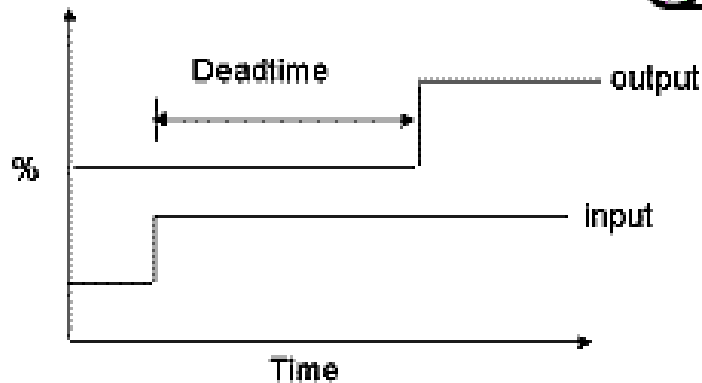
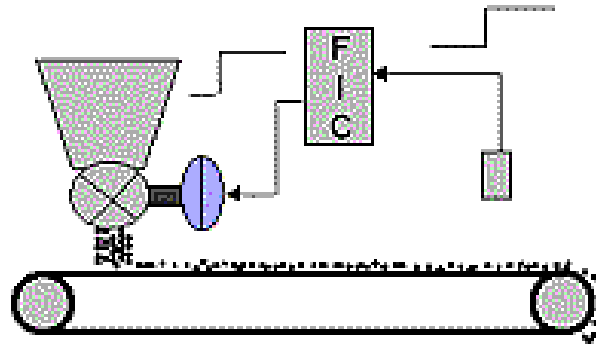
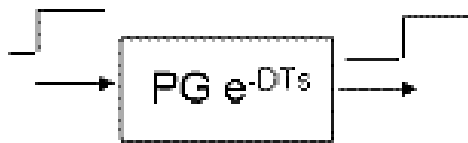


# Lecture 11 - Processes with Deadtime, Internal Model Control

- Processes with deadtime
- Model-reference control
- Deadtime compensation: Dahlin controller
- IMC
- Youla parametrization of all stabilizing controllers
- Nonlinear IMC
  - Receding Horizon - MPC - Lecture 14

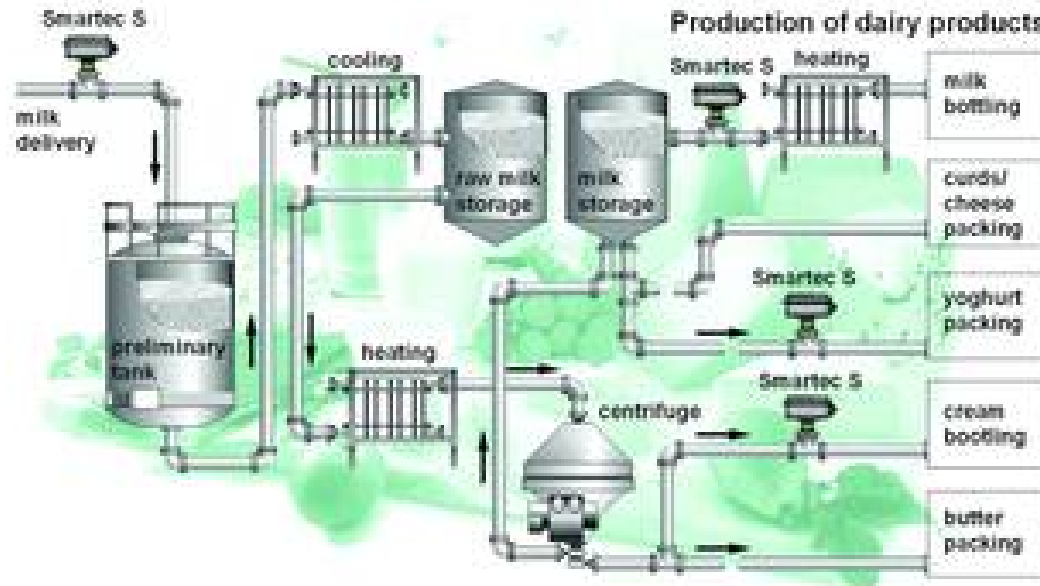
# Processes with Deadtime

- Examples: transport deadtime in paper, mining, oil
- Deadtime = transportation time



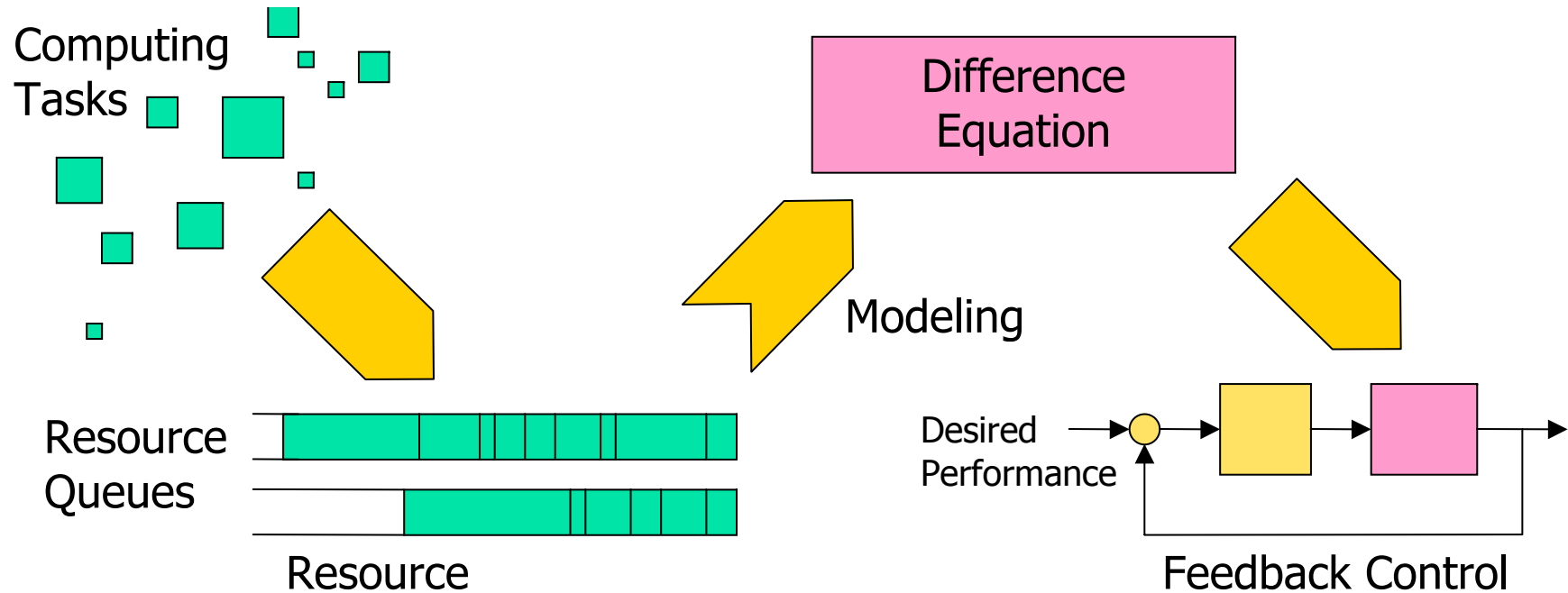
# Processes with Deadtime

- Example: transport deadtime in food processing



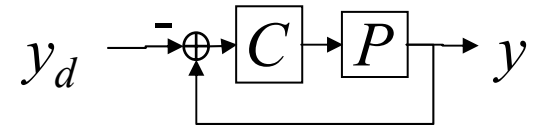
# Processes with Deadtime

- Example: resource allocation in computing



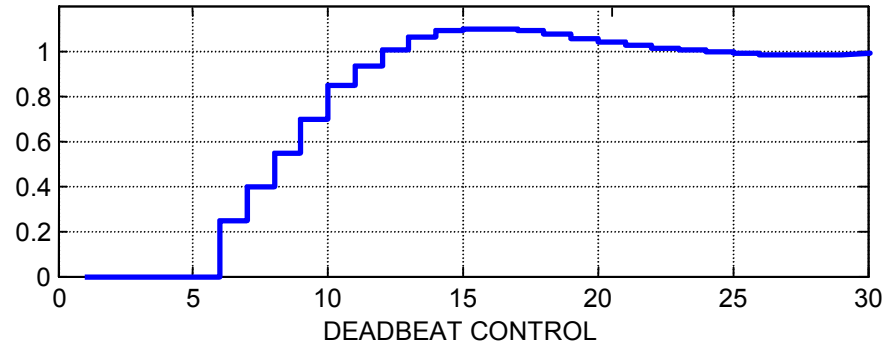
# Control of process with deadtime

- PI control of a deadtime process



PLANT:  $P = z^{-5}$  ; PI CONTROLLER:  $k_p = 0.3, k_i = 0.2$

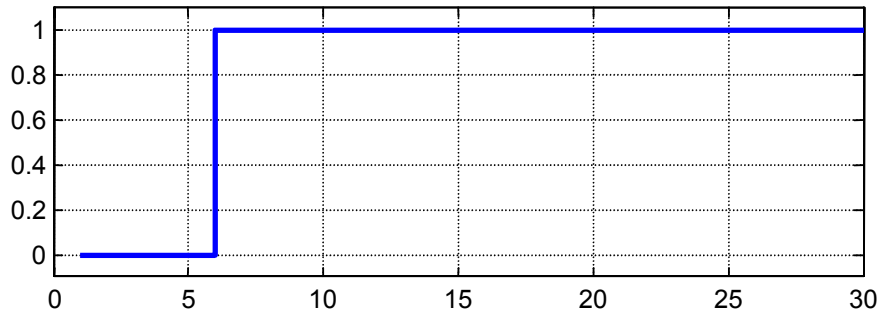
$P = e^{-sT_D}$  continuous time  
 $P = z^{-d}$  discrete time



- Can we do better?

- Make  $\frac{PC}{1+PC} = z^{-d}$
- Deadbeat controller

$$PC = \frac{z^{-d}}{1 - z^{-d}} \implies C = \frac{1}{1 - z^{-d}}$$



$$u(t) = u(t - d) + e(t)$$

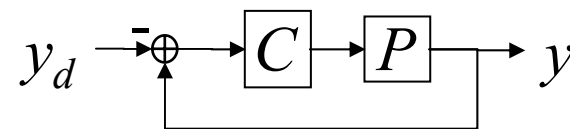
# Model-reference Control

- Deadbeat control has bad robustness, especially w.r.t. deadtime
- More general model-reference control approach
  - make the closed-loop transfer function as desired

$$\frac{P(z)C(z)}{1 + P(z)C(z)} = Q(z)$$

$Q(z)$  is the reference model for the closed loop

$$C(z) = \frac{1}{P(z)} \cdot \frac{Q(z)}{1 - Q(z)}$$



- Works if  $Q(z)$  includes a deadtime, at least as large as in  $P(z)$ . Then  $C(z)$  comes out causal.

# Causal Transfer Function

$$\begin{aligned} C(z) &= \frac{B(z)}{A(z)} = \frac{b_0 z^M + b_1 z^{M-1} + \dots + b_N}{z^N + a_1 z^{N-1} + \dots + a_N} \\ &= \frac{b_0 z^{M-N} + b_1 z^{M-N-1} + \dots + b_N z^{-N}}{1 + a_1 z^{-1} + \dots + a_N z^{-N}} \end{aligned}$$

- Causal implementation requires that  $N \geq M$

$$\underbrace{\left(1 + a_1 z^{-1} + \dots + a_N z^{-N}\right)}_{A(z)} u(t) = \underbrace{\left(b_0 z^{M-N} + b_1 z^{M-N-1} + \dots + b_N z^{-N}\right)}_{B(z)} e(t)$$

# Dahlin's Controller

- Eric Dahlin worked for IBM in San Jose (?) then for Measurex in Cupertino.

- Dahlin's controller, 1967

$$C(z) = \frac{1}{P(z)} \cdot \frac{Q(z)}{1-Q(z)}$$

$$P(z) = \frac{g(1-b)}{1-bz^{-1}} z^{-d}$$

- plant, generic first order response with deadtime

$$Q(z) = \frac{1-\alpha}{1-\alpha z^{-1}} z^{-d}$$

- reference model: 1<sup>st</sup> order+deadtime

$$C(z) = \frac{1-bz^{-1}}{g(1-b)} \cdot \frac{1-\alpha}{1-\alpha z^{-1} - (1-\alpha)z^{-d}}$$

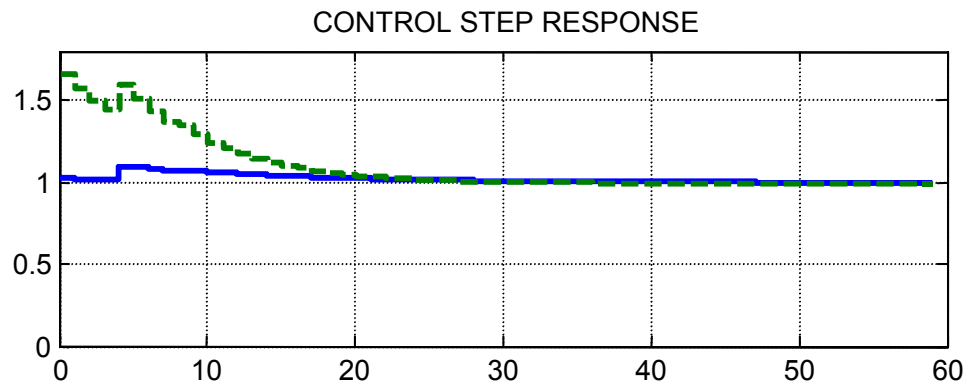
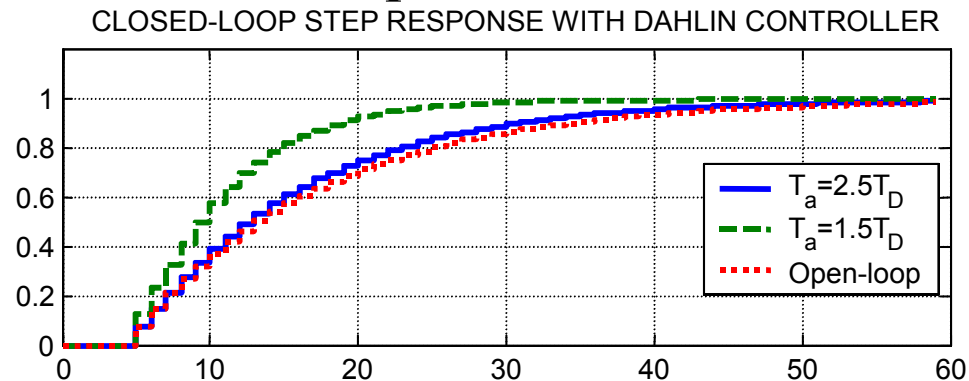
- Dahlin's controller

- Single tuning parameter:  $\alpha$  - tuned controller  
a.k.a.  $\lambda$  - tuned controller



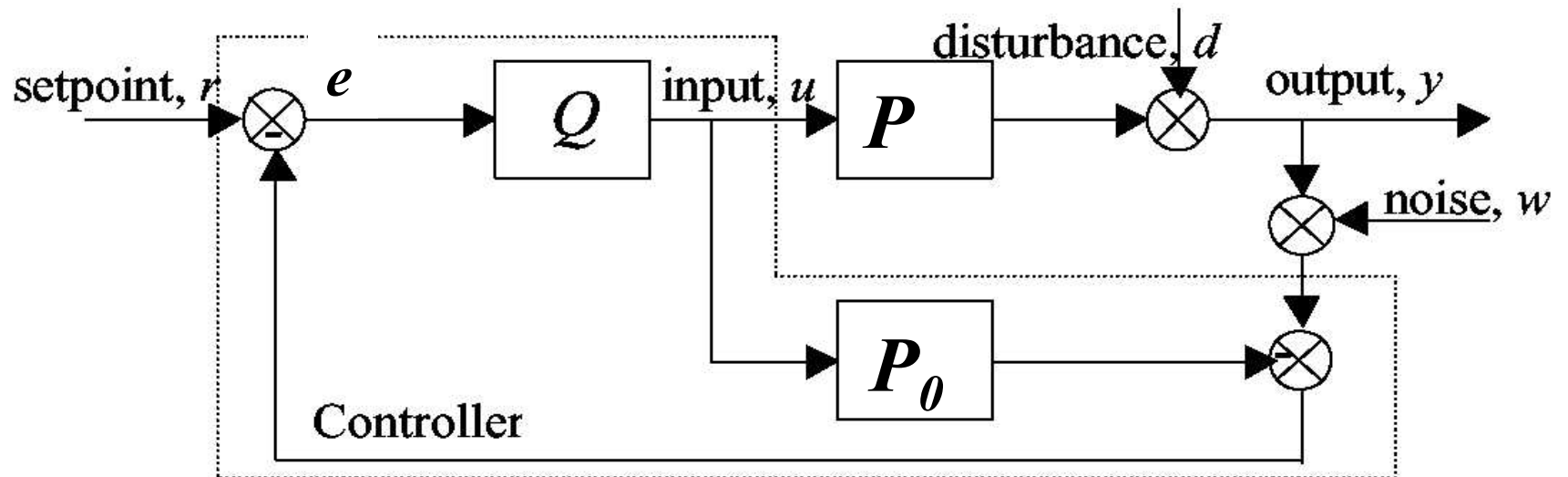
# Dahlin's Controller

- Dahlin's controller is broadly used through paper industry in supervisory control loops - Honeywell-Measurex, 60%.
- Direct use of the identified model parameters.
- Industrial tuning guidelines:  
Closed loop time constant = 1.5-2.5  
deadtime.



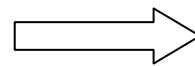
# Internal Model Control - IMC

General controller design approach; some use in process industry



$$e = r - (y - P_0 u)$$

$$u = Qe$$



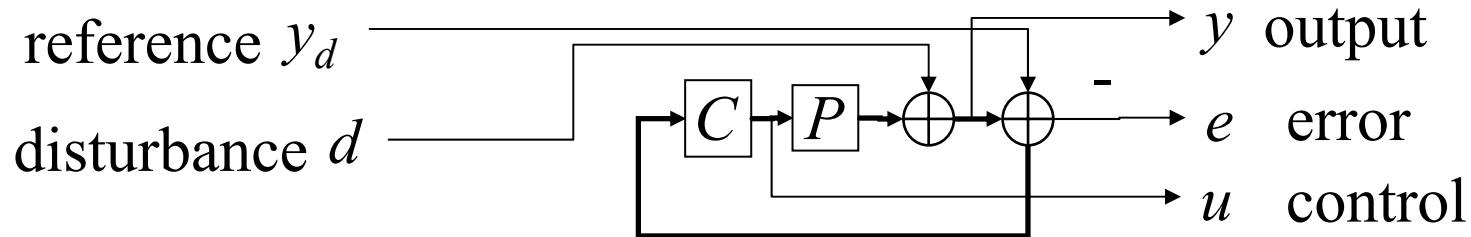
$$C = \frac{Q}{1 - QP_0}$$

- continuous time  $s$
- discrete time  $z$

Reference model:  $T = QP_0$

Filter  $Q$     Internal model:  $P_0$

# IMC and Youla parametrization



$$C = \frac{Q}{1 - QP_0}$$

• Sensitivities

$$S = 1 - QP_0 \quad d \rightarrow y$$

$$T = QP_0 \quad y_d \rightarrow y$$

$$S_u = Q \quad d \rightarrow u$$

$$Q = \frac{C}{1 + CP_0}$$

- If  $Q$  is stable, then  $S$ ,  $T$ , and the loop are stable
- If the loop is stable, then  $Q$  is stable

- Choosing various stable  $Q$  parameterizes all stabilizing controllers. This is called Youla parameterization
- Youla parameterization is valid for unstable systems as well

# Q-loopshaping

- Systematic controller design: select  $Q$  to achieve the controller design tradeoffs
- The approach used in modern advanced control design:  $H_2/H_\infty$ , LMI,  $H_\infty$  loopshaping

- Q-based loopshaping: 

$$S = 1 - QP_0 \quad S \ll 1 \Rightarrow Q \approx (P_0)^{-1} \quad \bullet \text{ in band}$$

- Recall system inversion 

# Q-loopshaping

- Loopshaping

$$\begin{array}{lll} S = 1 - QP_0 & S \ll 1 \Rightarrow Q \approx (P_0)^{-1} & \bullet \text{ in band} \\ T = QP_0 & T \ll 1 \Rightarrow QP_0 \ll 1 & \bullet \text{ out of band} \end{array}$$

- For a minimum phase plant

$$\begin{array}{ll} Q = P_0^\dagger = F(P_0)^{-1}, & T = QP_0 = F \\ F = \frac{1}{(1 + \lambda s)^n} & S = 1 - QP_0 = 1 - F \end{array}$$

- $F$  is called IMC filter,  $F \approx T$ , reference model for the output

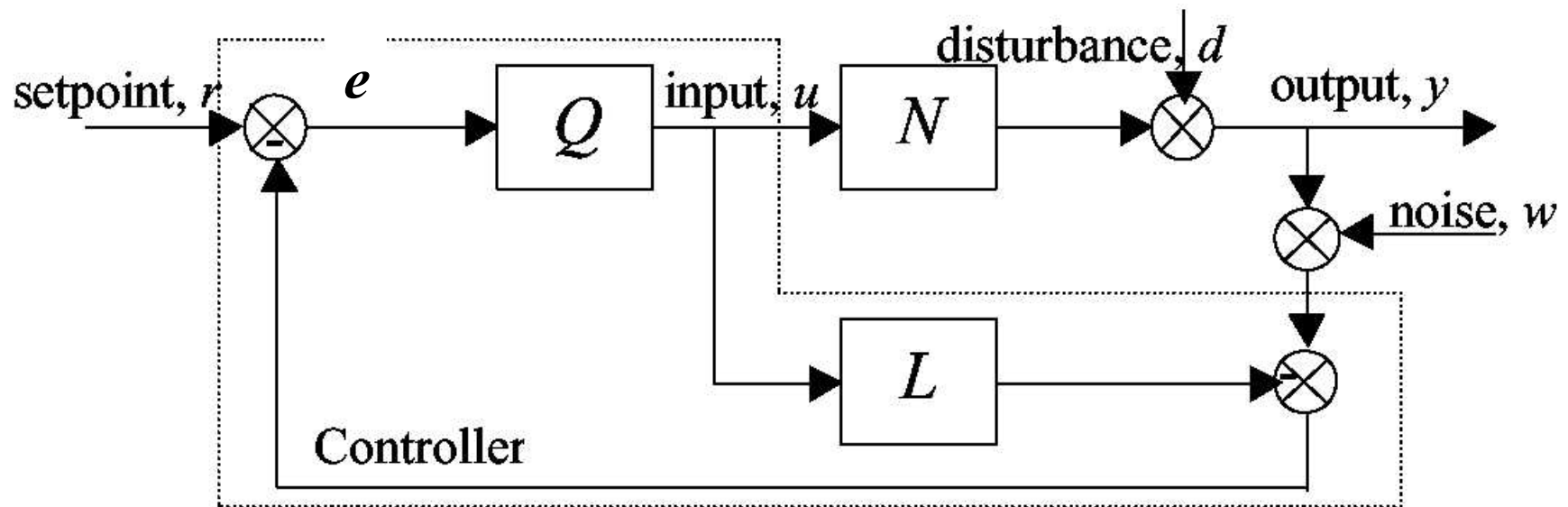
- Lambda-tuned IMC

# IMC extensions

- Multivariable processes
- Nonlinear process IMC
- Multivariable predictive control - Lecture 14

# Nonlinear process IMC

- Can be used for nonlinear processes
  - linear  $Q$
  - nonlinear model  $N$
  - linearized model  $L$



# Industrial applications of IMC

- Multivariable processes with complex dynamics
- Demonstrated and implemented in process control by academics and research groups in very large corporations.
- Not used commonly in process control (except Dahlin controller)
  - detailed analytical models are difficult to obtain
  - field support and maintenance
    - process changes, need to change the model
    - actuators/sensors off
    - add-on equipment



# Dynamic inversion in flight control

$$\dot{v} = F(x, v) + G(x, v)u$$

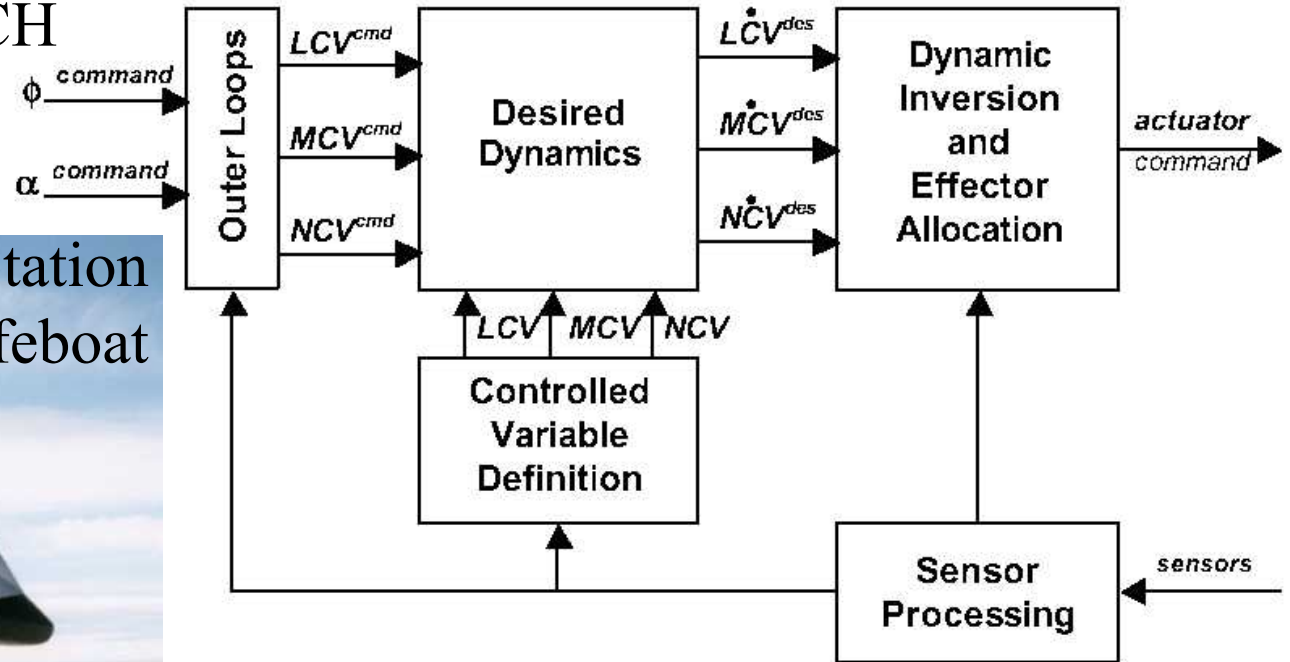
$$u = G^{-1}(\dot{v}^{des} - F)$$

Reference model:

$$v = \frac{1}{s} \dot{v}^{des}$$

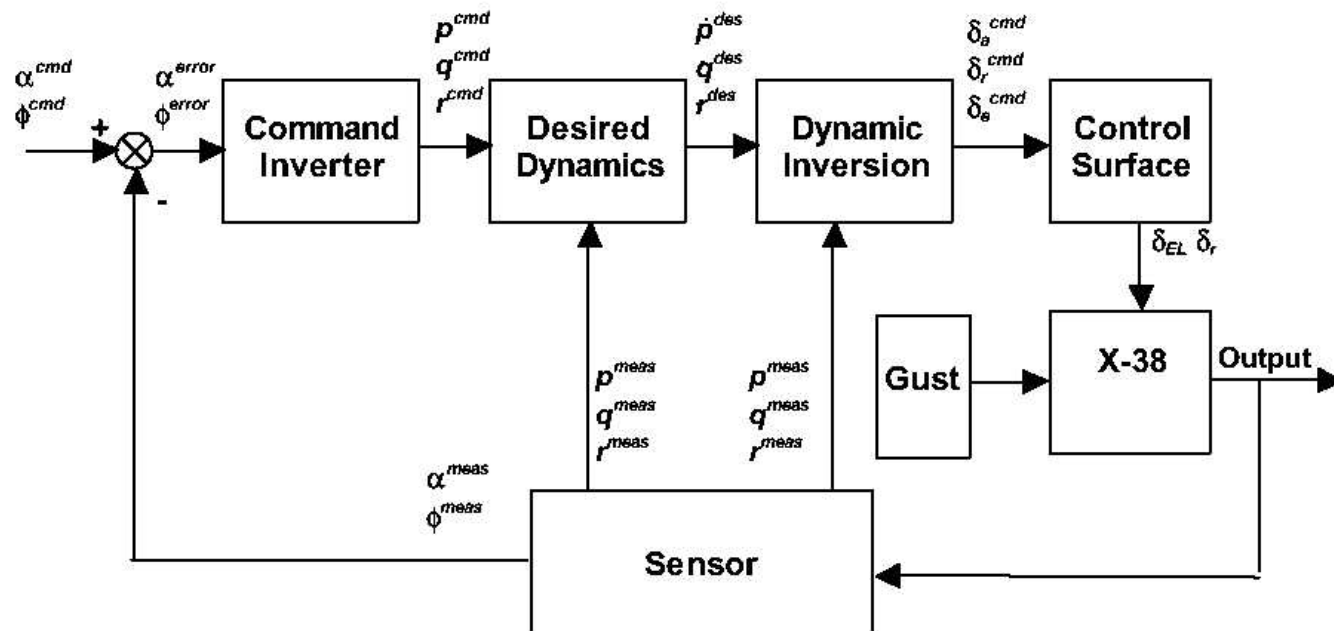
$$v = \begin{bmatrix} LCV \\ MCV \\ NCV \end{bmatrix}$$

- Honeywell MACH
- Dale Enns



# Dynamic inversion in flight control

- NASA JSC study for X-38
- Actuator allocation to get desired forces/moments
- Reference model (filter): vehicle handling and pilot 'feel'
- Formal robust design/analysis ( $\mu$ -analysis etc)



# Summary

- Dahlin controller is used in practice
  - easy to understand and apply
- IMC is not really used much
  - maintenance and support issues
  - is used in form of MPC – Lecture 14
- Youla parameterization is used as a basis of modern advanced control design methods.
  - Industrial use is very limited.
- Dynamic inversion is used for high-performance control of air and space vehicles
  - this was presented for breadth, the basic concept is simple
  - need to know more of advanced control theory to apply in practice