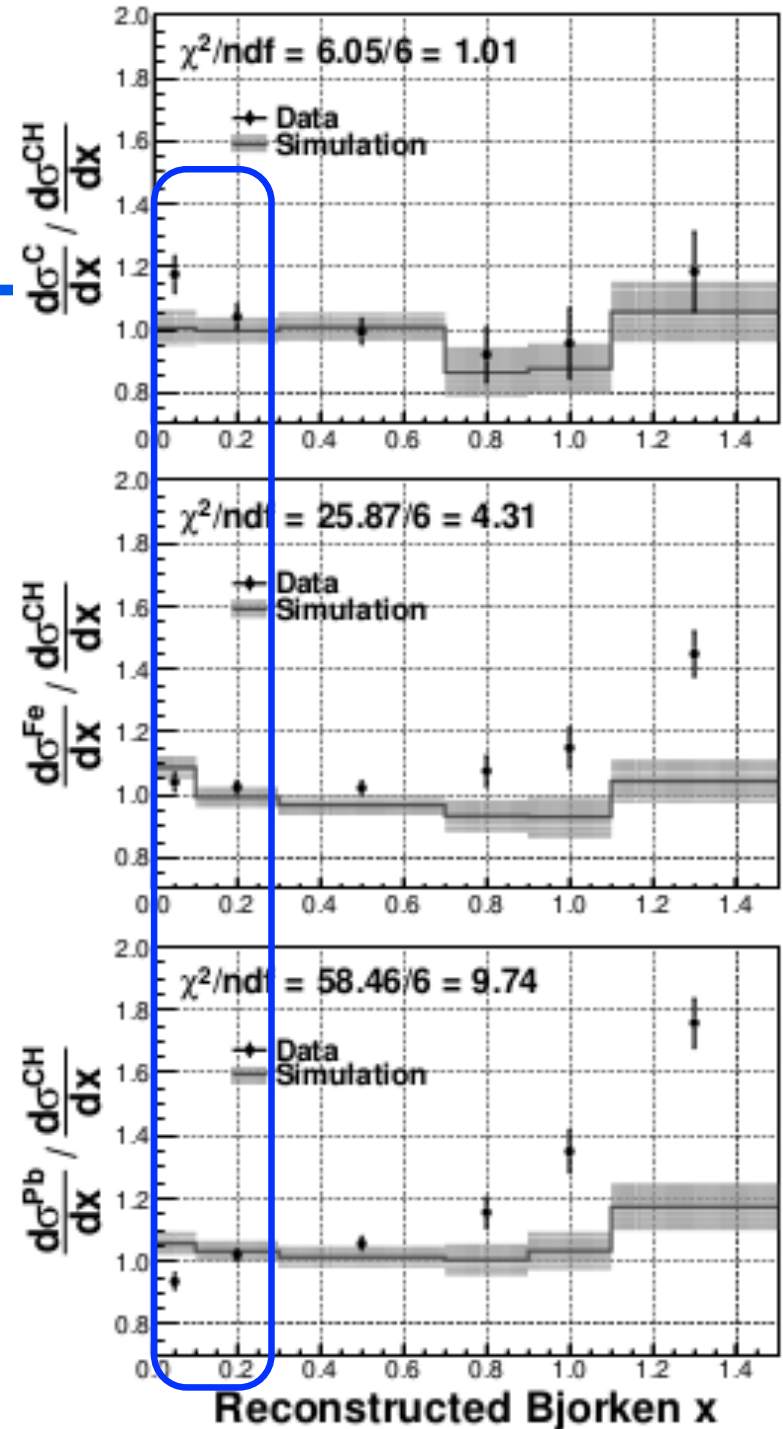
$x_{bj}$	QE	DIS	OTHER
0.0 – 0.1	11.3%	5.9%	77.4%
0.1 – 0.3	13.6%	16.7%	68.5%
0.3 – 0.7	32.7%	11.8%	55.3%
0.7 – 0.9	55.1%	4.3%	40.5%
0.9 – 1.1	62.7%	2.8%	34.4%
1.1 – 1.5	69.9%	1.9%	28.4%
> 1.5	79.1%	0.6%	20.2%



# Low x summary INCLUSIVE RATIOS

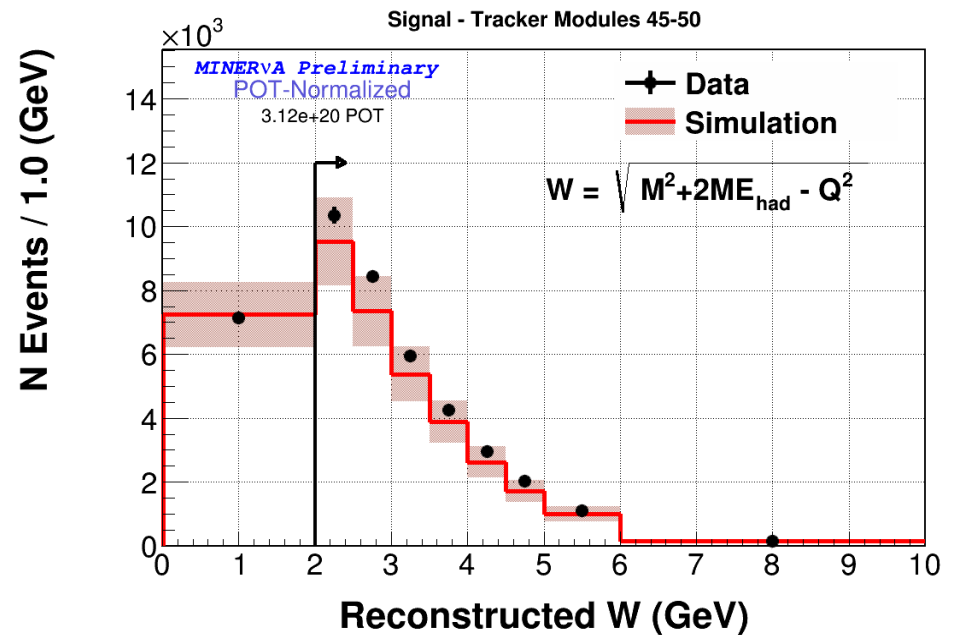
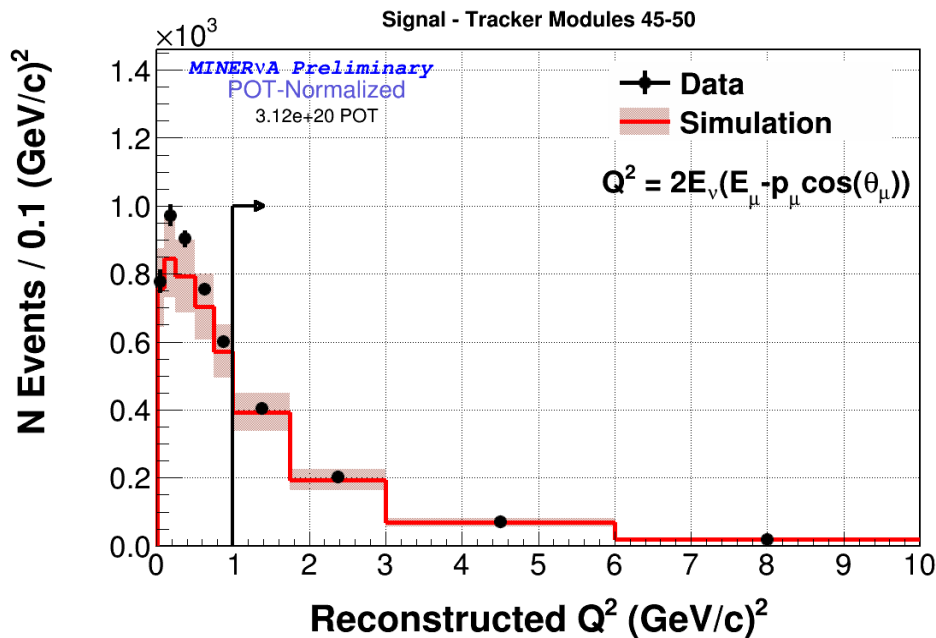
- ◆ At  $x = [0.0, 0.1]$ , we observe a **deficit** that increases with the size of the nucleus. This effect is not modeled in the simulation.
- ◆ Expected Neutrino Differences in shadowing
  - ▼ Neutrino sensitive to  $xF_3$ .
  - ▼ Axial-vector current has a different coherence length.

$x_{bj}$	QE	DIS	OTHER
0.0 – 0.1	11.3%	5.9%	77.4%
0.1 – 0.3	13.6%	16.7%	68.5%
0.3 – 0.7	32.7%	11.8%	55.3%
0.7 – 0.9	55.1%	4.3%	40.5%
0.9 – 1.1	62.7%	2.8%	34.4%
1.1 – 1.5	69.9%	1.9%	28.4%
> 1.5	79.1%	0.6%	20.2%

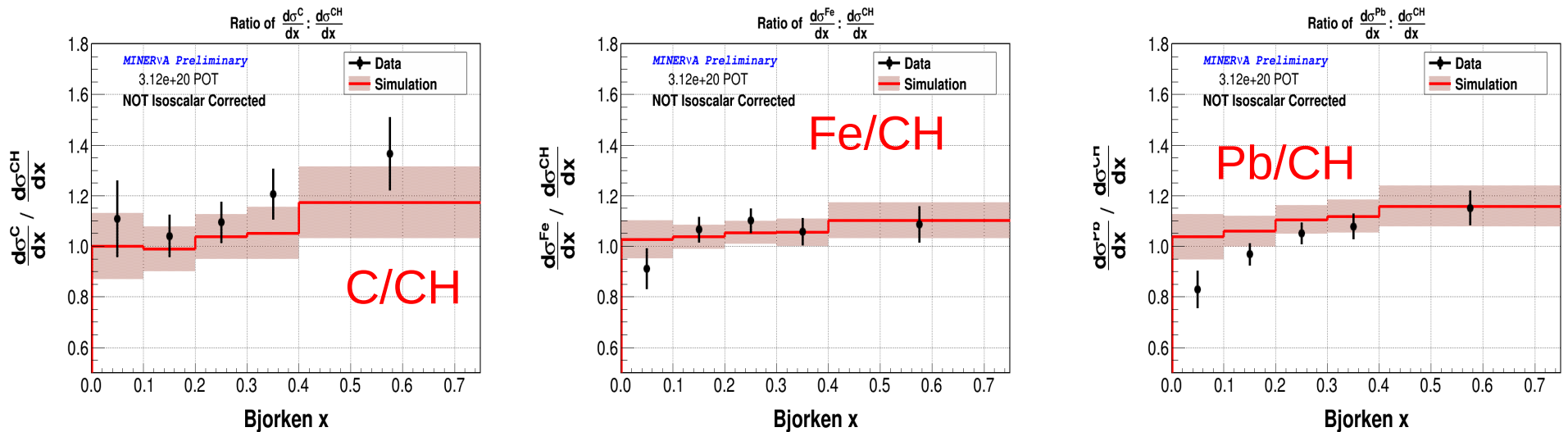


# MINERvA Nuclear DIS Cross Section Ratios

- ◆ Require  $Q^2 > 1.0 \text{ (GeV / c)}^2$  and  $W > 2.0 \text{ GeV}$ .
- ◆ Cuts are illustrated for CH events between 5 and 50 GeV  $E_\nu$  and  $\theta_\mu < 17^\circ$



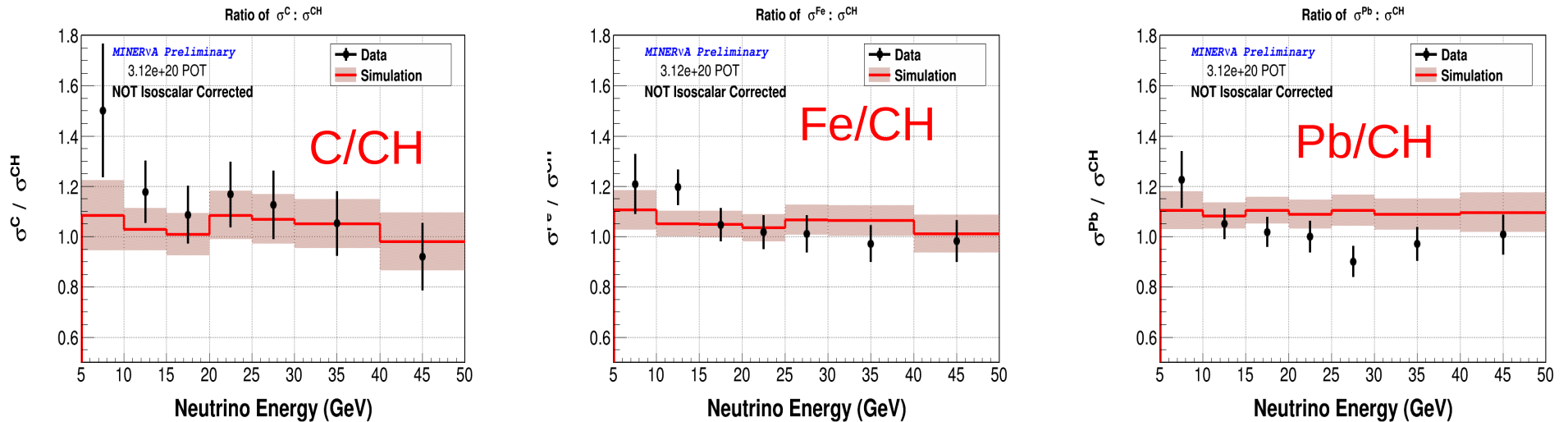
# MINERvA Nuclear DIS Cross Section Ratios



- ◆ Our data suggest additional nuclear shadowing in the lowest x bin ( $0 < x < 0.1$ ) than predicted in lead with a hint also in iron.
- ◆ Lowest x bin is at  $\langle x \rangle \sim 0.07$  and  $\langle Q^2 \rangle \sim 2.0$  (GeV/c)<sup>2</sup>
- ◆ At this x and Q<sup>2</sup>, shadowing is not expected in Pb with the vector current.



# MINERvA Nuclear DIS Cross Section Ratios



- ◆ The measured ratios – in 5 GeV bins(!) - do not demonstrate big deviations from the simulation for C and Fe.
- ◆ The data points falling below the simulation in Pb at higher energies could be mainly a reflection of the larger low-x shadowing seen in the x distributions.

# First Conclusions

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- ◆ Need to move away from the simple IA models of the nucleus used in most even generators.
- ◆ Need to develop a model of neutrino nucleus interactions that is not a patchwork of individual thoughts that are difficult/impossible to combine in a smooth continuous and correct whole.
- ◆ The model has to work for nuclei from C to Ar to Fe and for energies from sub-to-multi-GeV. **NP-HEP Collaborations!**
- ◆ Need highly accurate neutrino nucleus scattering measurements to constrain the nuclear model. **NP-HEP Collaborations!**
- ◆ We may have the detector (LAr TST) (but lost the beam with nuSTORM)

# In Summary: Nuclear Physics Meets Neutrino Physics

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**No single nuclear model comes close to fitting all of the accumulated data.**

**However, it is not a knockout – we are simply “on the ropes” and need collaboration with the nuclear physics community.**

# NuSTEC

## A Collaboration of HEP and Nuclear Experimentalists and Theorists Studying Low-energy Neutrino Nucleus Scattering Physics

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### GOALS:

- ◆ **Coordinate NP (theorist) - HEP experimentalist collaborative efforts:**
  - ▼ Coordinate theorist-experimentalist collaborative efforts to improve generators
  - ▼ Improve general understanding of the physics via enhanced theoretical background for experimentalists and ensuring theorists have the latest experimental data and correctly incorporated errors to test models.
- ◆ **Workshops:** Organize Community-wide Workshops when needed
  - ▼ Main Conference: The NuInt Neutrino Interaction Workshop (next, November 2015)
  - ▼ Organization beginning on workshop to investigate np-nh/MEC nuclear effects
- ◆ **Training Programs:** Organize and run training programs in:
  - ▼ Neutrino Scattering Event Generators: University of Liverpool, 14 – 16 May
  - ▼ Theory-oriented Neutrino-nucleus Scattering physics occurred at Fermilab in October.
- ◆ **Global Fits:** Combine results from multiple experiments to compare with and then, if necessary, modify a theory/model framework.
- ◆ **First meeting of the NuSTEC Board in September:** Representatives of each  $\nu$ -A experiment, each nuclear theory “school” and each  $\nu$  event generator

# Green's Function Monte Carlo Techniques

## Full description of initial state including N-N Correlations

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- ◆ Calculations have to expand in  $A$  up to argon in the higher energy kinematical regime relevant to current/future neutrino experiments.
- ◆ Additional effort required to incorporate these models into a neutrino nucleus event generators.
- ◆ **Example of NP – HEP Collaboration to face this challenge and expand GFMC techniques to larger nuclei and increased energy  $E$ . Then to incorporate results in the GENI Event Generator**

Project Title: Nuclear Theory for Neutrino-Nucleus Interactions

R. Schiavilla and J.W. Van Orden, Old Dominion University (ODU and TJNAF)

A. Lovato), S.C. Pieper, and R.B. Wiringa (ANL)

J. Carlson and S. Gandolfi (LANL)

T.W. Donnelly (MIT)

S.J. Brice, J.G. Morfín, G.N. Perdue, and G.P. Zeller (Fermilab)

S.A. Dytman (Pittsburgh)

H. Gallagher (Tufts)

# Further Coordinated Collaboration of NP-HEP The NuSTEC Concept

Neutrino Scattering Theorist Experimentalist Collaboration

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Nuclear Physics Meets  
Particle Physics



Theorists and  
Experimentalists

# Summary and Conclusions

- ◆ Nuclear effects, present in the data of all contemporary neutrino oscillation experiments, **mixes topologies and changes energy between produced and (detected) final states.**
- ◆ The precision with which neutrino properties can be extracted from oscillation experiments is clearly limited by the quality of the generator used.
- ◆ The neutrino generators used by experiments have grown historically into a collection of sometimes inconsistent nuclear physics recipes and still contain outdated physics modeling.
- ◆ The time has come to build a scientific community, based on NP-HEP collaboration, around the question of neutrino-nucleus interactions.
- ◆ BOTH communities will benefit from this collaboration.
- ◆ NuSTEC is in the process of becoming this NP-HEP collaboration.

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Backup



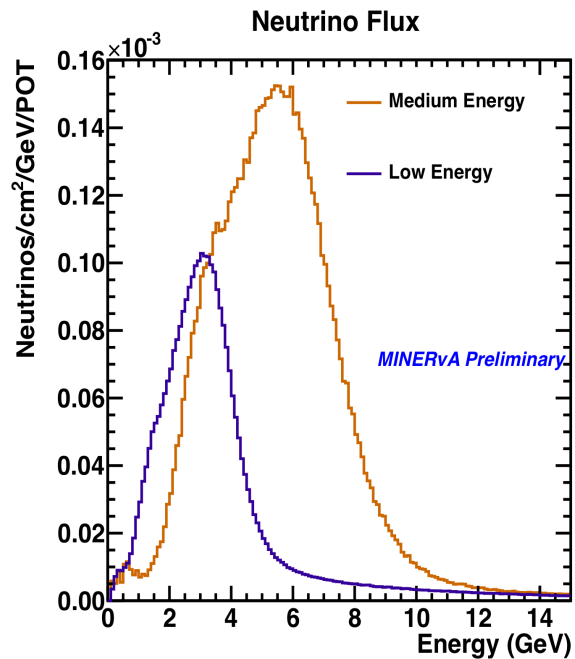
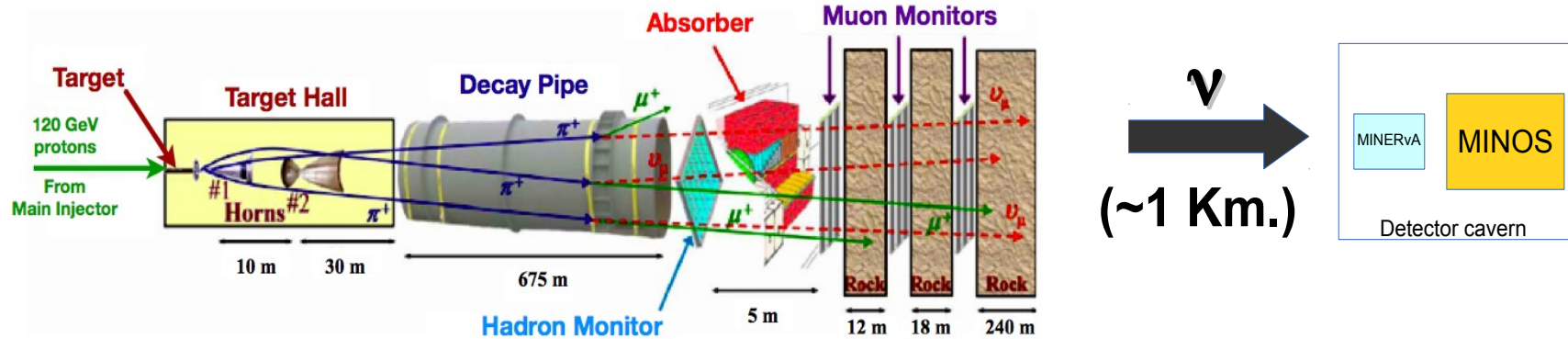
# NuSTEC Training in Neutrino Nucleus Scattering Physics

21 – 29 October 2014 with 85 International Students

<http://nustec2014.phys.vt.edu>

- 
- ◆ **Electroweak interactions on the nucleon (L. Alvarez-Ruso)** [lecture videos: [1,2,3](#)]
  - ◆ **Strong and electroweak interactions in nuclei (R. Schiavilla)** [lecture videos: [1, 2, 3, 4](#)]
  - ◆ **The nuclear physics of electron and neutrino scattering in nuclei in the quasi-elastic regime and beyond (T. W. Donnelly, J. Nieves and O. Benhar)**
    - ▼ Approximate methods for nuclei (I) (T. W. Donnelly) [lecture videos: [1,2,3](#)]
    - ▼ Approximate methods for nuclei (II) (J. Nieves) [lecture videos: [1, 2, 3](#)]
    - ▼ Ab initio methods for nuclei (O. Benhar) [lecture videos: [1, 2, 3](#)]
  - ◆ **Pion production (T. Sato)** [lecture videos: [1, 2, 3](#)]
  - ◆ **Description of exclusive channels and final state interactions (P. Danielewicz)** [lecture videos: [1, 2, 3](#)]
  - ◆ **Inclusive electron and neutrino scattering in the deep inelastic regime (J. Owens)** [lecture videos: [1, 2, 3](#)]
  - ◆ **Impact of uncertainties in neutrino cross-sections (P. Coloma and T. Dealtry)**
    - ▼ General analysis (P. Coloma) [lecture videos: [1, 2](#)]
    - ▼ The T2K analysis (T. Dealtry) [lecture video: [1](#)]
  - ◆ **Selected experimental illustrations (K. Mahn, C. Mauger and M. Soderberg)**
    - ▼ Fine-grained Sampling detector (C. Mauger) [lecture videos: [1, 2](#)]:
    - ▼ LAr detectors (M. Soderberg) [lecture videos: [1, 2](#)]
    - ▼ Cerenkov vs. fine-grained measurement techniques (K. Mahn) [lecture video: [1](#)]

# Brief Summary of Determining $\Phi(E)$ , the Neutrino Flux: NuMI Example

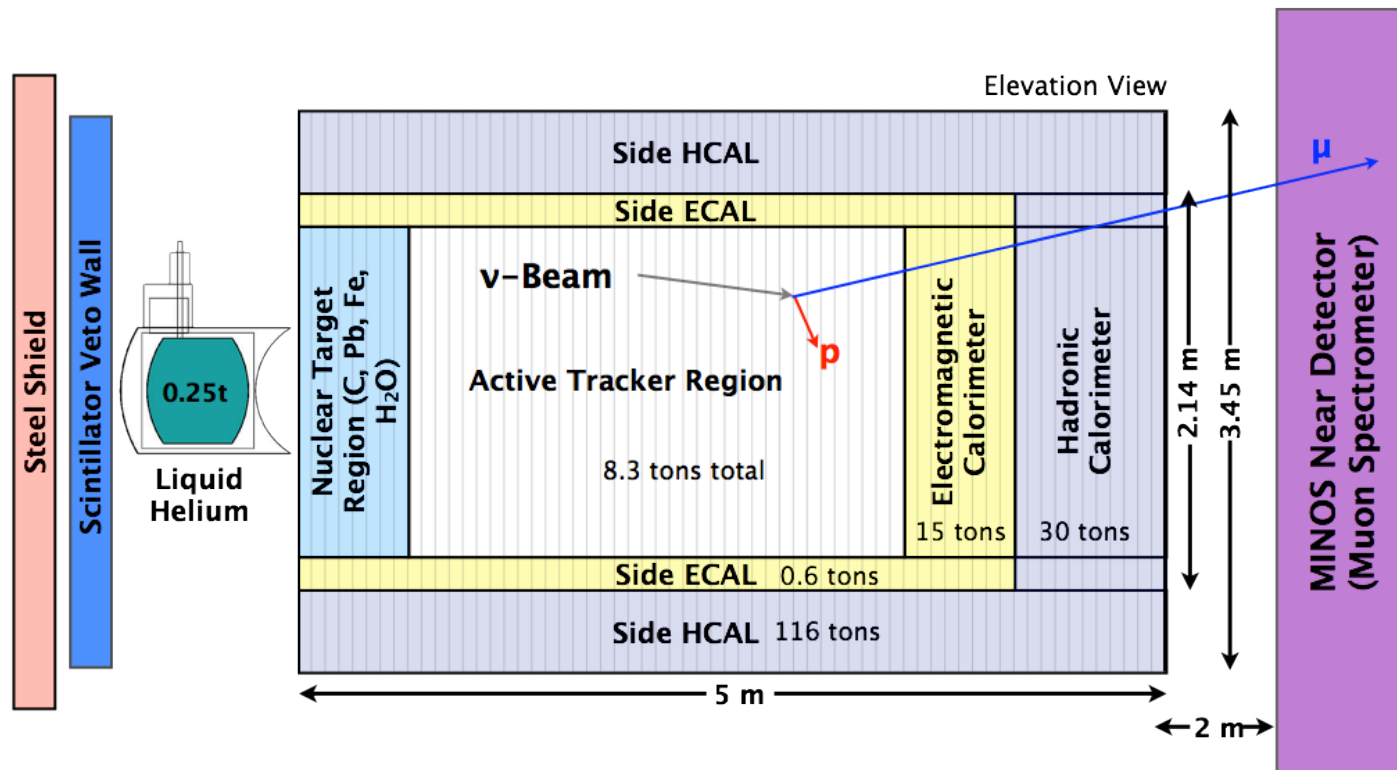


Two basic source of uncertainties:

- The description of the focusing components in the Monte Carlo is uncertain or incomplete.
- The theory of the hadronic interactions is not complete (MC needs a model).

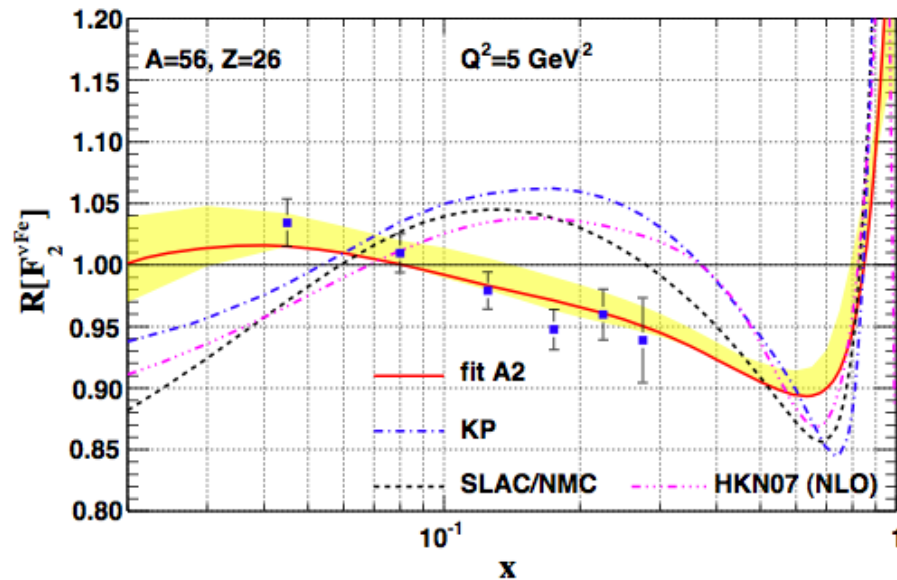
# MINERvA

- ◆ 120 polystyrene (CH) modules for tracking and calorimetry (~32k channels)
- ◆ Tracker surrounded by electromagnetic and hadronic calorimetry.
- ◆ MINOS Near Detector provides a muon spectrometer
- ◆ Nuclear targets of C (166 Kg), Fe (653 kg) and Pb (750 Kg)

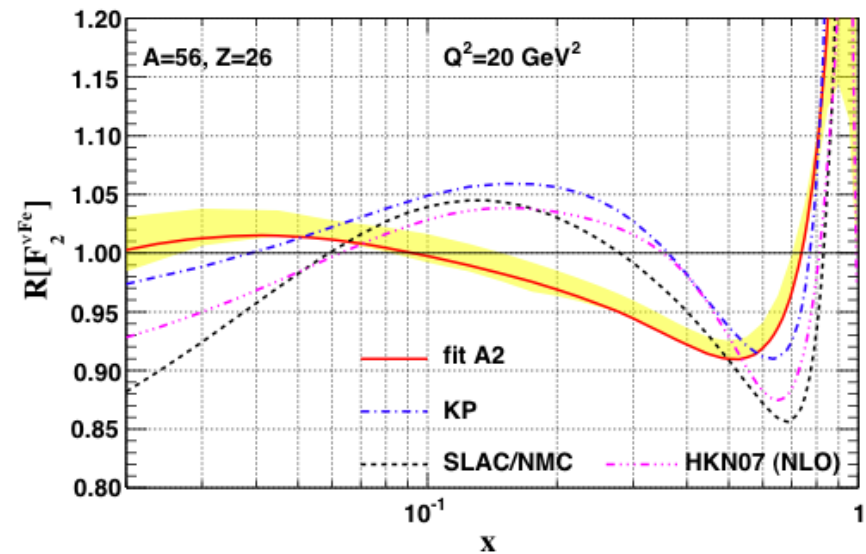


# An nCTEQ $F_2^{\nu}$ DIS Nuclear Effects Analysis using NuTeV $\nu$ -Iron DIS Events

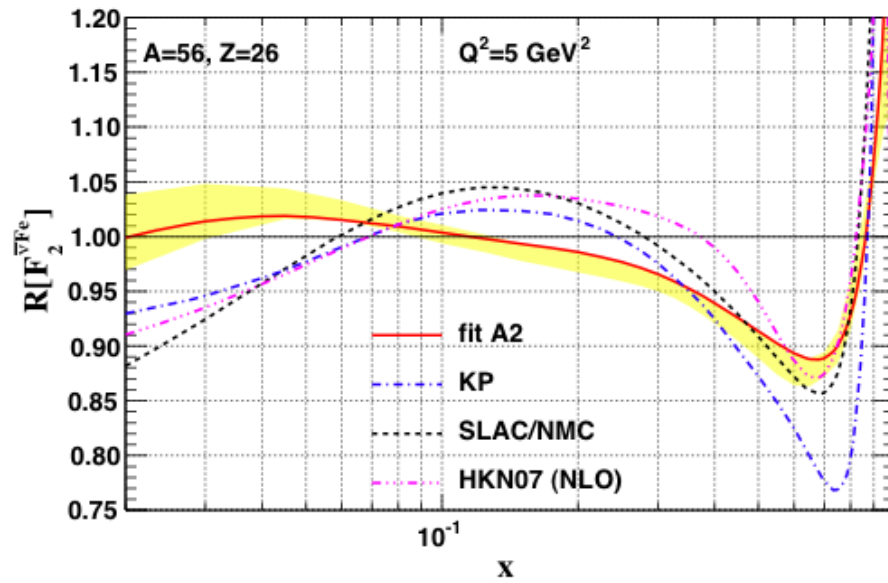
K. Kovarik et al - Phys.Rev.Lett. 106 (2011) 122301



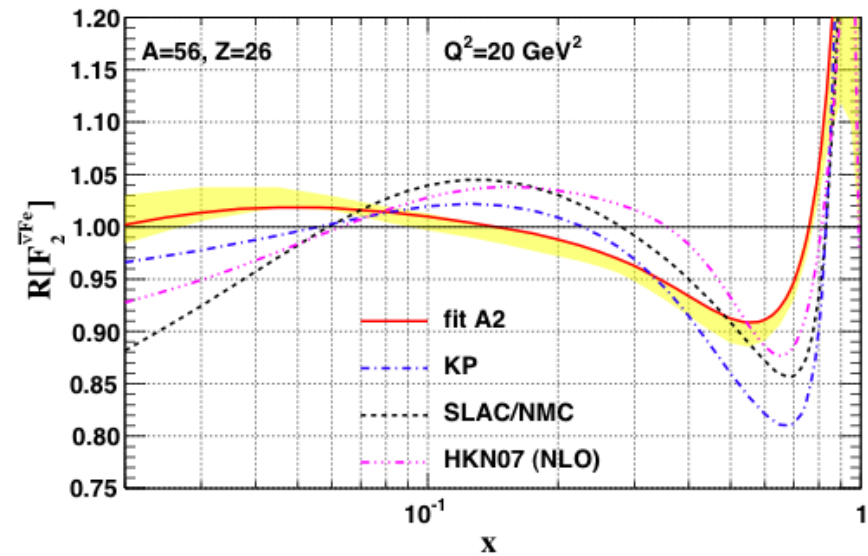
$$\frac{F_2(\nu + \text{Fe})}{F_2(\nu + [n+p])}$$



# $F_2$ Structure Function Ratios: $\bar{\nu}$ -Iron

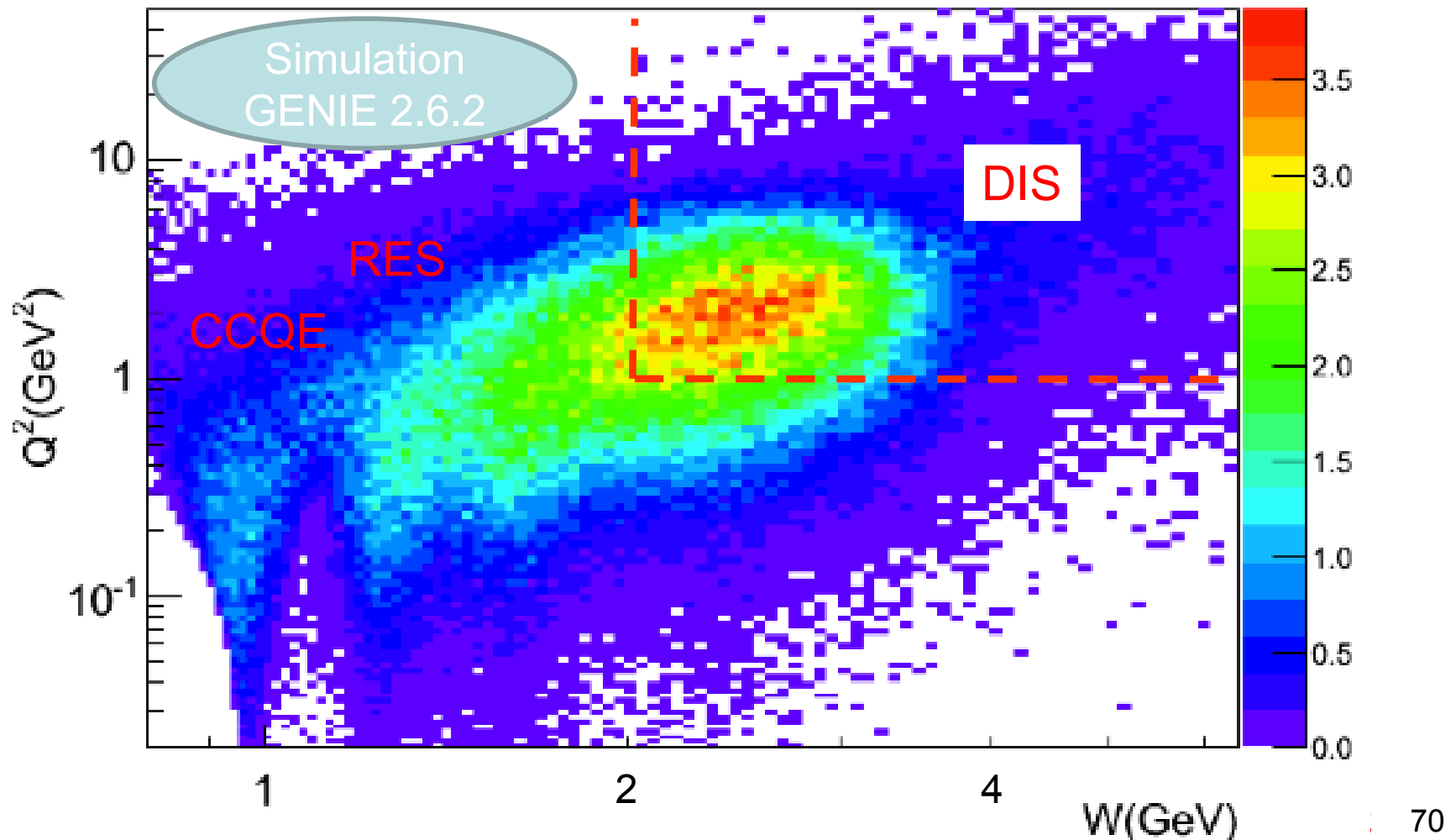


$$\frac{F_2(\bar{\nu} + \text{Fe})}{F_2(\bar{\nu} + [n+p])}$$

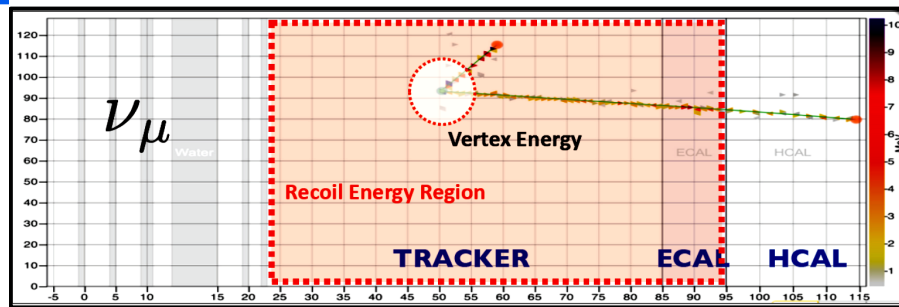


The current ME data being taken by MINERvA will have a large sample of DIS events on nuclear targets.

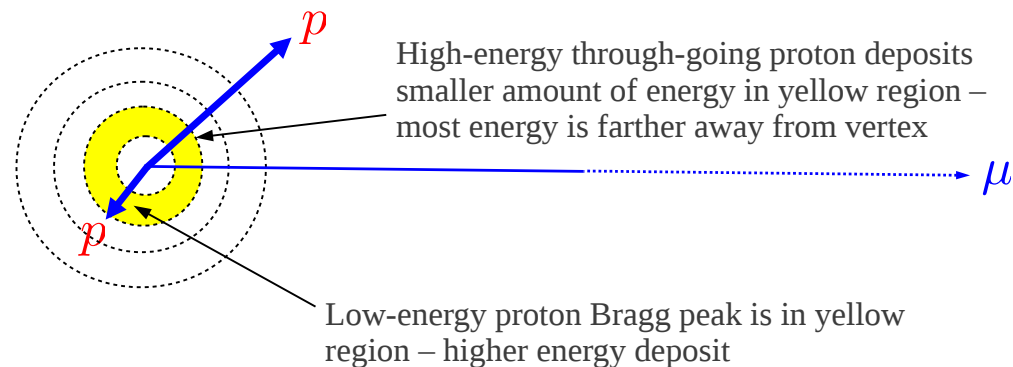
Event statistics for ME neutrino run



# Vertex Energy



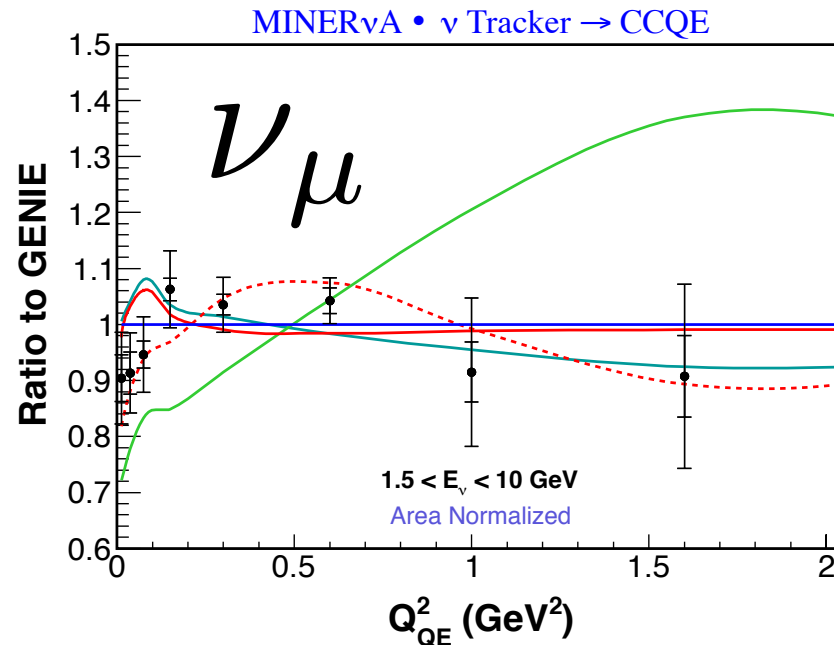
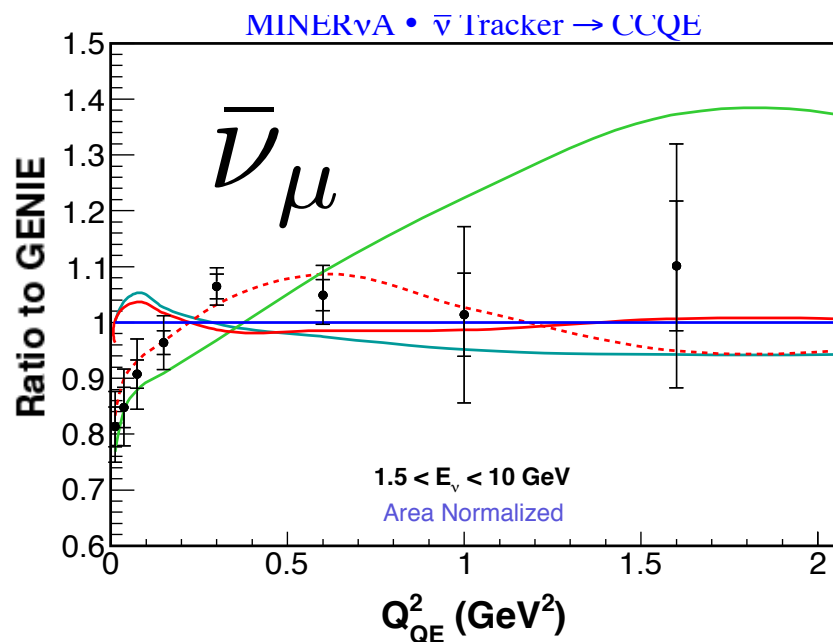
- ◆ Examine annular rings around the reconstructed vertex
  - ▼ Out to 10 cm for antineutrino ( $\sim 120$  MeV proton)
  - ▼ Out to 30 cm for neutrino ( $\sim 225$  MeV proton)



Note: to add visible energy to an inner annulus you must **add a charged hadron**, not just increase energy of an existing one

# MINERvA: Single Muon QE-like Analysis

Emphasis on the Shape



**GENIE**



independent nucleons in a mean field ( $M_A = 0.99$  GeV)

**$M_A = 1.35$  GeV**



best fit to MiniBooNE data

**Spectral Function**



improved nucleon momentum-energy relation

**TEM**



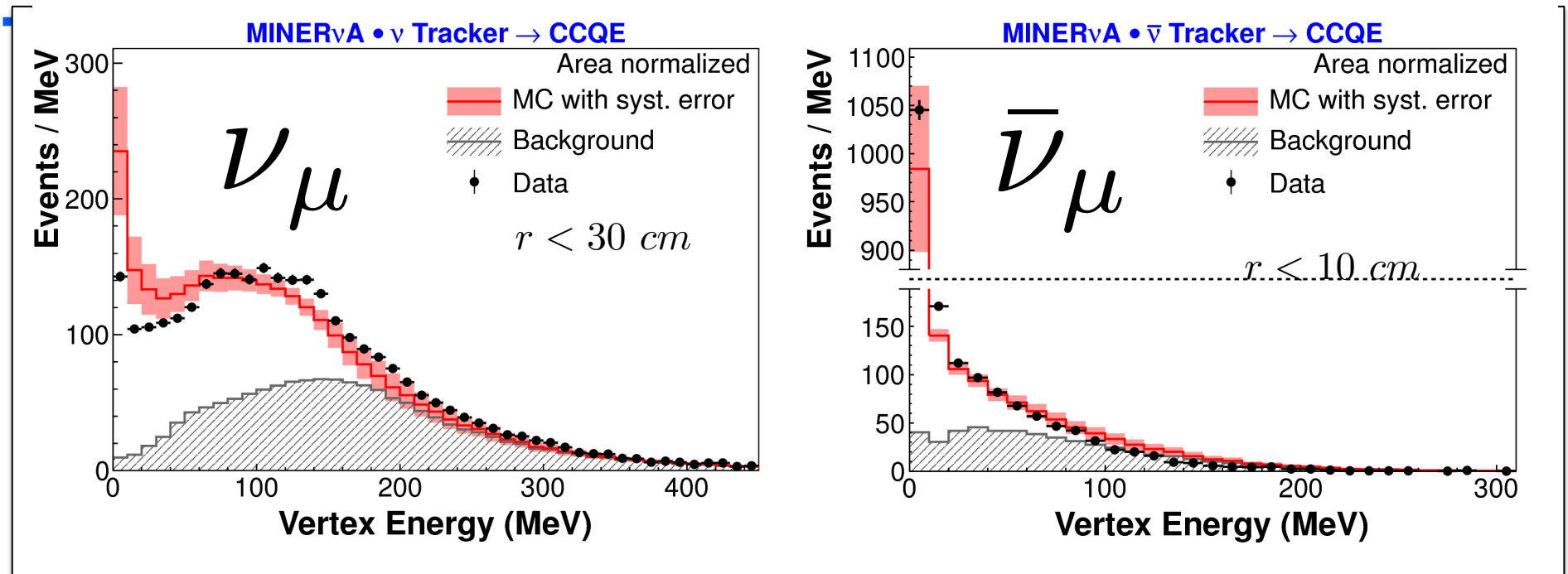
empirical model based on electron scattering data to account for nucleon-nucleon correlations. **V current only!**



# A small step to the Hadron Vertex

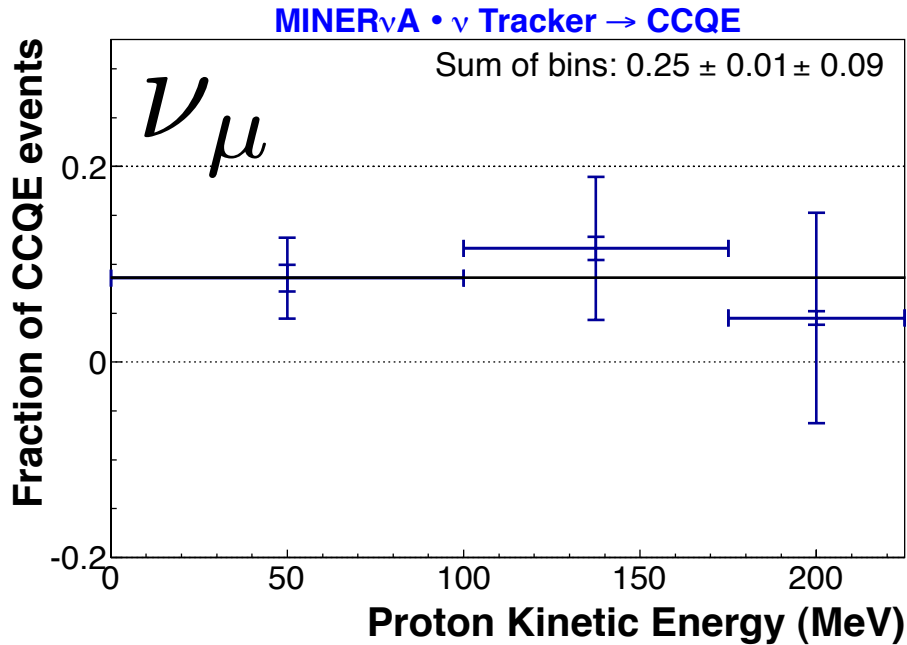
## MINERvA $\nu$ Tracker $\rightarrow$ CCQE

### MINERvA $\bar{\nu}$ Tracker $\rightarrow$ CCQE

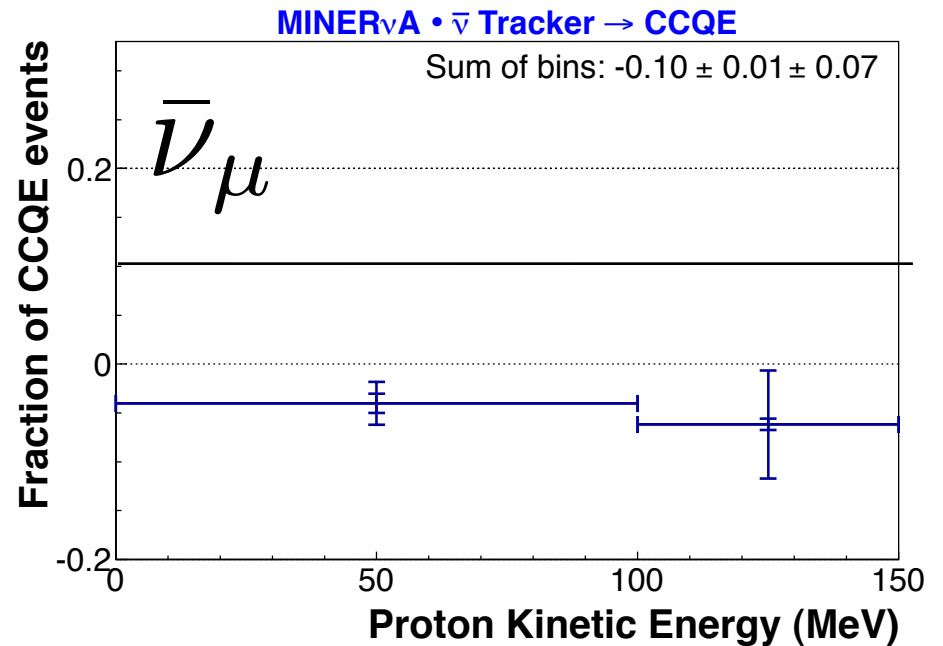


- ◆ A harder spectrum of vertex energy is observed in neutrinos.
- ◆ All systematics considered, including energy scale errors on charged hadrons and FSI model uncertainties.
- ◆ At this point, we make the *working assumption* that the additional vertex energy per event in data is *due to protons*

# Vertex Energy – suggestion of additional protons coming out of the nucleus in neutrino interactions



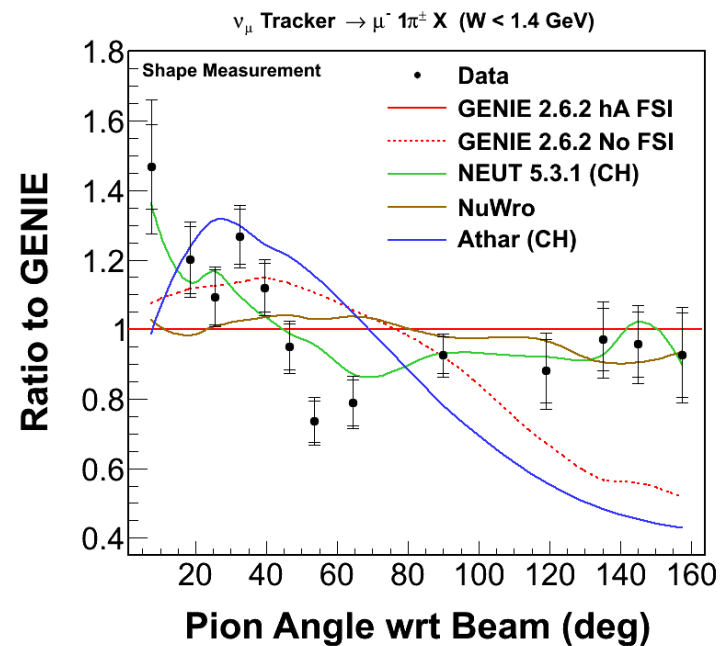
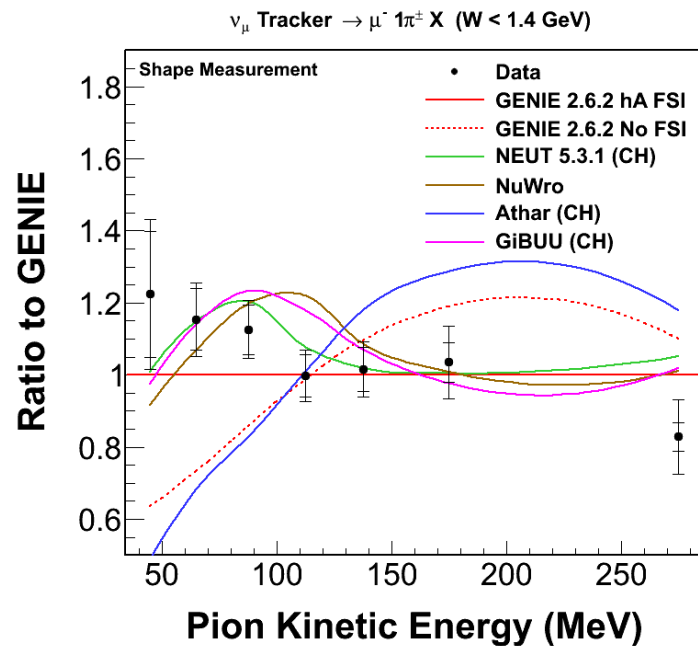
The fit wants to add an additional low-energy proton (KE < 225 MeV) to  **$(25 \pm 9)\%$  of QE events** to improve agreements with data



No such additional proton is required for antineutrinos. Slight reduction if anything.  **$(-10 \pm 7)\%$  of QE events**

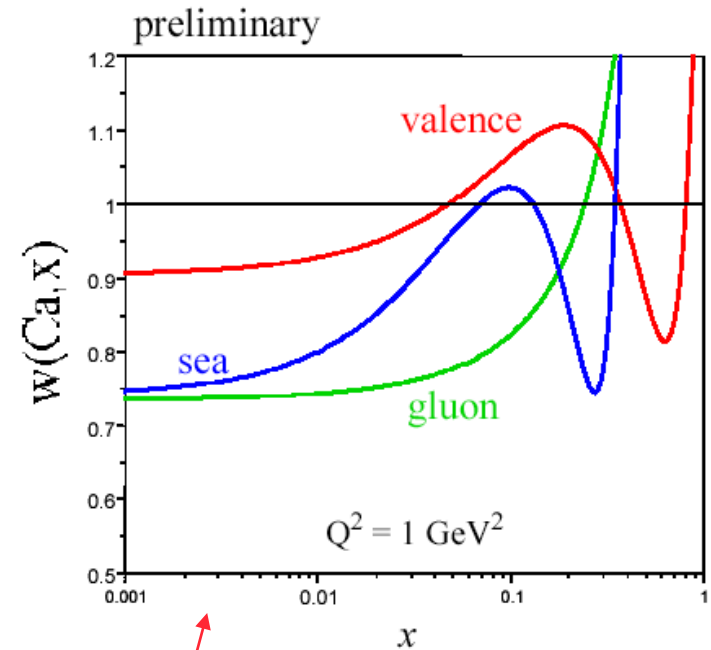
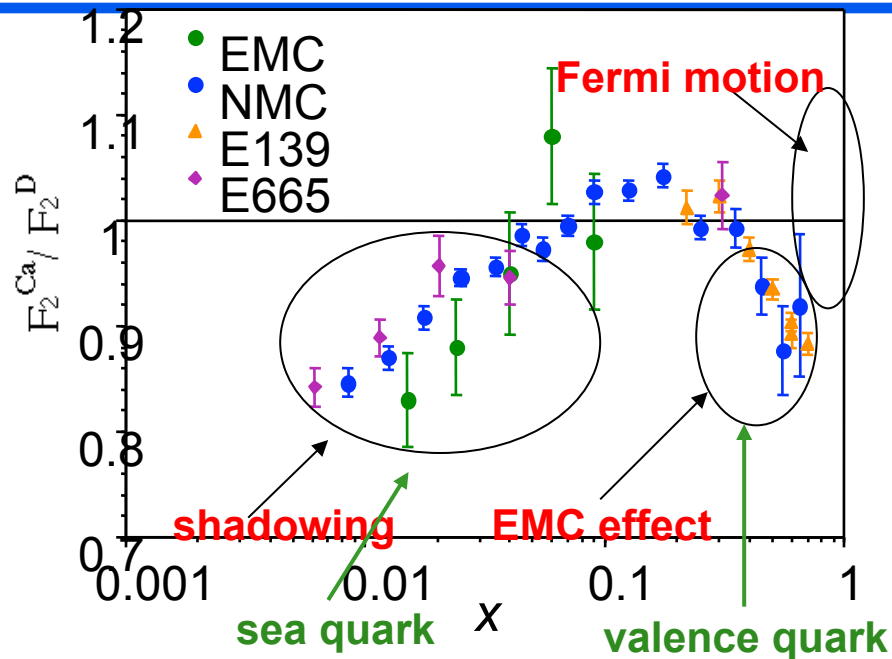
# More details: charged pion ( $W < 1.4$ GeV) model shape comparisons

- ◆ Each calculation is normalized to data, show ratio to GENIE w/FSI



- GiBUU, NuWro, NEUT and GENIE all predict the data shape well
- Data sensitive to the details in pion interaction models
- Athar does not agree with data. Likely due to insufficient FSI.

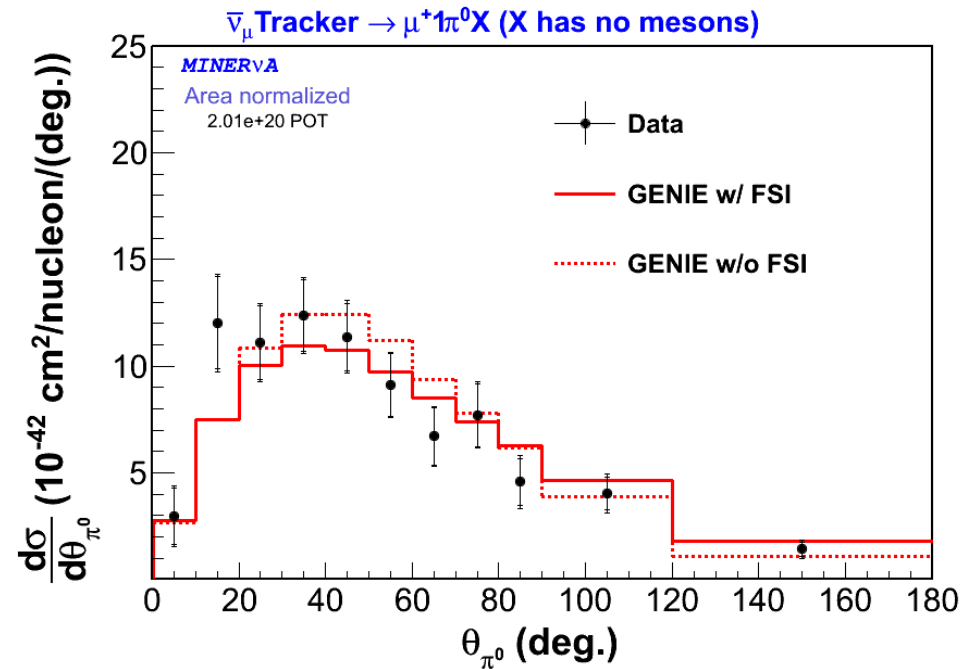
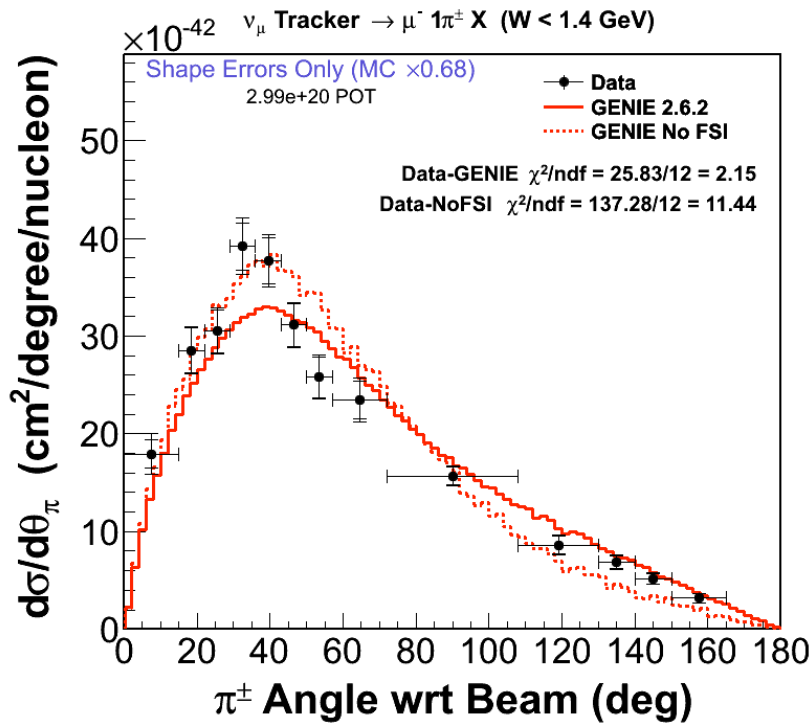
# Studies of DIS x-dependent Nuclear Effects with Neutrinos



- ◆  $F_2$  / nucleon changes as a function of  $A$ . Specifically measured in  $\mu/e - A$  not in  $\nu - A$
- ◆ Good reason to consider nuclear effects are DIFFERENT in  $\nu - A$ .
  - ▼ Presence of axial-vector current.
  - ▼ SPECULATION: Stronger shadowing for  $\nu - A$  but somewhat weaker “EMC” effect.
  - ▼ Different nuclear effects for valence and sea --> different shadowing for  $x F_3$  compared to  $F_2$ .

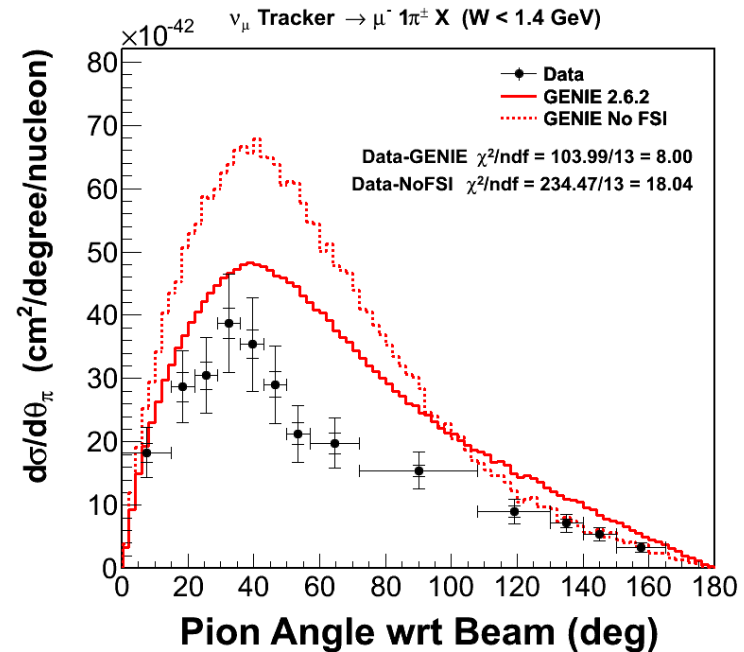
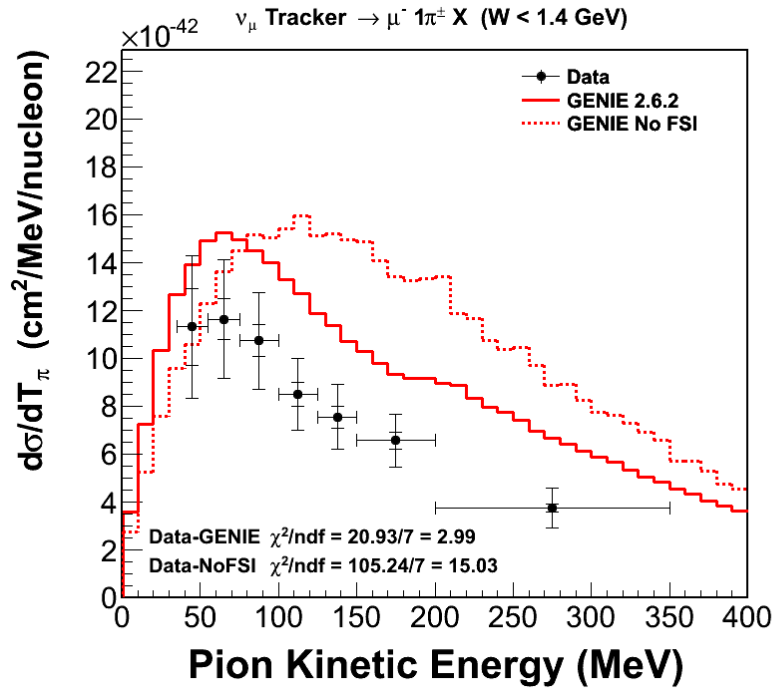
# FSI Conclusions for Pion Angle

## (Shape Comparisons)



- ◆ Data prefer GENIE with FSI

# More details: charged pion ( $W < 1.4$ GeV) absolute cross sections



- GENIE (MC) magnitude is too large with only a small dip
- Model with FSI strongly favored over no FSI

Suggested Improvement: full description of initial state including N-N Correlations

## Green's Function Monte Carlo Techniques

ANL - A. Lovato, S. C. Pieper, and R. B. Wiringa

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- ◆ Current neutrino event generators:
  - ▼ Generally lag behind theory by decades and are an assembly of multiple independent processes that require additional care to be combined.
  - ▼ Eg. beware double counting when combining spectral functions with MEC.
- ◆ Quantum Monte Carlo (QMC), in particular Green's Function Monte Carlo (GFMC), methods make it possible to carry out first-principle, exact calculations of nuclear properties for light nuclei (to carbon) .
- ◆ GFMC
  - ▼ based on realistic Hamiltonians including two- and three-nucleon potentials.
  - ▼ Calculations retain the full complexity of the many-body correlations
  - ▼ reproduce very well the observed energy spectra of  $A = 2 - 4$  nuclei, and the ground-state and low-lying excited-state energies of nuclei in the mass range  $A = 6 - 12$ .
- ◆ GFMC still need to incorporate crucial dynamical aspects into theoretical models to provide a reliable description of the interactions between a neutrino and a heavy nucleus
  - ▼ correlations, many-body currents, and interference effects.