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Stanford CS224W: Reasoning over Knowledge Graphs

CS224W: Machine Learning with Graphs Jure Leskovec, Stanford University http://cs224w.stanford.edu



- 10/31: Homework 3 released
- 11/4 (Mon): Homework 2 due
 - Gradescope submissions close at midnight

HW 2 was updated last Wednesday (check ed)!

- Recitation recording is on edstem
- 11/5 (Tues): No class election day
- 11/7 (Thurs): Colab 3 due
- 11/7 (Tues): Project Milestone due

Response to high-frequency feedbacks

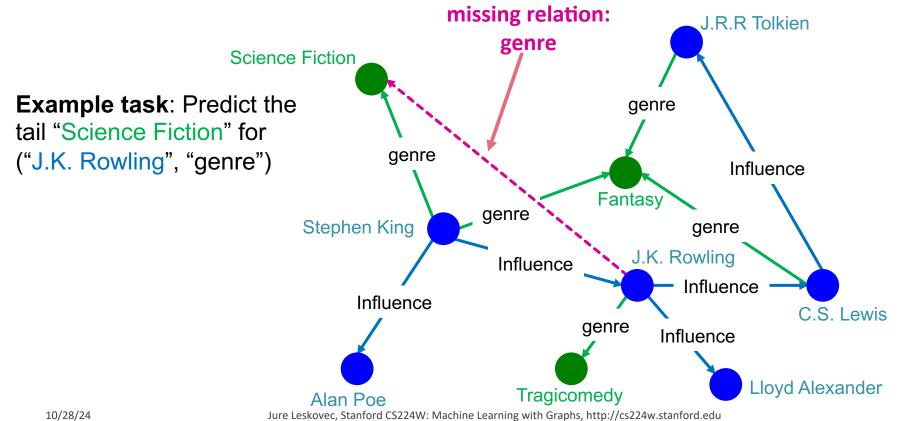
Ed post We will enforce 24 hours response time.

 Assignment description
 We will make sure to expand the homework description to make them clear

Recap: KG Completion Task

Given an enormous KG, can we complete the KG?

- For a given (head, relation), we predict missing tails.
 - (Note this is slightly different from link prediction task)



4

Today: Reasoning over KGs

Goal:

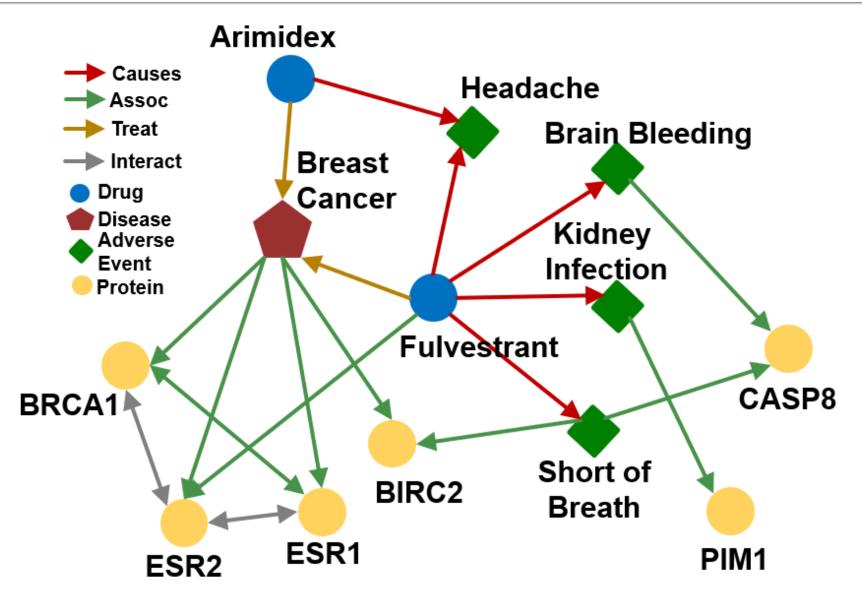
How to perform multi-hop reasoning over KGs?

Reasoning over Knowledge Graphs

- Answering multi-hop queries
 - Path Queries
 - Conjunctive Queries

Query2Box

Example KG: Biomedicine



Predictive Queries on KG

Can we do multi-hop reasoning, i.e., answer complex queries on an incomplete, massive KG?

Query Types	Examples: Natural Language Question, Query
One-hop Queries	What adverse event is caused by Fulvestrant? (e:Fulvestrant, (r:Causes))
Path Queries	What protein is associated with the adverse event caused by Fulvestrant? (e:Fulvestrant, (r:Causes, r:Assoc))
Conjunctive Queries	What is the drug that treats breast cancer and caused headache? ((e:BreastCancer, (r:TreatedBy)), (e:Migraine, (r:CausedBy))

In this lecture, we only focus on answering queries on a KG! The notation will be detailed next.



One-hop Queries



Path Queries



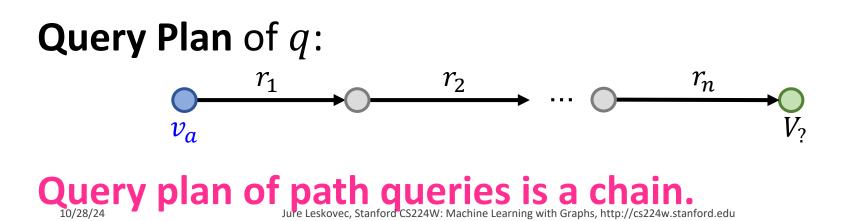
Conjunctive Queries

Predictive One-hop Queries

- We can formulate knowledge graph completion problems as answering one-hop queries.
- KG completion: Is link (h, r, t) in the KG?
- One-hop query: Is t an answer to query (h, r)?
 For example: What side effects are caused by drug Fulvestrant?

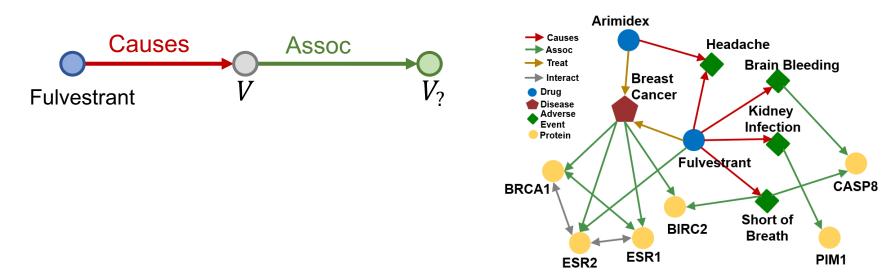
Path Queries

- Generalize one-hop queries to path queries by adding more relations on the path.
- An *n*-hop path query q can be represented by $q = (v_a, (r_1, ..., r_n))$
 - v_a is an "anchor" entity,
 - Let answers to q in graph G be denoted by $\llbracket q \rrbracket_G$.



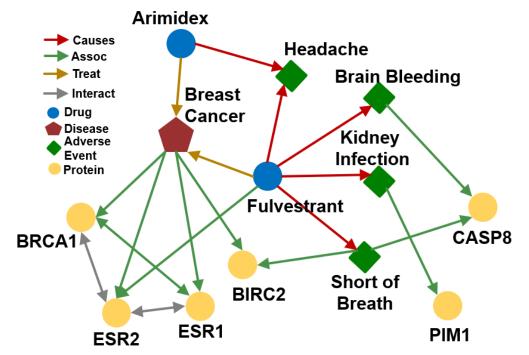
Question: "What proteins are **associated** with adverse events **caused** by **Fulvestrant**?"

- *v_a* is e:Fulvestrant
- (r_1, r_2) is (**r:Causes**, **r:Assoc**)
- Query: (e:Fulvestrant, (r:Causes, r:Assoc))



Question: "What proteins are associated with adverse events caused by Fulvestrant?" Query: (e:Fulvestrant, (r:Causes, r:Assoc))

Given a KG, how to answer a path query?



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Traversing Knowledge Graphs

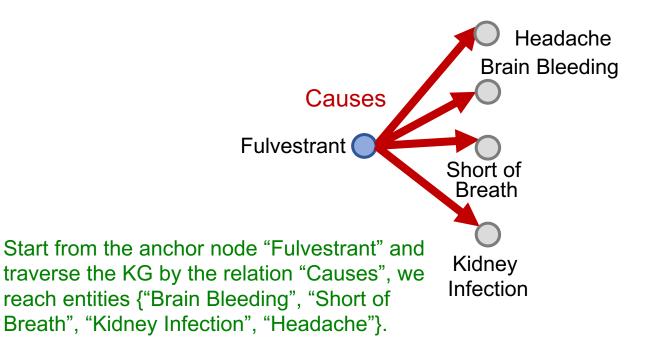
 We answer path queries by traversing the KG: "What proteins are associated with adverse events caused by Fulvestrant?"
 Query: (e:Fulvestrant, (r:Causes, r:Assoc))



Start from the **anchor node** (Fulvestrant).

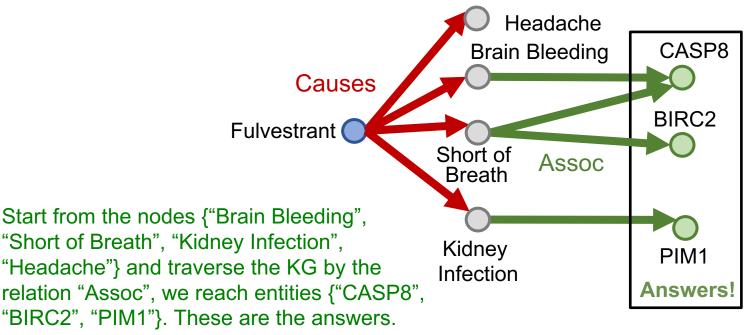
Traversing Knowledge Graphs

 We answer path queries by traversing the KG: "What proteins are associated with adverse events caused by Fulvestrant?"
 Query: (e:Fulvestrant, (r:Causes, r:Assoc))



Traversing Knowledge Graphs

 We answer path queries by traversing the KG: "What proteins are associated with adverse events caused by Fulvestrant?"
 Query: (e:Fulvestrant, (r:Causes, r:Assoc))



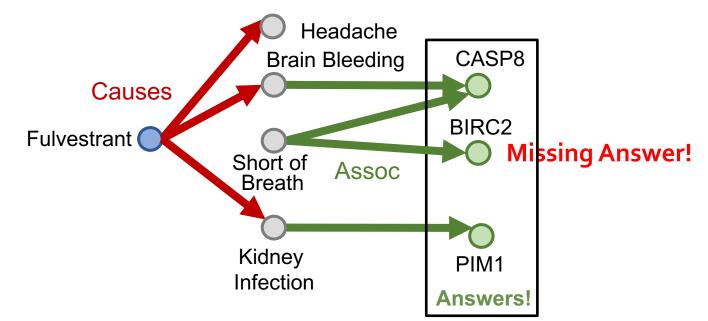
However, KGs are incomplete

- Answering queries seems easy: Just traverse the graph.
- But KGs are incomplete and unknown:
 - Many relations between entities are missing or are incomplete
 - For example, we lack all the biomedical knowledge
 - Enumerating all the facts takes non-trivial time and cost, we cannot hope that KGs will ever be fully complete

Due to KG incompleteness, one is not able to identify all the answer entities

Example: Incomplete KG

 We answer path queries by traversing the KG: "What proteins are associated with adverse events caused by Fulvestrant?"
 Query: (e:Fulvestrant, (r:Causes, r:Assoc))

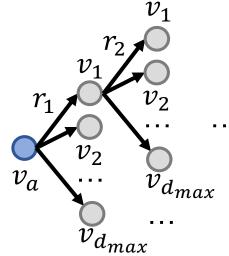


Can KG Completion Help?

Can we first do KG completion and then traverse the completed (probabilistic) KG?

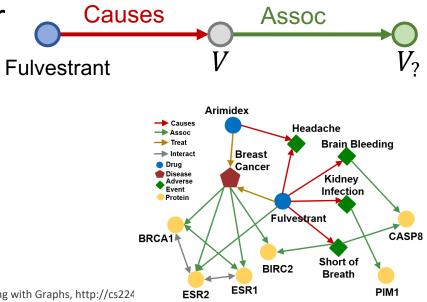
No! The "completed" KG is a dense graph!

- Most (h, r, t) triples (edge on KG) will have some non-zero probability.
- Time complexity of traversing a dense KG is exponential as a function of the path length L: O(d^L_{max})



Task: Predictive Queries

- We need a way to answer path-based queries over an incomplete knowledge graph.
- We want our approach to implicitly impute and account for the incomplete KG.
- Task: <u>Predictive queries</u>
 - Want to be able to answer arbitrary queries while Fu implicitly imputing for the missing information
 - Generalization of the link prediction task



Outline of the Lecture

1) Given entity embeddings, how do we answer an arbitrary query?

- Path queries: Using a generalization of TransE
- Conjunctive queries: Using Query2Box
- And-Or Queries: Using Query2Box and query rewriting

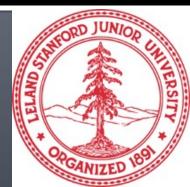
(We will assume entity embeddings and relation embeddings are given)

2) How do we train the embeddings?

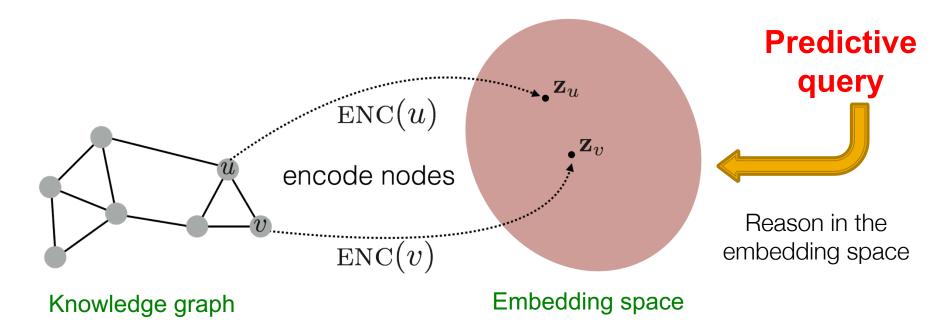
The process of determining entity and relation embeddings which allow us to embed a query.

Stanford CS224W: Answering Predictive Queries on Knowledge Graphs

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General Idea



Map queries into embedding space. Learn to reason in that space

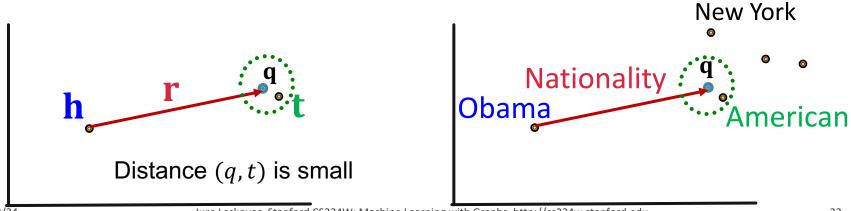
- Embed query into a single **point** in the Euclidean space: answer nodes are close to the query.
- Query2Box: Embed query into a hyper-rectangle (box) in the Euclidean space: answer nodes are enclosed in the box.

[Embedding Logical Queries on Knowledge Graphs. Hamilton, et al., NeurIPS 2018] [Query2box: Reasoning over Knowledge Graphs in Vector Space Using Box Embeddings. Ren, et al., ICLR 2020]

Idea: Traversing KG in Vector Space

Key idea: Embed queries!

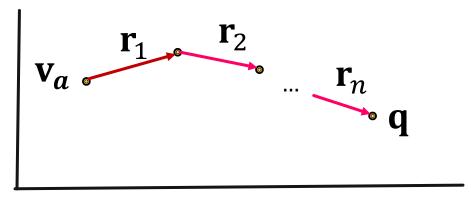
- Let's generalize TransE to multi-hop reasoning.
- **Recap: TransE:** Translate **h** to **t** using **r** with score function $f_r(h, t) = -||\mathbf{h} + \mathbf{r} \mathbf{t}||$.
- Another way to interpret this is that:
 - Query embedding: q = h + r
 - Goal: query embedding **q** is close to the answer embedding **t** $f_q(t) = -\|\mathbf{q} \mathbf{t}\|$



Traversing KG in Vector Space

Key idea: Embed queries!

• Generalize **TransE** to multi-hop reasoning. **Given a path query** $q = (v_a, (r_1, ..., r_n)),$



$$\mathbf{q} = \mathbf{v}_a + \mathbf{r}_1 + \dots + \mathbf{r}_n$$

The embedding process only involves vector addition, independent of # entities in the KG!

Traversing KG in Vector Space (1)

Embed path queries in vector space.

- Question: "What proteins are associated with adverse events caused by Fulvestrant?"
- Query: (e:Fulvestrant, (r:Causes, r:Assoc))
 Follow the query plan:

Query Plan

Embedding Process

Fulvestrant •



Traversing KG in Vector Space (2)

Embed path queries in vector space.

- Question: "What proteins are associated with adverse events caused by Fulvestrant?"
- Query: (e:Fulvestrant, (r:Causes, r:Assoc))
 Follow the query plan:

Query Plan

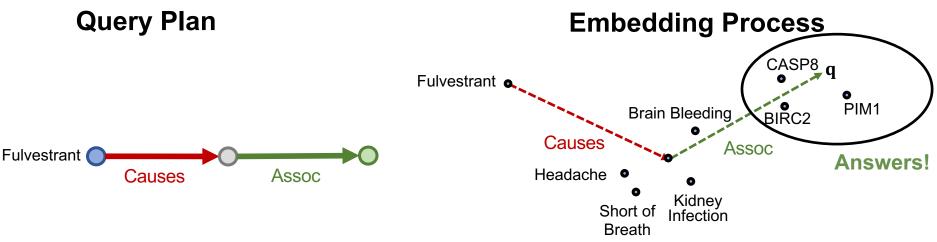
Embedding Process



Traversing KG in Vector Space (3)

Embed path queries in vector space.

- Question: "What proteins are associated with adverse events caused by Fulvestrant?"
- Query: (e:Fulvestrant, (r:Causes, r:Assoc))
 Follow the query plan:



Traversing KG in Vector Space (4)

Insights:

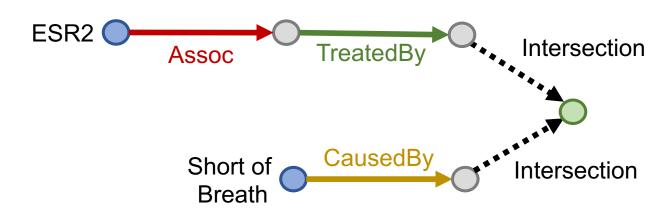
- We can train TransE to optimize knowledge graph completion objective
- Since TransE can naturally handle compositional relations, it can handle path queries by translating in the latent space for multiple hops using addition of relation embeddings.
- DistMult / ComplEx, since they cannot handle compositional relations, cannot be easily extended to handle path queries.

Conjunctive Queries

Can we answer more complex queries with logic conjunction operation?

Conjunctive Queries: "What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?" ((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

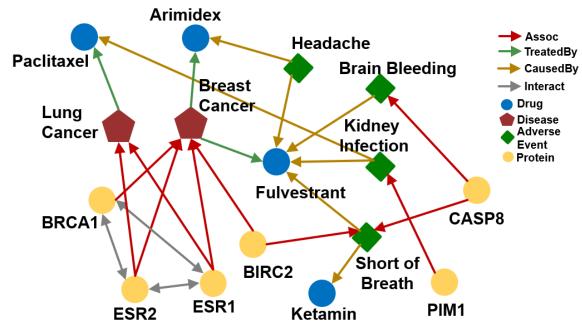
Query plan:



Conjunctive Queries

 "What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?" ((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

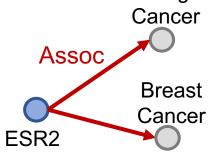
How do we answer the question by KG traversal?



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 "What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?" ((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

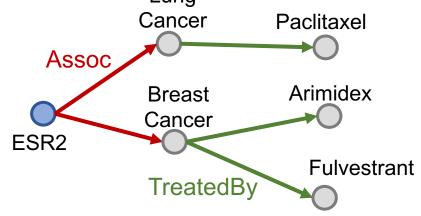
Traverse KG from anchor nodes: ESR2 and Short of Breath: Lung



Traverse from the first anchor "ESR2" by relation "Assoc", we reach a set of entities {"Lung Cancer", "Breast Cancer"}

 "What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?" ((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

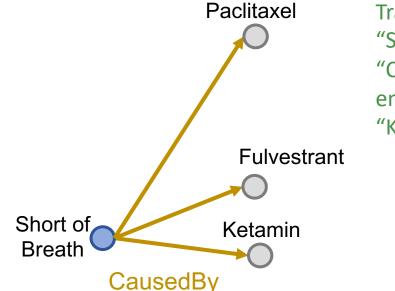
Traverse KG from anchor nodes: ESR2 and Short of Breath: Lung



Traverse from the set of entities {"Lung Cancer", "Breast Cancer"} by relation TreatedBy, we reach a set of entities {"Paclitaxel", "Arimidex", "Fulvestrant"}

 "What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?" ((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

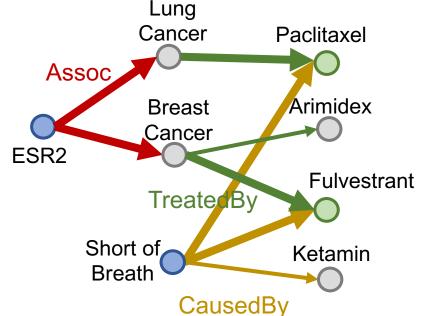
Traverse KG from **anchor nodes**: **ESR2** and **Short of Breath**:



Traverse from the second anchor "Short of Breath" by relation "CausedBy", we reach a set of entities {"Fulvestrant", "Ketamin", "Paclitaxel"}

 "What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?" ((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

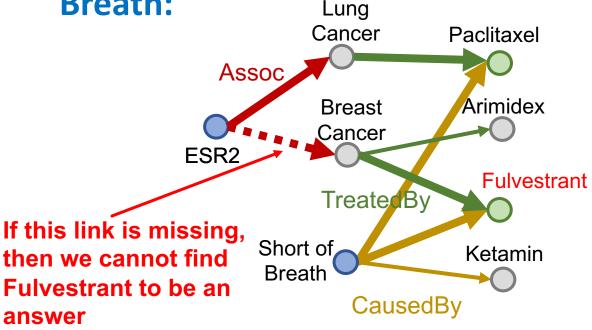
Traverse KG from anchor nodes: ESR2 and Short of Breath: Lung

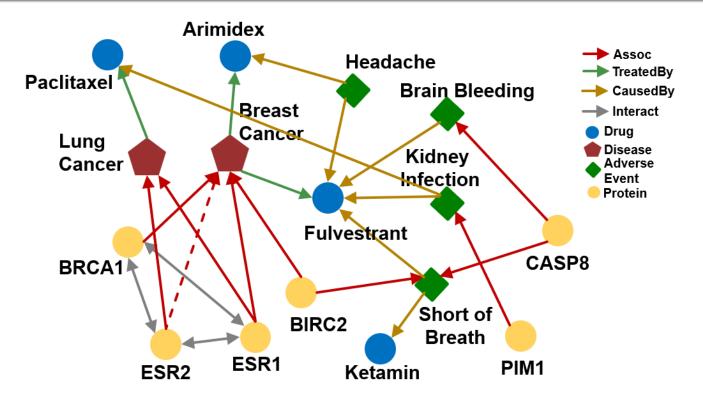


We take intersection between the two sets and get the answers {"Fulvestrant", "Paclitaxel"}

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- "What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?" ((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))
- Traverse KG from anchor nodes: ESR2 and Short of Breath:

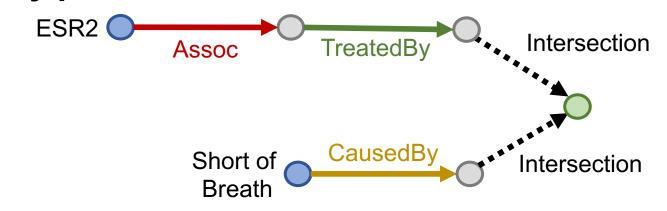




 How can we use embeddings to implicitly impute the missing (ESR2, Assoc, Breast Cancer)?
 Intuition: ESR2 interacts with both BRCA1 and ESR1. Both proteins are associated with breast cancer.

Traversing KG in Vector Space

 "What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?" ((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))
 Query plan:



Each intermediate node represents a <u>set of entities</u>, how do we represent it? How do we define the intersection operation in the latent space?

Stanford CS224W: Query2Box: Reasoning over KGs Using Box Embeddings

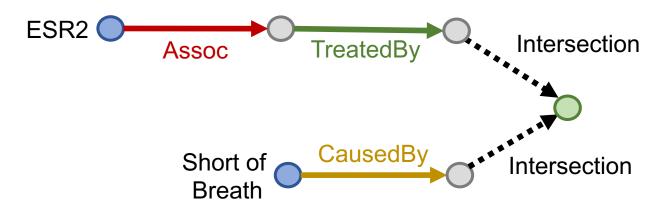
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Conjunctive Queries

How can we answer more complex queries with logical conjunction operation?

Query plan:

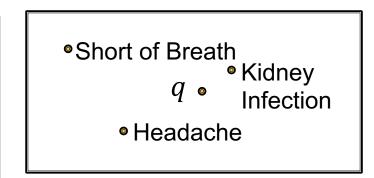


(1) Each intermediate node represents a set of entities; how do we represent it?(2) How do we define the intersection operation in the latent space?

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Box Embeddings

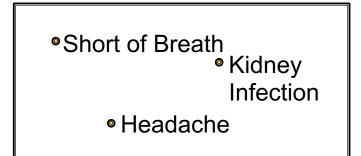
Embed queries with hyper-rectangles (boxes) q = (Center(q), Offset(q))



For example, we can embed the adverse events of Fulvestrant with a box that enclose all the answer entities.

Key Insight: Intersection

- Intersection of boxes is well-defined!
- When we traverse the KG to find the answers, each step produces a set of reachable entities.
- How can we better model these sets?
 - Boxes are a powerful abstraction, as we can project the center and control the offset to model the set of entities enclosed in the box



Things to figure out:

- Entity embeddings (# params: d|V|):
 - Entities are seen as zero-volume boxes
- Relation embeddings (# params 2d|R|)

Notation d: out degree |V|: # entities |R|: # relations

- Each relation takes a box and produces a new box
- Intersection operator f :
 - New operator, inputs are boxes and output is a box
 - Intuitively models intersection of boxes

Embed queries in vector space: "What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?" ((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

Traverse KG from **anchor nodes**: **ESR2** and **Short of Breath**:

Query plan



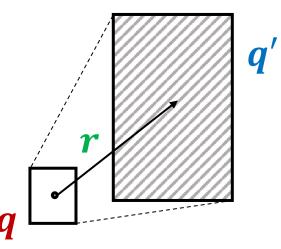
Projection Operator

Projection Operator 𝒫 ■ Intuition:

- Take the current box as input and use the relation embedding to project and expand the box!
- \mathcal{P} : Box × Relation \rightarrow Box

$$Cen(q') = Cen(q) + Cen(r)$$
$$Off(q') = Off(q) + Off(r)$$

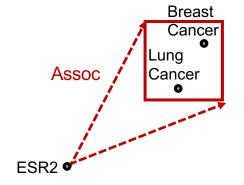
"×" (cross) means the projection operator is a relation from any box and relation to a new box



- Embed queries in vector space: "What are drugs that cause Short of Breath and treat diseases associated with protein ESR2?"
- Traverse KG from anchor nodes: ESR2 and Short of Breath:
 Use projection operator again following the query plan.

Query Plan



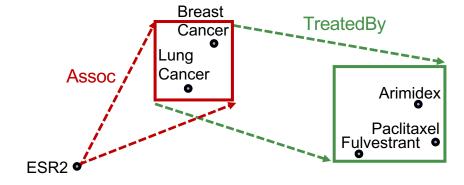


"What is the drug that causes Short of Breath and treats disease associated with protein ESR2?" ((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

Use projection operator again following the query plan.

Query Plan

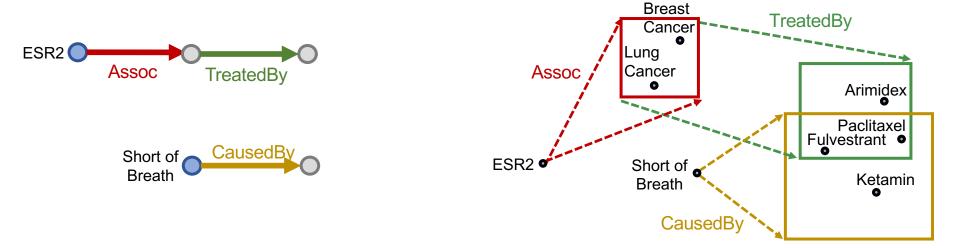




"What is the drug that causes Short of Breath and treats disease associated with protein ESR2?" ((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

Use projection operator again following the query plan.

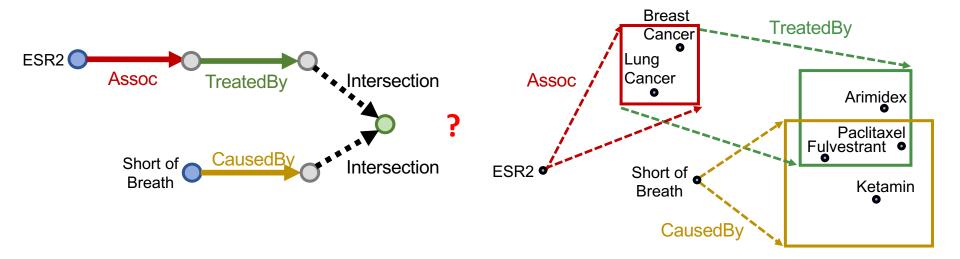




"What is the drug that causes Short of Breath and treats disease associated with protein ESR2?" ((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

How do we take intersection of boxes?

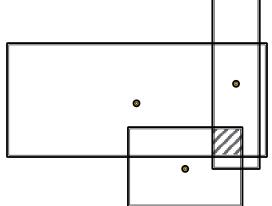
Query Plan



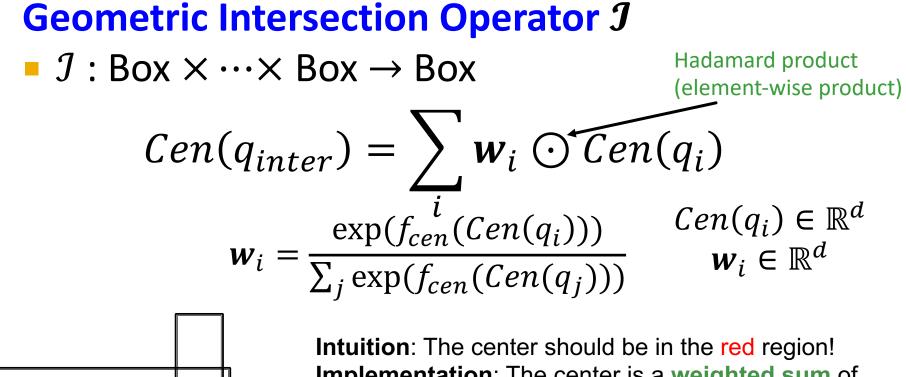
Intersection Operator

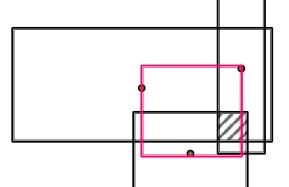
Geometric Intersection Operator $\boldsymbol{\mathcal{I}}$

- Take multiple boxes as input and produce the intersection box
- Intuition:
 - The center of the new box should be "close" to the centers of the input boxes
 - The offset (box size) should shrink (since the size of the intersected set is smaller than the size of all the input set)
- $\mathcal{I}: Box \times \cdots \times Box \to Box$



Intersection Operator





Intuition: The center should be in the red region! Implementation: The center is a weighted sum of the input box centers

 $w_i \in \mathbb{R}^d$ is calculated by a neural network f_{cen} (with trainable weights)

 w_i represents a "self-attention" score for the center of each input $Cen(q_i)$.

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Intersection Operator

Geometric Intersection Operator \mathcal{J}

 $= \min(Off(q_1), \dots, Off(q_n))$

 $\bigcirc \sigma(f_{off}(Off(q_1), \dots, Off(q_n)))$

• $\mathcal{I}: Box \times \cdots \times Box \rightarrow Box$

 $Off(q_{inter})$

guarantees shrinking

Sigmoid function: squashes output in (0,1)

 f_{off} is a neural network (with trainable parameters) that extracts the representation of the input boxes to increase expressiveness

Intuition: The offset should be smaller than the offset of the input box

Implementation: We first **take minimum** of the offset of the input box, and then we make the model more expressive by introducing a new function f_{off} to extract the **representation** of the input boxes with a **sigmoid function** to **guarantee shrinking**.

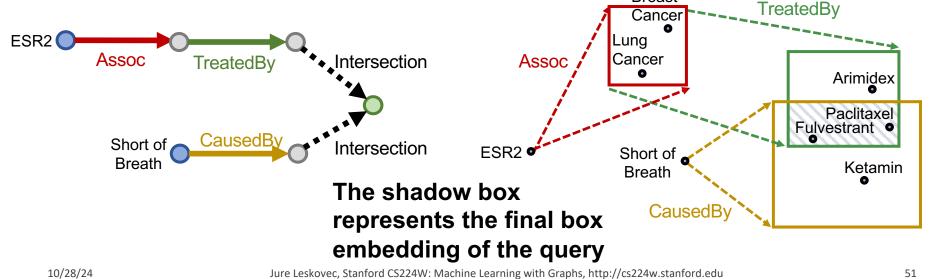
"What is the drug that causes Short of Breath and treats disease associated with protein ESR2?" ((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

Use box intersection operator

Query Plan

Embedding Space

Breast



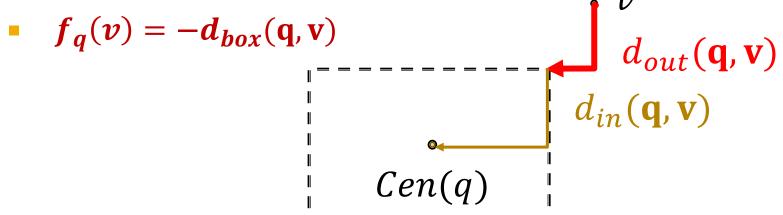
Entity-to-Box Distance

- How do we define the score function $f_q(v)$ (negative distance)? ($f_q(v)$ captures inverse distance of a node v as answer to q)
- Given a query box q and entity embedding (box) v,

$$d_{box}(\mathbf{q}, \mathbf{v}) = d_{out}(\mathbf{q}, \mathbf{v}) + \alpha \cdot d_{in}(\mathbf{q}, \mathbf{v})$$

where $0 < \alpha < 1$.

Intuition: if the point is enclosed in the box, the distance should be downweighted.



Extending to Union Operation

- Can we embed complex queries with union?
 E.g.: "What drug can treat breast cancer or lung cancer?"
- Conjunctive queries + disjunction is called
 Existential Positive First-order (EPFO) queries.
 We'll refer to them as AND-OR queries.
- Can we also design a disjunction operator and embed AND-OR queries in low-dimensional vector space?

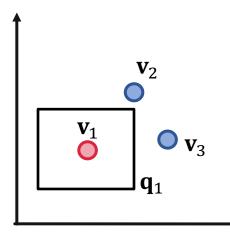
- Can we embed AND-OR queries in a lowdimensional vector space?
- No! Intuition: Allowing union over arbitrary queries requires high-dimensional embeddings!

Example:

- Given 3 queries q_1, q_2, q_3 , with answer sets:
- $\llbracket q_1 \rrbracket = \{v_1\}, \llbracket q_2 \rrbracket = \{v_2\}, \llbracket q_3 \rrbracket = \{v_3\}$
- If we allow union operation, can we embed them in a two-dimensional plane?

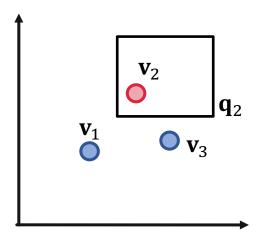
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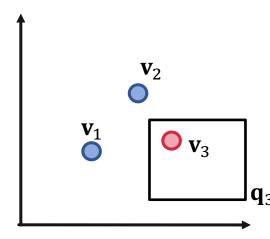
Example:

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- If we allow union operation, can we embed them in two-dimensional plane?



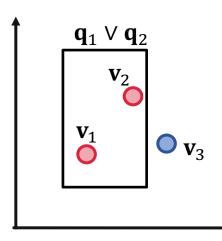
Example:

- Given 3 queries q_1, q_2, q_3 , with answer sets:
- $\llbracket q_1 \rrbracket = \{v_1\}, \llbracket q_2 \rrbracket = \{v_2\}, \llbracket q_3 \rrbracket = \{v_3\}$
- If we allow union operation, can we embed them in two-dimensional plane?



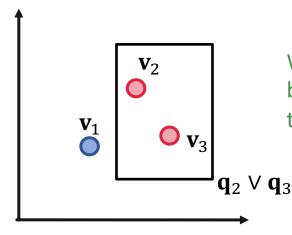
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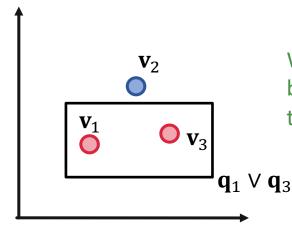
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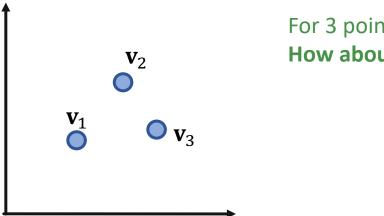
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Example:

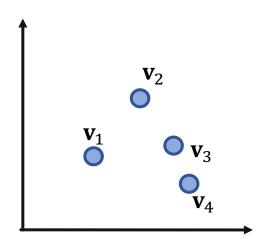
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For 3 points, 2-dimension is okay! How about 4 points?

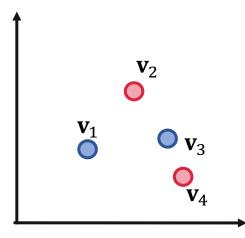
Example 2:

- Given 4 queries q_1, q_2, q_3, q_4 with answers:
- $\llbracket q_1 \rrbracket = \{v_1\}, \llbracket q_2 \rrbracket = \{v_2\}, \llbracket q_3 \rrbracket = \{v_3\}, \llbracket q_4 \rrbracket = \{v_4\},$
- If we allow union operation, can we embed them in two-dimensional plane?



Example 2:

- Given 4 queries q_1, q_2, q_3, q_4 with answers:
- $\llbracket q_1 \rrbracket = \{v_1\}, \llbracket q_2 \rrbracket = \{v_2\}, \llbracket q_3 \rrbracket = \{v_3\}, \llbracket q_4 \rrbracket = \{v_4\},$
- If we allow union operation, can we embed them in two-dimensional plane?



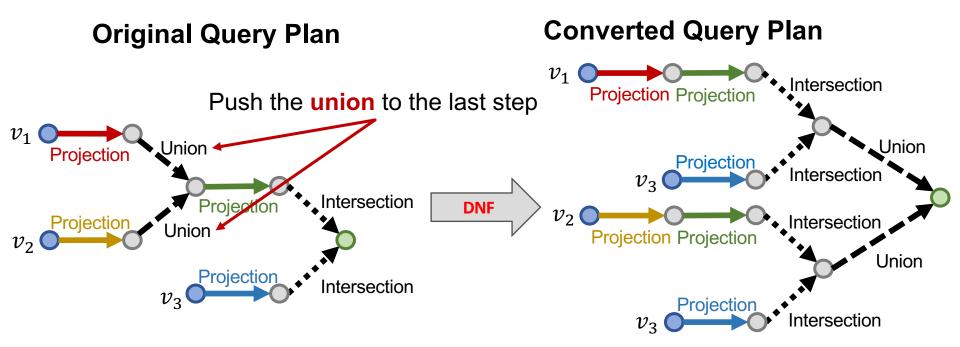
We cannot design a box embedding for $q_2 \lor q_4$, that only v_2 and v_4 are in the box but v_1 and v_3 are outside the box.

Can we embed AND-OR queries in lowdimensional vector space?

- **Conclusion**: Given any *M* conjunctive queries q_1, \ldots, q_M with non-overlapping answers, we need dimensionality of $\Theta(M)$ to handle all OR queries.
 - For real-world KG, such as FB15k, we find $M \ge 13,365$, where |V| = 14,951.
 - Remember, this is for arbitrary OR queries.

Since we **cannot embed** AND-OR queries in lowdimensional space, can we still handle them?

Key idea: take all unions out and only do union at the last step!



Disjunctive Normal Form

- Any AND-OR query can be transformed into equivalent DNF, i.e., disjunction of conjunctive queries.
- Given any AND-OR query q, $q = q_1 \lor q_2 \lor \cdots \lor q_m$ where q_i is a conjunctive query.
- Now we can first embed each q_i and then "aggregate" at the last step!

Distance Between q and an Entity

 Distance between entity embedding and a DNF q = q₁ ∨ q₂ ∨ … ∨ q_m is defined as:
 d_{box}(q, v) = min(d_{box}(q₁, v), ..., d_{box}(q_m, v))

Intuition:

- As long as v is the answer to one conjunctive query q_i, then v should be the answer to q
- As long as v is close to one conjunctive query q_i, then v should be close to q in the embedding space

Distance Between q and an Entity

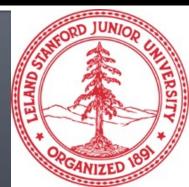
 Distance between entity embedding and a DNF q = q₁ ∨ q₂ ∨ … ∨ q_m is defined as: d_{box}(q, v) = min(d_{box}(q₁, v), ..., d_{box}(q_m, v))

The process of embedding any AND-OR query q

- 1. Transform q to equivalent DNF $q_1 \vee \cdots \vee q_m$
- **2.** Embed q_1 to q_m
- 3. Calculate the (box) distance $d_{box}(\mathbf{q}_i, \mathbf{v})$
- 4. Take the **minimum** of all distance
- 5. The final score $f_q(v) = -d_{box}(\mathbf{q}, \mathbf{v})$

Stanford CS224W: How to Train Query2box

CS224W: Machine Learning with Graphs Jure Leskovec, Stanford University http://cs224w.stanford.edu



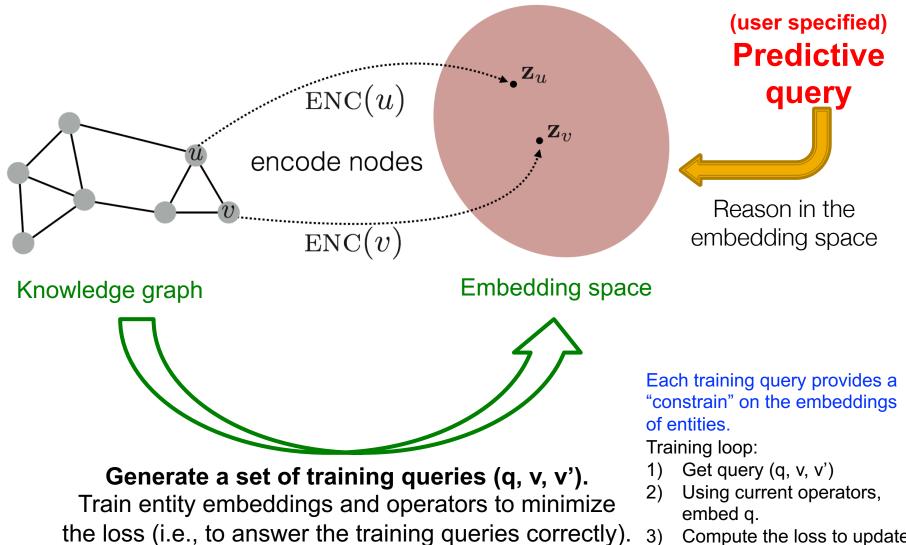
Training Overview

Overview and Intuition (similar to KG completion):

- Given a query embedding \mathbf{q} , maximize the score $f_q(v)$ for answers $v \in \llbracket q \rrbracket$ and minimize the score $f_q(v')$ for negative answers $v' \notin \llbracket q \rrbracket$
- Trainable parameters:
 - Entity embeddings with d|V| # params
 - Relation embeddings with 2d|R| # params
 - Intersection operator

How to achieve a query, its answers, its negative answers from the KG to train the parameters?
How to split the KG for query answering?

Training Overview



3) Compute the loss to update entity embs. and operators

Training: Details

Training:

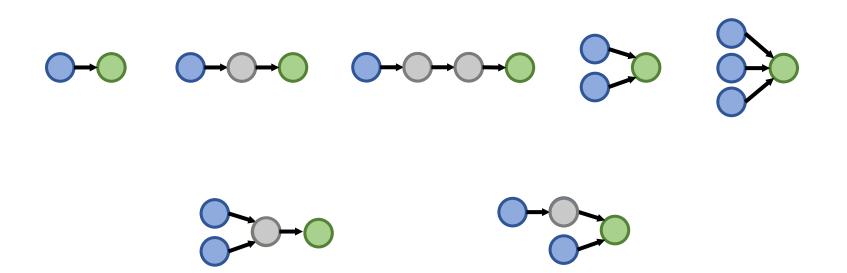
1. Sample a query q from the training graph G_{train} , answer $v \in [\![q]\!]_{G_{train}}$, and non-answer $v' \notin [\![q]\!]_{G_{train}}$

2. Embed the query **q**.

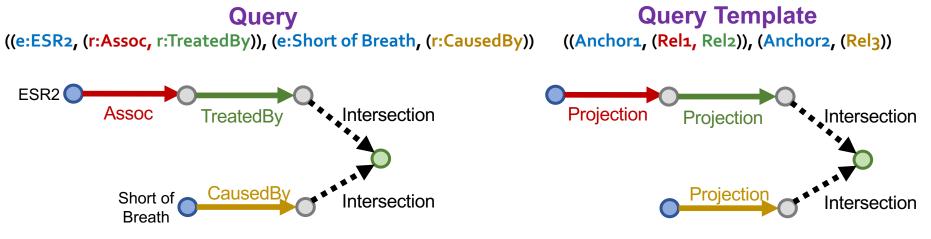
- Use current operators, to compute query embedding.
- 3. Calculate the score $f_q(v)$ and $f_q(v')$.
- 4. Optimize embeddings and operators to minimize the loss ℓ (maximize $f_q(v)$ while minimize $f_q(v')$):

$$\ell = -\log\sigma\left(f_q(\nu)\right) - \log(1 - \sigma\left(f_q(\nu')\right))$$

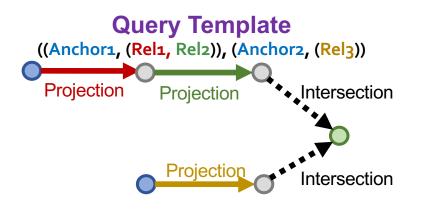
 Generate queries from multiple query templates:



- How can we generate a complex query?
- We start with a query template
- Query template is an abstraction of the query
- We generate a query by instantiating every variable with a concrete entity and relation from the KG
 - E.g., instantiate Anchor1 with ESR2 (a node on KG)
 - E.g., instantiate Rel1 with Assoc (an edge on KG)
- How to instantiate query template given a KG?



How to instantiate a query template given a KG?

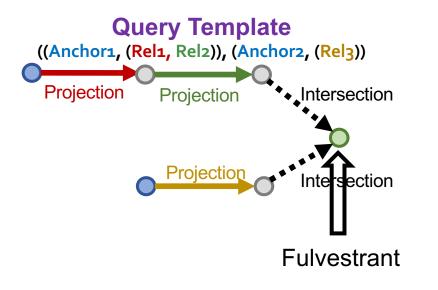


Knowledge Graph Lung Cancer Paclitaxel Breast Arimidex Cancer ESR2 Fulvestrant Short of Ketamin Breath CausedBy

Overview:

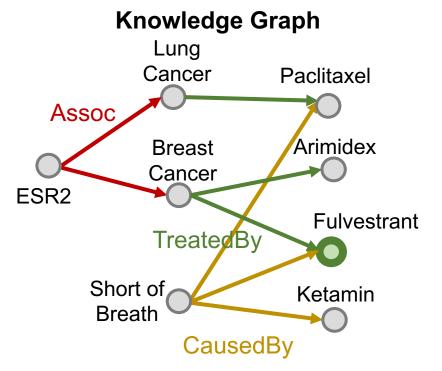
Start from instantiating the **answer node** of the query template and then iteratively instantiate the other edges and nodes until we ground **all the anchor nodes**

How to instantiate a query template given a KG?

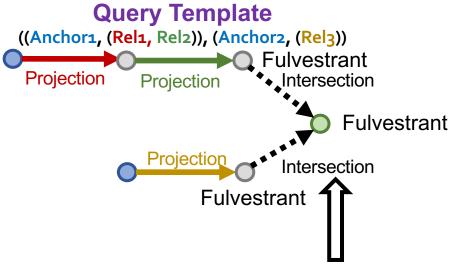


Start from instantiating the **root node** of the query template.

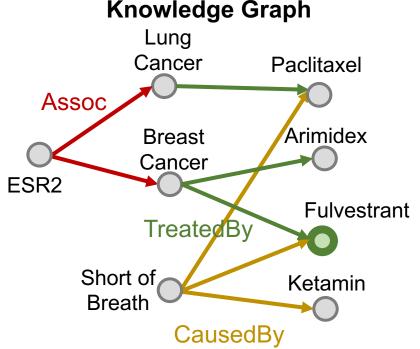
Randomly pick one entity from KG as the root node, e.g., we pick **Fulvestrant**.



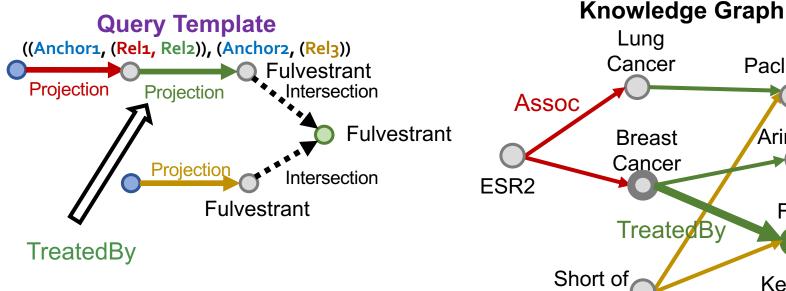
How to instantiate a query template given a KG?



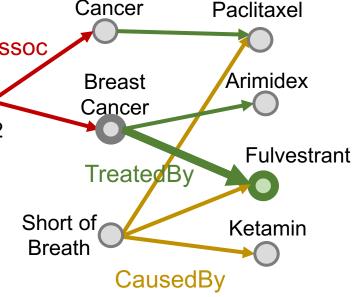
U Now we look at intersection. What we have is that the intersection of the sets of entities is **Fulvestrant**, then naturally the two sets should also contain **Fulvestrant**.



How to instantiate a query template given a KG?



We instantiate the **Projection edge** in the template by randomly sample one relation associated with the current entity **Fulvestrant**. For example, we may select relation **TreatedBy**, and check what entities are connected to Fulvestrant with TreatedBy: {Breast Cancer}.



How to instantiate a query template given a KG?

Knowledge Graph

Paclitaxel

Arimidex

Ketamin

Fulvestrant

Lung

Cancer

Breast

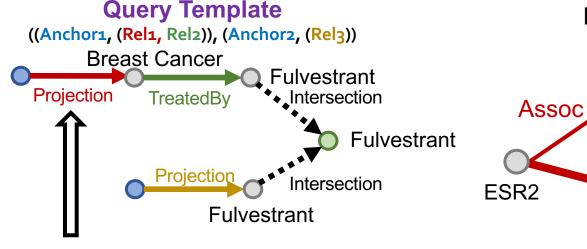
Cancer

Short of

Breath

TreatedBy

CausedBy



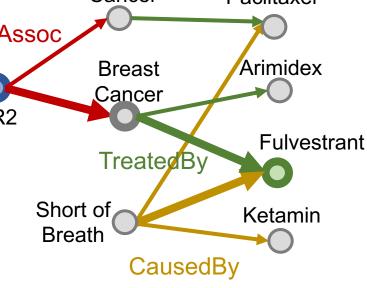
Assoc

We first look at one branch and ground the **Projection edge** with the relation associated with **Breast Cancer**, e.g., **Assoc**. Then we check what entities are connected to **Breast Cancer** with **Assoc**: {**ESR2**}.

How to instantiate a query template given a KG? **Query Template** Knowledge Graph ((Anchor1, (Rel1, Rel2)), (Anchor2, (Rel3)) Lung ESR2 **Breast Cancer** Cancer Paclitaxel **Fulvestrant** Assoc TreatedBv Intersection Assoc **Fulvestrant Breast** Arimidex Cancer Projection Intersection ESR2 **Fulvestrant**

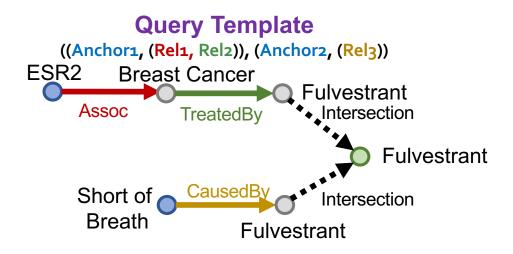
CausedBy

Then we look at the second branch and ground the **Projection edge** with the relation associated with Fulvestrant, e.g., CausedBy. Then we check what entities are connected to Fulvestrant with CausedBy: {Short of Breath}.



How to instantiate a query template given a KG? **Query Template** Knowledge Graph ((Anchor1, (Rel1, Rel2)), (Anchor2, (Rel3)) Lung ESR2 **Breast Cancer** Cancer Paclitaxel Fulvestrant Assoc **TreatedBv** Intersection Assoc **Fulvestrant Breast** Arimidex Cancer CausedB Short of Intersection ESR2 **Breath Fulvestrant Fulvestrant** TreatedBy Short of Ketamin We select entity from {Short of **Breath Breath**}, set it as the anchor node. CausedBy

How to instantiate a query template given a KG?



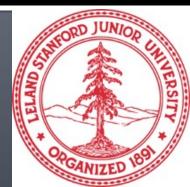
Now, we instantiated a **query** *q*!

q: ((e:ESR2, (r:Assoc, r:TreatedBy)), (e:Short of Breath, (r:CausedBy))

- The query *q* must have answers on the KG and one of the answers is the instantiated answer node: Fulvestrant.
- We may obtain the full set of answers $\llbracket q \rrbracket_G$ by KG traversal.
- We can sample negative answers $v' \notin \llbracket q \rrbracket_G$

Stanford CS224W: Example of Query2box

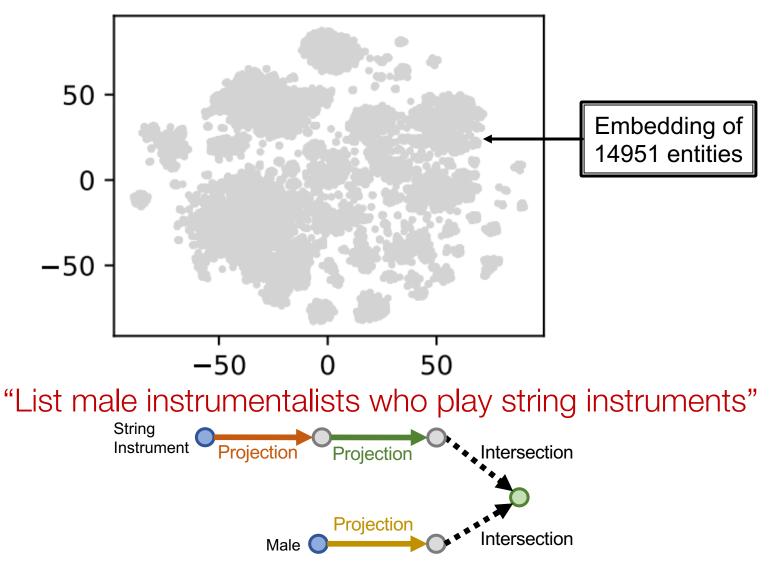
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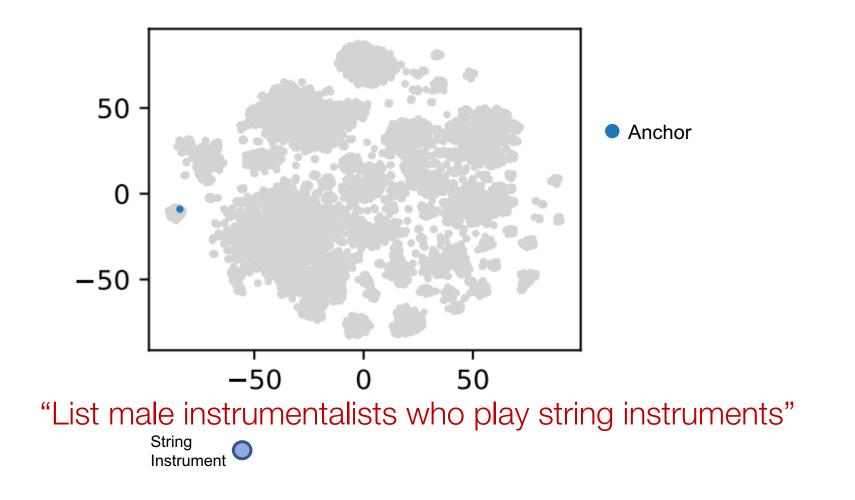
What do box embeddings actually learn?

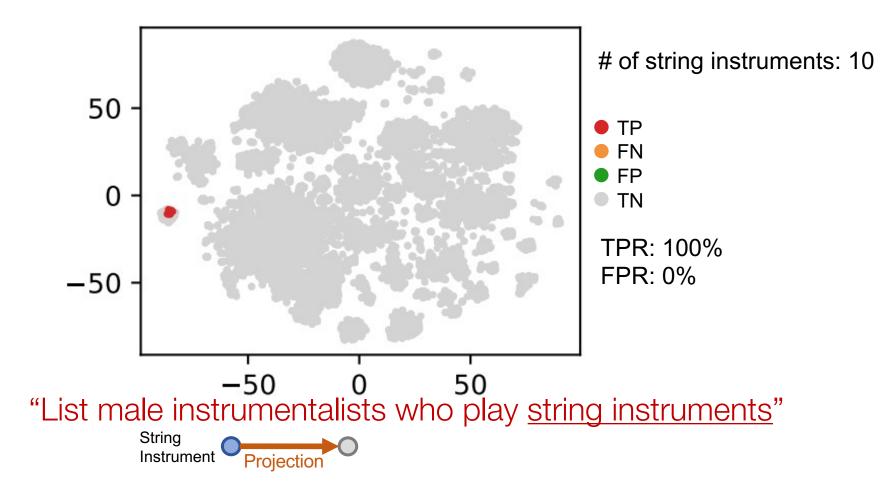
Example: "List male instrumentalists who play string instruments"

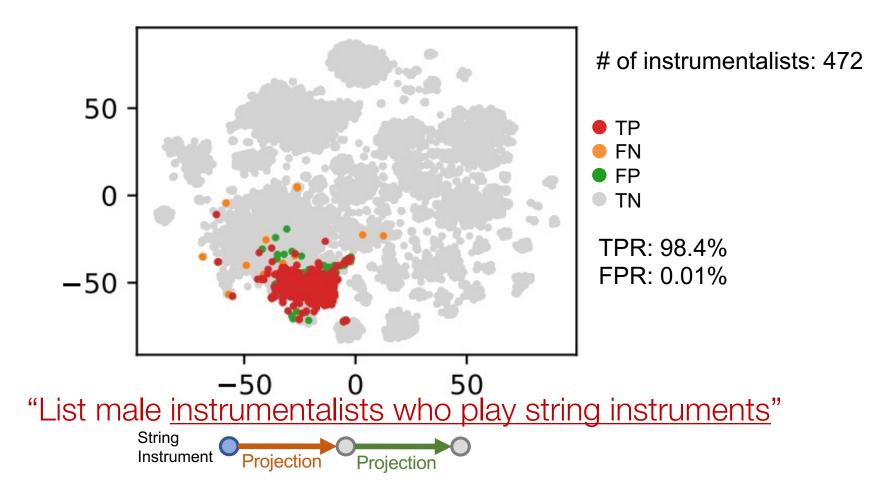
 We use t-SNE to reduce the embedding space to a 2-dimensional space, in order to visualize the query results

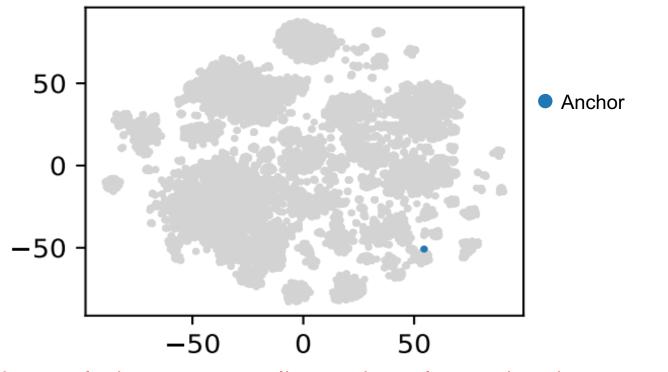


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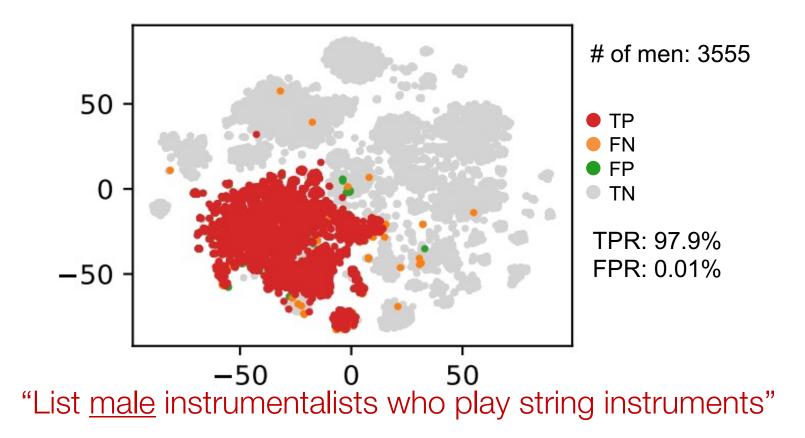






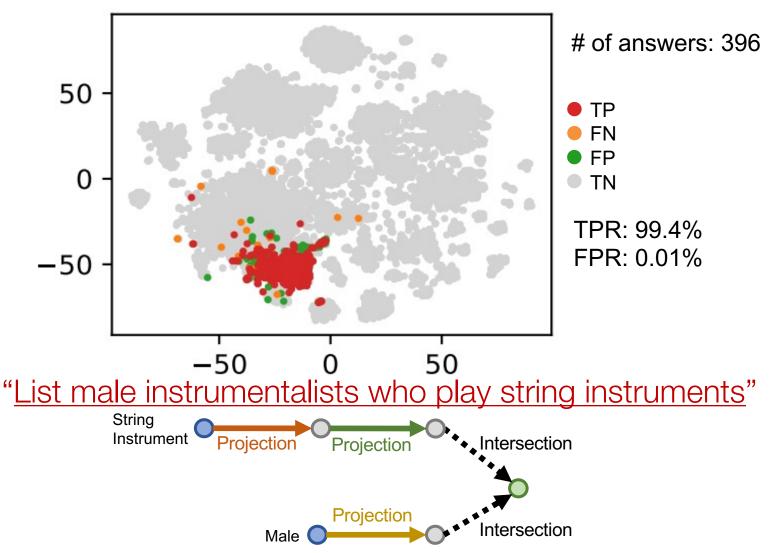
"List male instrumentalists who play string instruments"







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Summary

- We introduce answering predictive queries on large knowledge graphs.
- The key idea is to embed queries by navigating the embedding space!
 - We embed the query by composing learned operators
 - Embedding of the query is close to its answers in the embedding space